# Exploring the Axiverse by Gravitational Waves and Gamma Rays



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- H Yoshino, HK: PTP128, 153 (2012) [arXiv:1203.5070]
  - ibid: PTEP2014, 043E02 (2014) [arXiv:1312.2326]
    - K Kohiri, K Ioka, HK: in preparation

# Cosmology Workshop 2014 @ IAS HKUST (26 May 2014)

#### Find phenomena characteristic to string theory!! 10D SST/ 11D MT Geometric Geometric Compactification moduli **Branes/orientifolds Matter sector** Singularities moduli **Background flux Moduli Stabilisation SUSY** Landscape **Problem** Breaking Problem **Hidden Sector Visible Sector 4D Effective Theory Axionic** Inflation DE SM moduli Not stabilised

# **Axion Cosmophysics**

# Super-light axionic fields produce a rich vareity of new cosmophysical phenomena !!

#### Phenomena irrelevant to abundance

- Instabilities of black hole systems
- Influence on high-energy gamma ray propagation
- Solar activity/heat transport

- .....

### Phenomena sensitive to abundance

- Deformation of the cosmological power spectrum
- Rotation of the CMB polarisation
- Dark matter/ Dark radiations
- Dark energy

- ....

# **Characteristic Mass Scales**

### Compton wavelength= Horizon size (m=3H)

- Present t=t<sub>0</sub>:  $m_0=4.5 \times 10^{-33} \text{ eV}$
- CMB last scattering t=t<sub>ls</sub>:  $m_{ls}=0.7 \times 10^{-28} \text{ eV}$
- H recombination t=t<sub>rec</sub>:  $m_{rec}=1.2 \times 10^{-28} \text{ eV}$
- Equidensity time t=t<sub>eq</sub>:  $m_{eq} = 0.9 \times 10^{-27} \text{ eV}$
- Compton wavelength= BH size  $(1/m=M_{pl}^2/M)$ 
  - Supermassive BH M=10<sup>10</sup>  $M_{\odot}$ :  $m_{bh,max}$ =1.3× 10<sup>-20</sup> eV
  - Solar mass BH M=1  $M_{\odot}$ :  $m_{bh,min}$ =1.3 × 10<sup>-10</sup> eV
- QCD axion  $m \approx \Lambda_{QCD}^2/f_a$ 
  - $f_a = 10^{16} \text{ GeV:} m \sim 10^{-9} \text{ eV}$
  - $f_a = 10^{12} \text{ GeV: } m \sim 10^{-5} \text{ eV}$

Cf. 
$$m_a = 1 \text{eV} \times \left(\frac{6 \times 10^6 \text{GeV}}{f_a}\right)$$

## Contents

- $\checkmark$  Axion Cosmophysics
- Superradiance Instability of a Rotating BH
- Axionic Bose Nova
- Constraints from GW Experiments
- Gamma Ray Astronomy vs CIRB
- Making the Universe Transparent by Axions
- Summary

# Axionic Superradiance Instability of Black Holes

## Superradiance

Scalar field around a Kerr BH

$$(\Box - \mu^2)\Phi = 0; \quad \Phi \propto e^{-i\omega t + im\phi}$$

KG flux across the future horizon

$$k = \xi + \Omega_h \eta; \quad \xi = \partial_t, \quad \eta = \partial_\phi$$
$$I_{\mathscr{H}^+} = \int_{\mathscr{H}^+} (ik^\mu) \Phi^* \overset{\leftrightarrow}{\partial}_\mu \Phi = (\omega - \Omega_h m) |C|^2$$

Flux across the horizon can become negative !!

Superradiance

$$\omega |A|_{\mathscr{I}^+}^2 + (\omega - \Omega_h m) |C|^2 = \omega |A|_{\mathscr{I}^-}^2$$

$$\omega - m\Omega_h < 0 \Rightarrow \quad I_{\mathcal{I}^+} > I_{\mathcal{I}^-}$$



## Superradiance Instability

Bound state modes of a massive scalar field around a Kerr BH become unstable due to superradiance.



[Damour, Deruelle, Ruffini (1976) ]

Zouros TJM, Eardley DM 19

# Instability Growth Rate

**Analytic Estimates** 

[Zouras & Eardley (1979), Detwiler (1980)]

$$\frac{\tau}{M} \approx \begin{cases} 10^7 e^{1.84\alpha_g} \\ 24 \left(\frac{a}{M}\right)^{-1} (\alpha_g) \end{cases}$$

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$$; \alpha_g \gg 1, \ a/M = 1 ; \alpha_g \ll 1, \qquad (\alpha_g = \mu M)$$

### **General Features**

- The growth rate is greatest for Mµ <0.5.</li>
- The mode with l=m=1 is most unstable:
- The maximum growth rate at a=0.99 is

 $\tau \sim 10^7 M$ 

 $M_{\odot} \Rightarrow au \sim 1$ minute  $10^6 M_{\odot} \Rightarrow au \sim 2$ years



Dolan SR(2007)PRD76,084001

### **G-Atom**



Arvanitaki A, Dubovsky S: arXiv:1004.3558

## Fate of G-Atom?



# » Axionic Bose Nova

## **Non-linear Effects**

Action of the axion field

$$S = \int d^4x \sqrt{-g} \left[ -\frac{1}{2} (\nabla \Phi)^2 - \frac{\mu^2 f_a^2}{2} \sin^2 \left( \Phi / f_a \right) \right]$$

Estimation by Non-relativistic Approximation

$$\Phi \simeq \frac{1}{\sqrt{2\mu}} \left( e^{-i\mu t} \psi + e^{i\mu t} \psi^* \right)$$
Averaging S over a time scale >> 1/µ
$$S_{\rm NR} = \int d^4 x \left[ i\psi^* \partial_t \psi - \frac{1}{2\mu} \partial_i \psi \partial_i \psi^* - \mu \Phi_g \psi^* \psi + \frac{1}{16f_a^2} (\psi^* \psi)^2 \right]$$
Attractive interaction
$$\propto E_a^2$$

# Behavior of the Energy Flux into BH

Our direct 3D simulations reproduced the SR instability growth rate obtained by the Leaver method with sufficient precisions.



## Full Relativistic 3D Numerical Simulations

### Example: I=m=2 mode



## Summary of the Simulation: I=m=2



- When the peak value is sufficiently large, fairly large amount of axion cloud (20% of total energy) suddenly falls into the black hole in a relatively short time scale.
- This "bosenova implosion" occurs when  $E_a/M \approx 10^{-3} (f_a/10^{16} {\rm GeV})^2 \iff |\Phi_{\max}(0)/f_a| \sim 0.72$

# Gravitational Wave Emissions



## Does the GW Emission Stop Instability?

### Estimation by Quadrupole Formula

For superradiant modes, however, level transitions are in general suppressed, and 2 axions -> graviton process is dominant.

We have to estimate the GW emission rate by this 2 axions -> graviton process.

### GW Energy Flux Formula in a Kerr Background

The formula for evaluating the amplitude

$$\triangle_L \psi_{\mu\nu} = 16\pi G T_{\mu\nu}$$

$$\int_{\partial D} \left( h_{ab}^* \nabla_c \psi^{ab} - \psi^{ab} \nabla_c h_{ab}^* \right) n^c d\Sigma = -16\pi G \int_D h_{ab}^* T^{ab} \sqrt{-g} d^4 x$$
Physical perturbation

Homogeneous solution



## Axion cloud in I = m = 2 mode

• 
$$(\tilde{\ell}, \tilde{m}) = (4, 4), (P = +1)$$
  
•  $(\tilde{\ell}, \tilde{m}) = (5, 4), (P = -1)$   
•  $(\tilde{\ell}, \tilde{m}) = (6, 4), (P = +1)$   
•  $(\tilde{\ell}, \tilde{m}) = (7, 4), (P = -1)$ 



# GW emissions do not hider the occurrence of the bose nova collapse!!

### Can We Observe GWs from Axion Bosenova?

Estimation by Quadrupole Formula

$$h \approx 8 \times 10^{-23} \left(\frac{\epsilon}{10^{-3}}\right) \left(\frac{c^3}{GM\omega}\right) \left(\frac{10 \text{kpc}}{d}\right) \left(\frac{M}{10M_{\odot}}\right) \left(\frac{3\alpha_g}{l+1}\right)^5$$
$$\approx 8 \times 10^{-21} \left(\frac{\epsilon}{10^{-3}}\right) \left(\frac{c^3}{GM\omega}\right) \left(\frac{10 \text{Mpc}}{d}\right) \left(\frac{M}{10^6M_{\odot}}\right) \left(\frac{3\alpha_g}{l+1}\right)^5$$

### Examples

Cygnus X-1

 $M = 14.8 \pm 1.0 M_{\odot}, \quad a/M \gtrsim 0.9$  $d = 1.86 \mathrm{kpc}$ 

$$\Delta t \approx 100M \approx 7.3 \text{ ms}$$
  
$$\Rightarrow \quad h\Delta t^{1/2} \approx 10^{-23} \text{Hz}^{-1/2}$$
$$(\alpha_g = 0.7, \quad l = 2)$$



### Sagitairus A\*

 $M \approx 10^6 M_{\odot}, \quad d \approx 8 \text{kpc}$  $\Delta t \approx 100 M \approx 500 \text{ s}$  $\Rightarrow \quad h \Delta t^{1/2} \approx 10^{-17} \text{Hz}^{-1/2}$ 



# GWs during the SR Growth Phase

# For stationary GWs, we can gain S/N by long time observations.

When the duration of observation/SR phase is T, and the frequency range of the GWs is  $\Delta v$ , the S/N is



## Axion cloud in $I = m = 1 \mod e$

• 
$$(\tilde{\ell}, \tilde{m}) = (2, 2), \ (P = +1)$$
  
•  $(\tilde{\ell}, \tilde{m}) = (3, 2), \ (P = -1)$   
□  $(\tilde{\ell}, \tilde{m}) = (4, 2), \ (P = +1)$   
•  $(\tilde{\ell}, \tilde{m}) = (5, 2), \ (P = -1)$ 



### Caveat

- When the axion cloud grows, nonlinear effects become important and produce modulations with intermediate periods.
- This modulation produces a frequency dispersion

$$\Delta \nu \sim \frac{1}{\Delta T} \sim \frac{1}{1000M} \sim \frac{10^4}{T}$$
$$\frac{h\sqrt{T}}{T} \sim 3 \times 10^{-25} \mathrm{Hz}^{-1/2}$$

 This difficulty will be resolve by the matched filtering to simulations.



# Gamma Ray Astropysics vs CIRB



### Gamma-Ray Horizon



### Deformation of the Gamma Ray Spectrum



PS Coppi and AF Aharonian: ApJ 487, L9 (1997).

*a* : 
$$\epsilon^2 n(\epsilon, 0) = 10^{-3} \text{eV/cm}^3$$
  
*c* :  $\epsilon^2 n(\epsilon, 0) = 10^{-2} \text{eV/cm}^3$ 

 $z=0.1 \Leftrightarrow L \simeq 430 \text{ Mpc}$ 

Cf. 
$$\rho_{\rm CMB} = 0.26 \, {\rm eV}/{\rm cm}^3$$

### Observation of EBL absorption in the spectra of AGNs

- HESS observation: power-law fitting
  - Two blazars with strong absorption were observed.
- Fermi-LAT observation: power-law fitting

[Ackermann at al (Fermi Coll): Science 338, 1190 (2012)]

The spectral deformation due to absorption has been observed for 150 blazars of BL Lac type.

(z=0.03 -1.6, E= 40GeV - 100 GeV)

Multi-frequency observation: synchrotron/SSC model

[Dominguez et al: apj770, 88 (2013)]

Opacity around a TeV range is determined by observations of 15 blazars from radio to Gamma-ray (Fermi-LAT & IACTs).

The opacity is consistent with the minimum EBL model.

(z=0.031 – 0.5, E=200 GeV – 10 TeV)

## Detection of the Absorption by Fermi

#### Sample: 150 blazers of BL Lac type (z=0.03 -1.6, E= 40GeV - 100 GeV)

Fig. 1. Measurement, at the 68 and 95% confidence levels (including systematic uncertainties added in quadrature), of the opacity  $\tau_{vv}$  from the best fits to the Fermi data compared with predictions of EBL models. The plot shows the measurement at  $z \approx 1$ , which is the average redshift of the most constraining redshift interval (i.e.,  $0.5 \le z <$ 1.6). The Fermi-LAT measurement was derived combining the limits on the best-fit EBL models. The downward arrow represents the 95% upper limit on the opacity at z = 1.05 derived in (13). For clarity, this figure shows only a selection of the models we tested; the full list is reported in table S1. The EBL models of (49), which are not defined for  $E \ge 250/$ (1 + z) GeV and thus could not be used, are reported here for completeness.



Ackermann at al (Fermi Coll): Science 338, 1190 (2012)

# Rejection of the intrinsic origin

**Fig. 2.** Absorption feature present in the spectra of BL Lac objects as a function of increasing redshift (data points, from top to bottom). The dashed curves show the attenuation expected for the sample of sources by averaging, in each redshift and energy bin, the opacities of the sample [the model of (*7*) was used] and multiplying this average by the best-fit scaling parameter *b* obtained independently in each redshift interval. The vertical line shows the critical energy  $E_{crit}$  below which  $\leq$  5% of the source photons are absorbed by the EBL. The thin solid curve represents the best-fit model, assuming that all the sources have an intrinsic exponential cutoff and that blazars follow the blazar sequence model of (*32, 33*).

Ackermann at al (Fermi Coll): Science 338, 1190 (2012)



# Observed CGRH: Eo(z)

Dominguez et al: apj770, 88 (2013)



**Figure 2.** Estimation of the CGRH from every blazar in our sample plotted with blue circles. The statistical uncertainties are shown with darker blue lines and the statistical plus 20% of systematic uncertainties are shown with lighter blue lines. The CGRH calculated from the EBL model described in Domínguez et al. (2011a) is plotted with a red thick line. The shaded regions show the uncertainties from the EBL modeling, which were derived from observed data.

# EBL models and measurements



Dominguez A et al: mnras 410, 2556 (2011)









#### Axion Cosmophysics AIU2012, KEK, Nov 6-9, 2012

### The CIBER Collaboration



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## Zodiacal Light



- Scattered sun light by interplanetary dust
- Strong ecliptic latitude dependence



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### Launch vehicle & orbit







- Rocket experiment CIBER
- We have already flown CIBER three times. (Feb 2009, Jul 2010 and Mar 2012)
- All flights were successful.
- Analyzing the data.



### New measurements of CIRB by the rocket experiment CIBER



# Making the Universe Transparent by Axions



## **Axion-Photon Conversion**

• Chern-Simons coupling of axion with EM fields

$$\mathscr{L} = -\frac{1}{2}(\partial a)^{2} - \frac{1}{2}m_{a}^{2}a^{2} - \frac{1}{2}F \cdot F - \frac{1}{2}g_{a\gamma}aF \cdot *F$$
$$\mathscr{L} = \frac{1}{2}|\dot{a}|^{2} - \frac{1}{2}\omega_{a}^{2}|a|^{2} + \frac{1}{2}|\dot{A}|^{2} - \frac{1}{2}|\mathbf{k} \times \mathbf{A}|^{2} - g_{a\gamma}a\mathbf{B}_{0} \cdot \dot{A}$$

• Wave equations in plasma

$$\begin{split} \epsilon \partial_t^2 \boldsymbol{E} &= c^2 \boldsymbol{k} \times (\mu^{-1} \boldsymbol{k} \times \boldsymbol{E}) - \frac{\omega_p^2 \omega^2}{\omega^2 - \omega_g^2} \boldsymbol{E} - g_{a\gamma} \omega^2 a \boldsymbol{B}_0 \\ &+ \frac{\omega_p^2}{\omega^2 - \omega_g^2} \left\{ i \omega \omega_g \boldsymbol{E} \times \boldsymbol{b} + \omega_g^2 (\boldsymbol{E} \cdot \boldsymbol{b}) \boldsymbol{b} \right\}, \\ \partial_t^2 a &= -\omega_a^2 a + g_{a\gamma} \boldsymbol{E} \cdot \boldsymbol{B}_0. \end{split}$$

0

0

where

$$\omega_g = \frac{eB_0}{cm_e}, \quad \omega_p^2 = \frac{4\pi n_e e^2}{m_e}.$$

### High frequency limit

When a wave propagates nearly at the speed of light, we have  $\partial_t X \approx -\partial_z X \approx -ikX$ 

$$(\partial_t^2 - \partial_z^2)X(t, z) = (\partial_t - \partial_z)(\partial_t + \partial_z)X \simeq -2ik(\partial_t + \partial_z)X = -2ik\frac{dX}{dz}$$

Hence, the wave equations can be approximated by a first-order system of ODEs as

$$\left(-i\frac{d}{dz} - \mathscr{M}\right) \begin{pmatrix} A_{\perp} \\ A_{\prime\prime} \\ a \end{pmatrix} = 0; \quad \mathscr{M} = \begin{pmatrix} \Delta_{\perp} & \Delta_{R} & 0 \\ \Delta_{R} & \Delta_{\prime\prime} & \Delta_{B} \\ 0 & \Delta_{B} & \Delta_{a} \end{pmatrix}$$

where

$$\Delta_{\perp} = \Delta_{\rm pl} + \Delta_{\rm CM}^{\perp}, \quad \Delta_{\prime\prime} = \Delta_{\rm pl} + \Delta_{\rm CM}^{\prime\prime}, \quad \Delta_{\rm pl} = \omega_{\rm pl}^2 / (2E)$$
$$\Delta_B = g_{a\gamma} B/2, \quad \Delta_a \simeq m_a^2 / (2E)$$

### Mass eigenvalues

Neglecting the Faraday rotation, the mass matrix can be diagonalised as



### Non-resonant transition

Neglecting the change of  $\,\theta,\,\lambda_1,\,\lambda_2$  , the solution is

$$\begin{pmatrix} A_{//}(z) \\ a(z) \end{pmatrix} = R(\theta) \begin{pmatrix} e^{i\lambda_1 z} & 0 \\ 0 & e^{i\lambda_2 z} \end{pmatrix} R(-\theta) \begin{pmatrix} A_{//}(0) \\ a(0) \end{pmatrix}.$$

Hence, the conversion rate is

$$P_{\gamma \to a} = P_0 := \sin^2(2\theta) \sin^2 \frac{s \,\Delta_{\rm osc}}{2} = \frac{4\Delta_B^2}{\Delta_{\rm osc}^2} \sin^2 \frac{s \,\Delta_{\rm osc}}{2}$$

where

$$\Delta_{\rm osc}^2 = (\Delta_{\rm CM} + \Delta_{\rm pl} - \Delta_a)^2 + 4\Delta_B^2.$$

Resonant transition (non-uniform case)

$$2\pi |\Delta'_{\rm pl} + \Delta'_{\rm CM}| \lesssim \Delta_B^2 \Rightarrow P_{\gamma \to a} = O(1)$$

## VHE gamma rays from AGNs can penetrate the CBR barrier



# **Conditions for Strong Conversion**

### • Conversion rate

$$P_{0} = \frac{1}{1 + (E_{*}/E)^{2}} \sin^{2} \left( g_{a\gamma} B \left[ 1 + (E_{*}/E)^{2} \right]^{1/2} \frac{L}{2} \right),$$
  
$$E_{*} := \frac{|m_{a}^{2} - m_{\gamma}^{2}|}{2g_{a\gamma} B} \simeq 0.7 \frac{|m_{a}^{2} - m_{\gamma}^{2}|}{(10^{-7} \text{eV})^{2}} \left( \frac{10\mu\text{G}}{B} \right) \left( \frac{g_{a\gamma}^{-1}}{10^{11}\text{GeV}} \right) \text{TeV}$$

Condition 1: Near resonance

$$E \gtrsim E_* \Rightarrow g_{a\gamma} \cdot 10^{11} \text{GeV} \gtrsim 0.7 \left(\frac{m_a}{10^{-7} \text{eV}}\right)^2 \frac{1}{B_{10\mu\text{G}} E_{\text{TeV}}}$$

Consition 2: Sufficient oscillations

$$g_{a\gamma}BL \gtrsim \pi \Rightarrow \quad g_{a\gamma} \cdot 10^{11} \text{GeV} \gtrsim 0.3 \frac{1}{B_{10\mu\text{G}}L_{10\text{kpc}}}$$

# **Axion solution**

Kohri K, Kodama H, Ioka K: in preparation



# Summary

# Summary

- Axionic Superradiance Instability
  - Superradiance instability produces recurrent phenomena of a linear growth of an axionic cloud around a rotating BH that is terminated and reset by bose nova collapse, if the axion mass  $m_a$  and the BH mass M satisfy the condition  $GMm_a = O(1)$ .
  - GW emissions from these phenomena can be detected by the ongoing and planned GW interferometers such as LIGO, KAGRA and the advanced LIGO, if they happen inside our galaxy.
  - Even null detection of GWs by these experiments can exclude axions with mass around 10<sup>-10</sup> eV.
- Gamma Ray Astrophysics
  - Blazar observations by FERMI-LAT and IACTs are quite inconsistent with the flux of CIRB measured by CIBER.
  - In order to resolve this inconsistency by axion, its mass and coupling are strongly constrained:  $m_a = 10^{-9} \sim 10^{-6} \text{ eV}$ ,  $g_{a\gamma} = 10^{-10} \text{ GeV}^{-1}$