

Cosmological Implications from BICEP2

Qing-Guo Huang

based on some works done with
Cheng Cheng and Wen Zhao

New perspectives on cosmology, HKUST-IAS
ITP-CAS, Beijing
05/21/2014

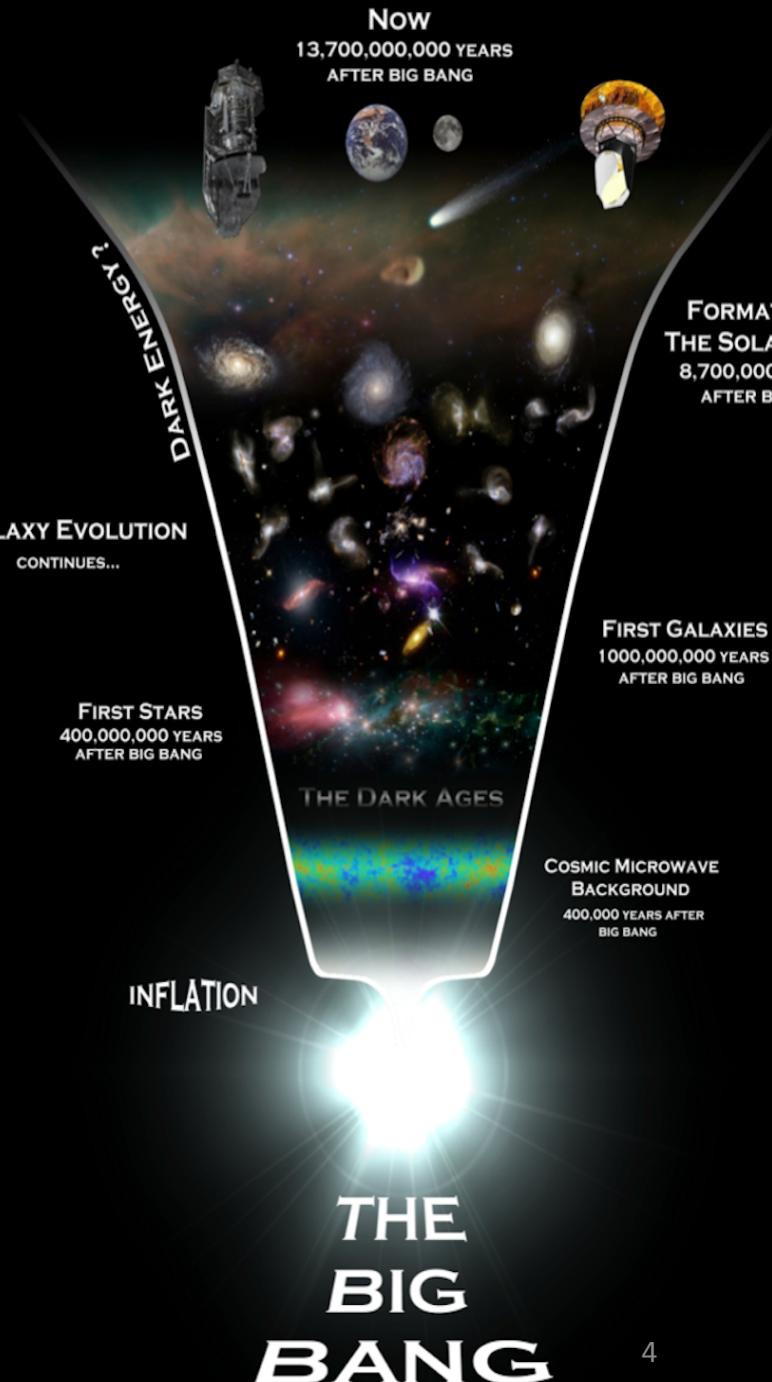
Outline

- Probing the inflationary universe from low-l CMB data
- How to reconcile Planck with BICEP2
- The tilt of relic gravitational waves power spectrum
- Summary

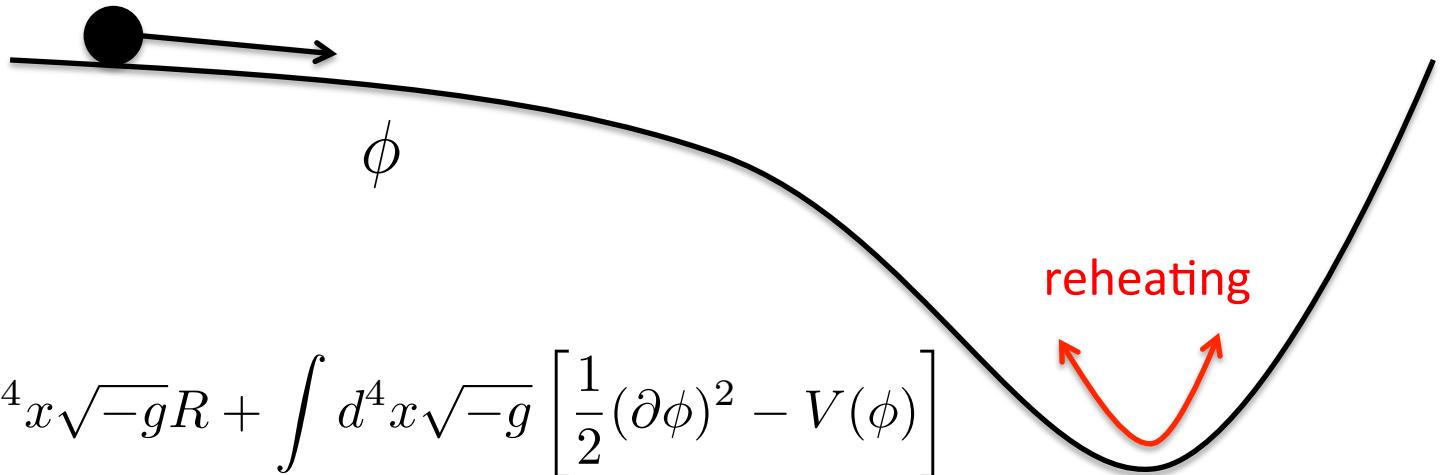
Probing the inflationary universe from low-l CMB data

Successes of Inflation:

- The Universe is big
- Homogeneity and isotropy
- Flatness problem
- Why no magnetic monopole?
- Nearly scale-invariant, adiabatic and Gaussian density perturbations.
- Nearly scale-invariant relic gravitational waves.
-



Slow-Roll Inflation



$$S = \frac{M_p^2}{2} \int d^4x \sqrt{-g} R + \int d^4x \sqrt{-g} \left[\frac{1}{2} (\partial\phi)^2 - V(\phi) \right]$$

$$H^2 = \frac{1}{3M_p^2} \left(\frac{1}{2} \dot{\phi}^2 + V(\phi) \right) \quad \ddot{\phi} + 3H\dot{\phi} + V'(\phi) = 0$$

$$\epsilon = \frac{M_p^2}{2} \left(\frac{V'}{V} \right)^2 \ll 1$$

$$\left| \eta = M_p^2 \frac{V''}{V} \right| \ll 1$$

$$H^2 \simeq \frac{V}{3M_p^2}$$

$$3H\dot{\phi} \simeq -V'$$

$$a(t) \sim e^{Ht}$$

- There are three kinds of perturbations: scalar, vector and tensor (gravitational waves) perturbations.
- At the linear order, these three kinds of perturbations evolve independently and therefore we can analyze them separately.
- Since there are no rotational velocity fields during inflation, the vector perturbations are not excited.

Scalar perturbations:

$$\zeta = \delta N = H\delta t = \frac{H}{\dot{\phi}}\delta\phi = -\frac{1}{\sqrt{2\epsilon}M_p}\delta\phi$$

$$P_s = \frac{H^2/M_p^2}{8\pi^2\epsilon}$$

$$n_s \equiv 1 + \frac{d \ln P_s}{d \ln k} = 1 - 6\epsilon + 2\eta$$

Gravitational waves:

$$P_t = \frac{H^2/M_p^2}{\pi^2/2}$$

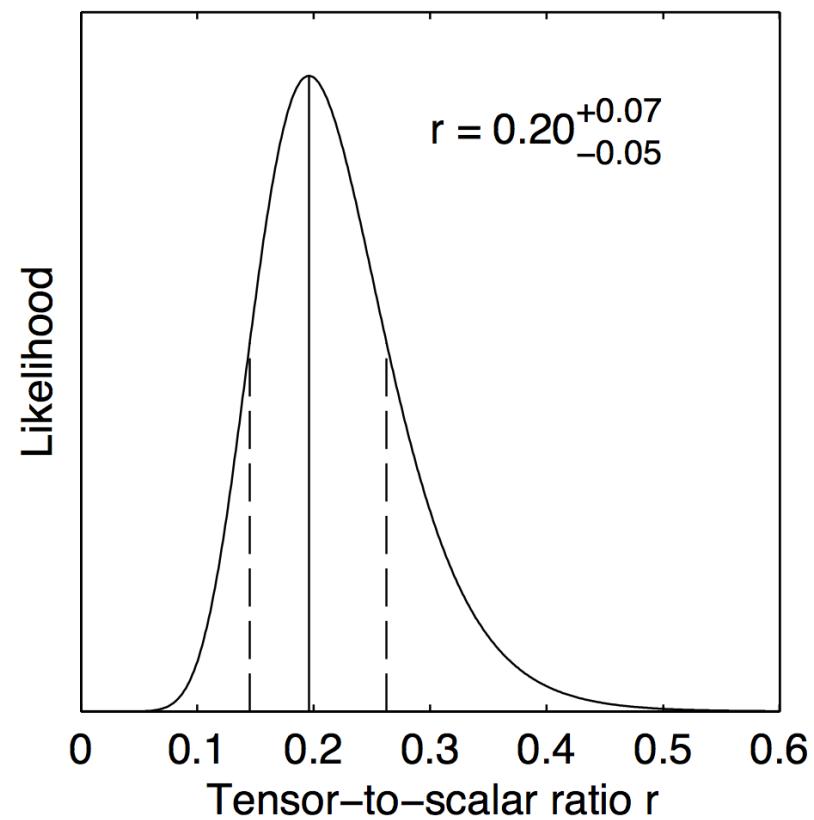
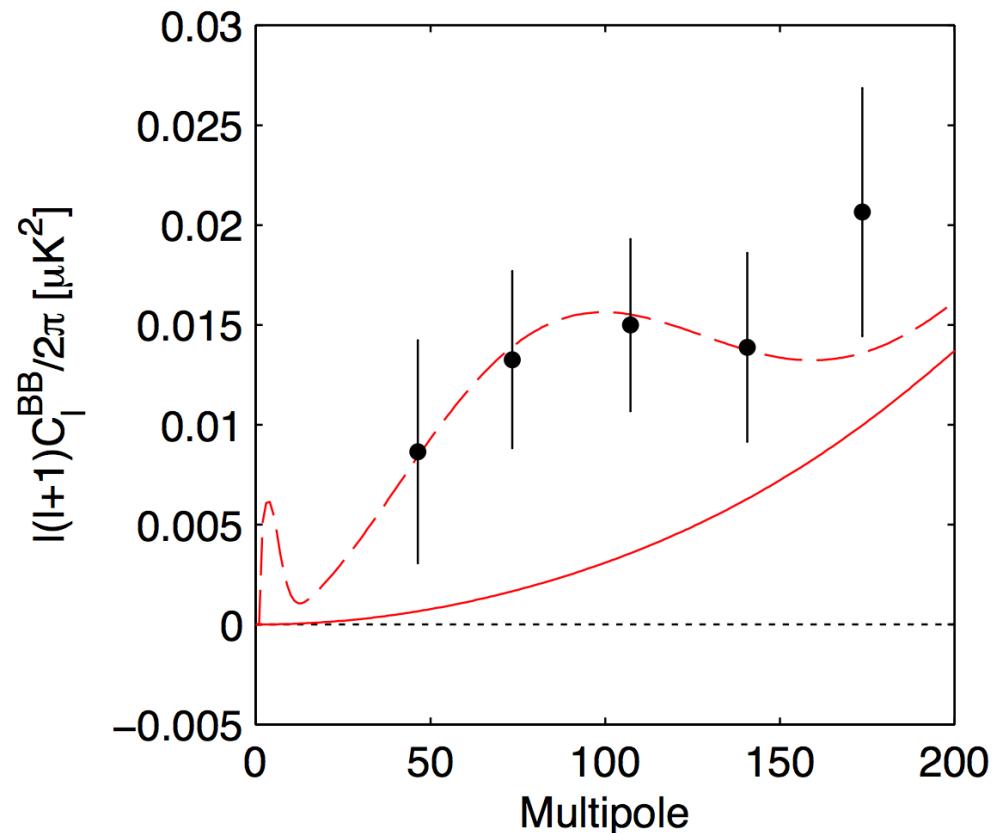
$$r = P_t/P_s = 16\epsilon$$

$$n_t = -2\epsilon$$

$$n_t = -r/8$$

Nearly scale-invariant!

Discovery of relic gravitational waves (BICEP2)



$r = 0.2^{+0.07}_{-0.05}$, with $r = 0$ is disfavored at 7.0σ

BICEP2 collaboration, arXiv:1403.3985

Naturalness of inflation?

$$\frac{\Delta T}{T} \sim 10^{-5} \quad \longleftrightarrow \quad \text{A small dimensionless parameter}$$

Lyth Bound:

$$\epsilon \equiv \frac{M_p^2}{2} \left(\frac{V'}{V} \right)^2 = \frac{1}{2} \frac{\dot{\phi}^2}{M_p^2 H^2}$$

$$r = 16\epsilon$$

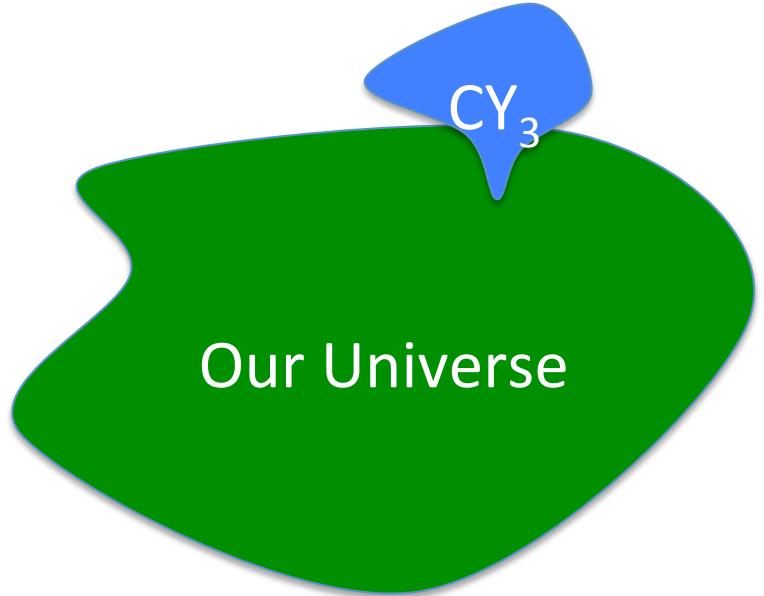
$$\frac{d\phi}{M_p} = \sqrt{\frac{r}{8}} H dt = \sqrt{\frac{r}{8}} dN$$

$$\frac{|\Delta\phi|}{M_p} \simeq \sqrt{\frac{r}{8}} \Delta N$$

$$\text{For } r = 0.2, \frac{|\Delta\phi|}{M_p} \simeq 0.16 \Delta N$$

Warped D-brane inflation

$$M_p^2 \sim \frac{M_s^8}{g_s^2} V_6$$

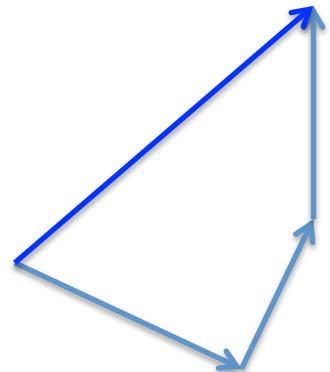


Single brane: $|\Delta\phi| = \sqrt{T_3}r \leq \frac{2}{\sqrt{N_B}}M_p$

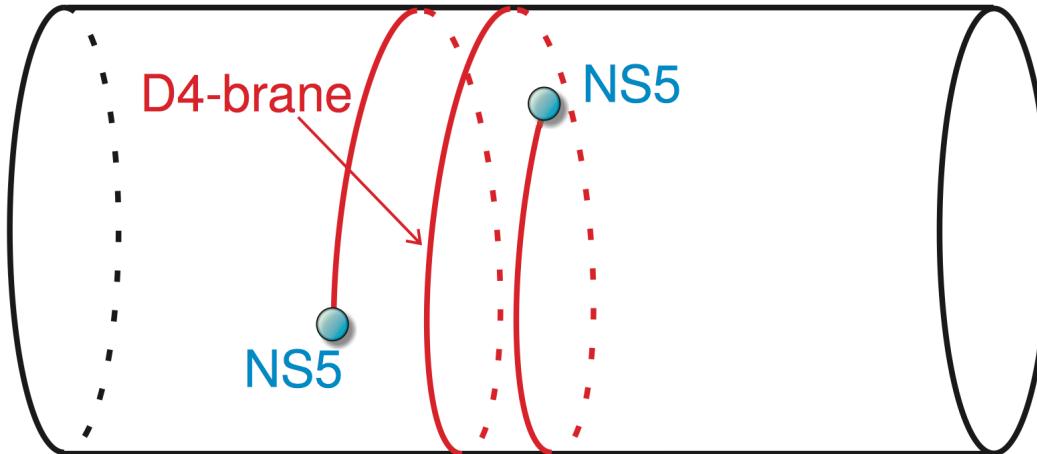
A stack of D-branes (N): $|\Delta\phi| = \sqrt{T_3}r \leq \frac{2}{\sqrt{N}}M_p$

$$\Delta\Phi \equiv \sqrt{\sum(\Delta\phi_i)^2} \leq 2M_p$$

Baumann, McAllister, 2007



Monodromy axion inflation in string theory



$$V \sim \phi^{2/3} \quad \text{Silverstein and Westphal, 2008}$$

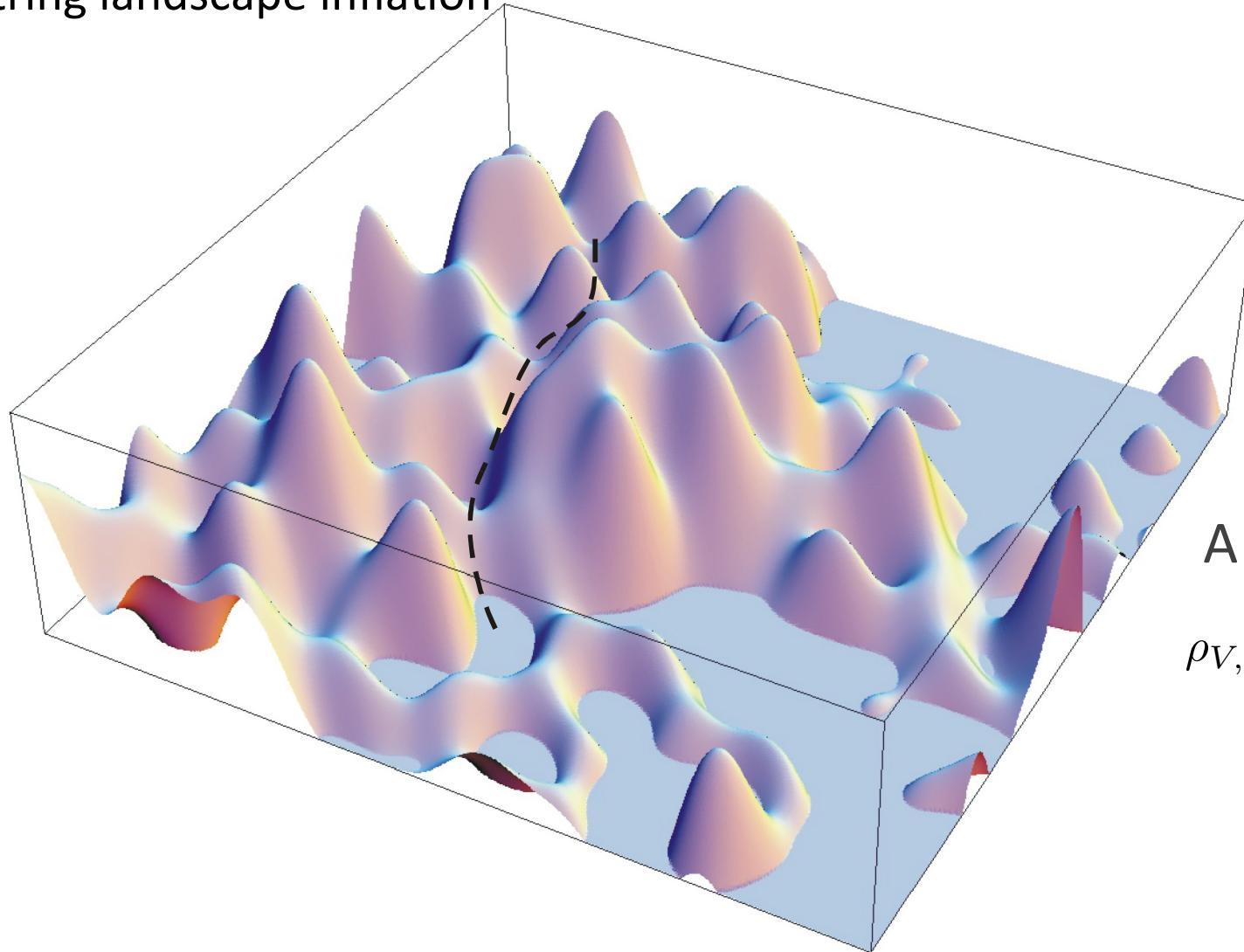
$$V \sim \phi \quad \text{McAllister, Silverstein and Westphal, 2008}$$

$$V \sim \phi^2 \quad \text{Marchesano, Shiu, Uranga, 2014}$$

$$V \sim \phi^3, \dots \quad \text{McAllister, Silverstein, Westphal, Wrase, 2014}$$

.....

String landscape inflation



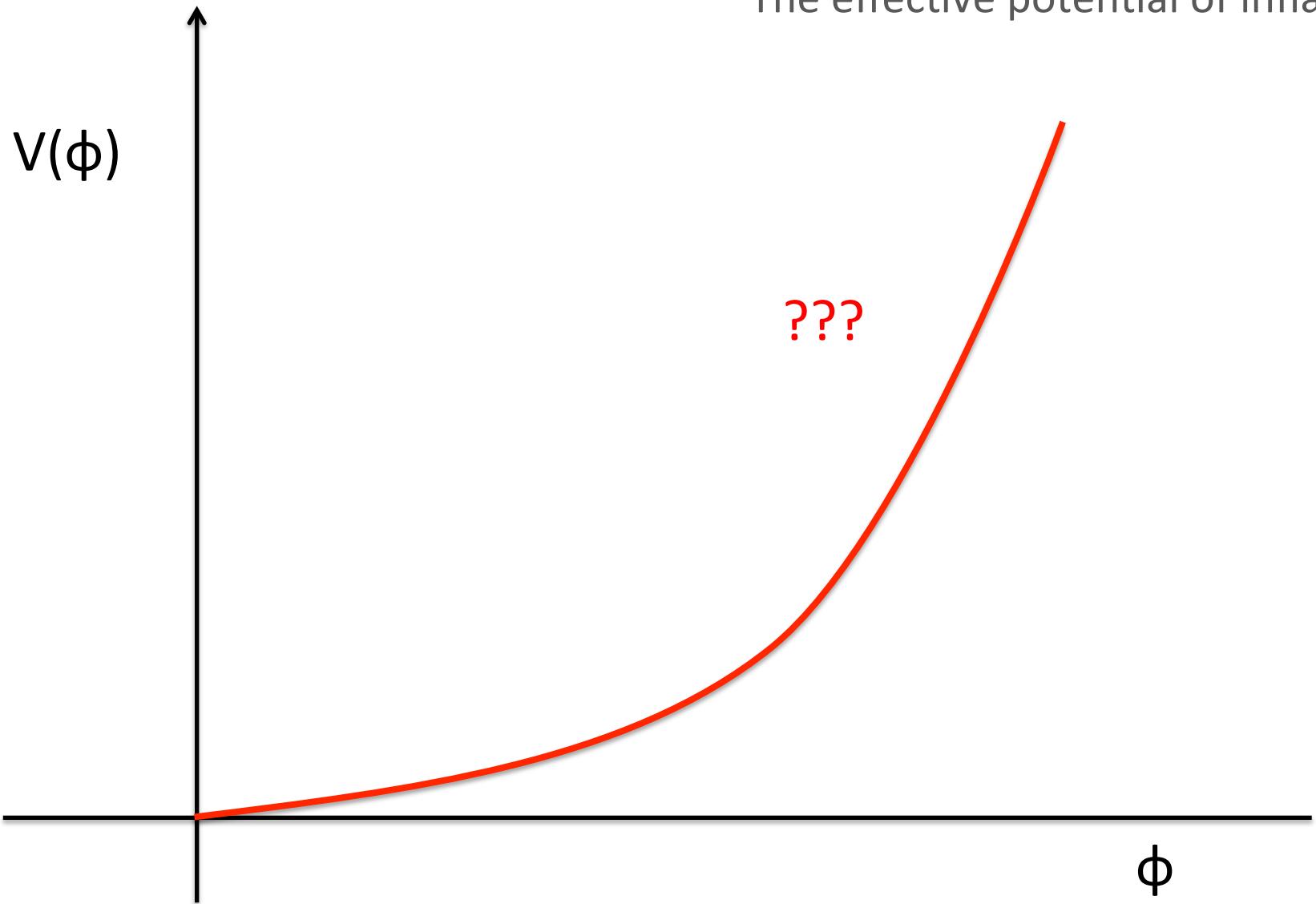
A Toy Model

$$\rho_{V,n+1} - \rho_{V,n} = \sigma$$

$$n_s = 1 - \frac{5}{3N}$$

$$r = \frac{16}{3N}$$

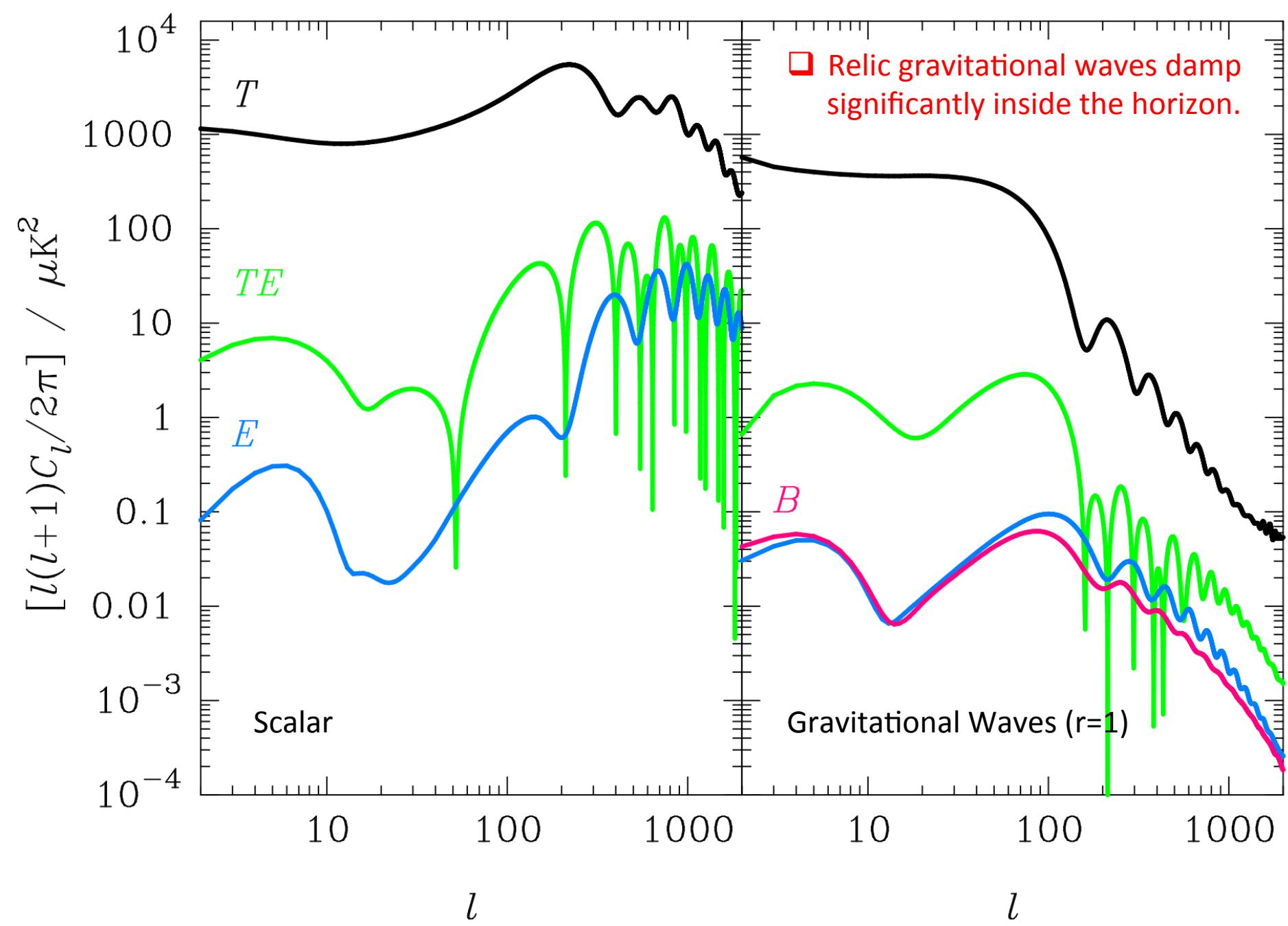
The effective potential of inflaton



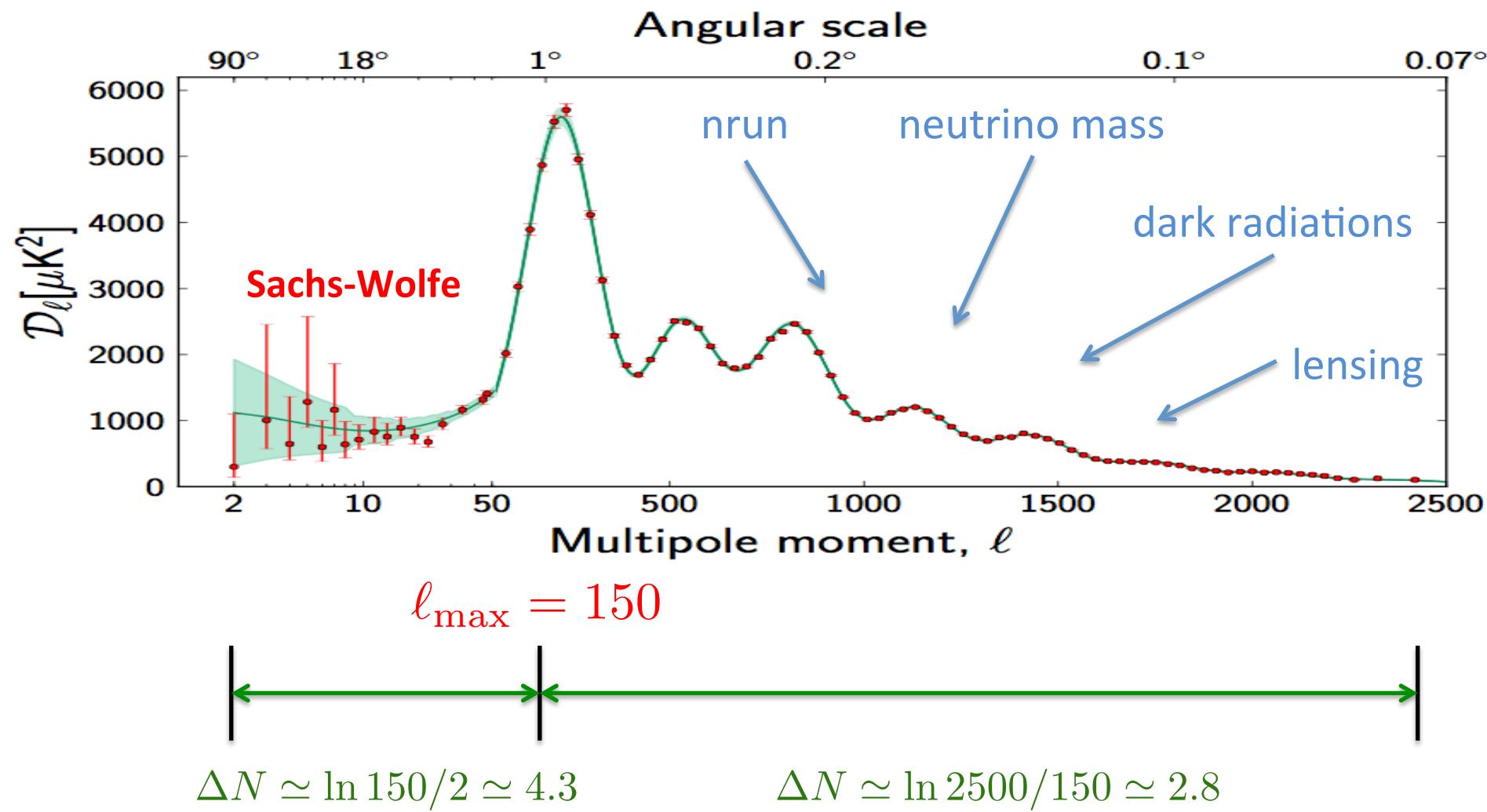
Everything is encoded in the data.

How to correctly extract the information from the data?

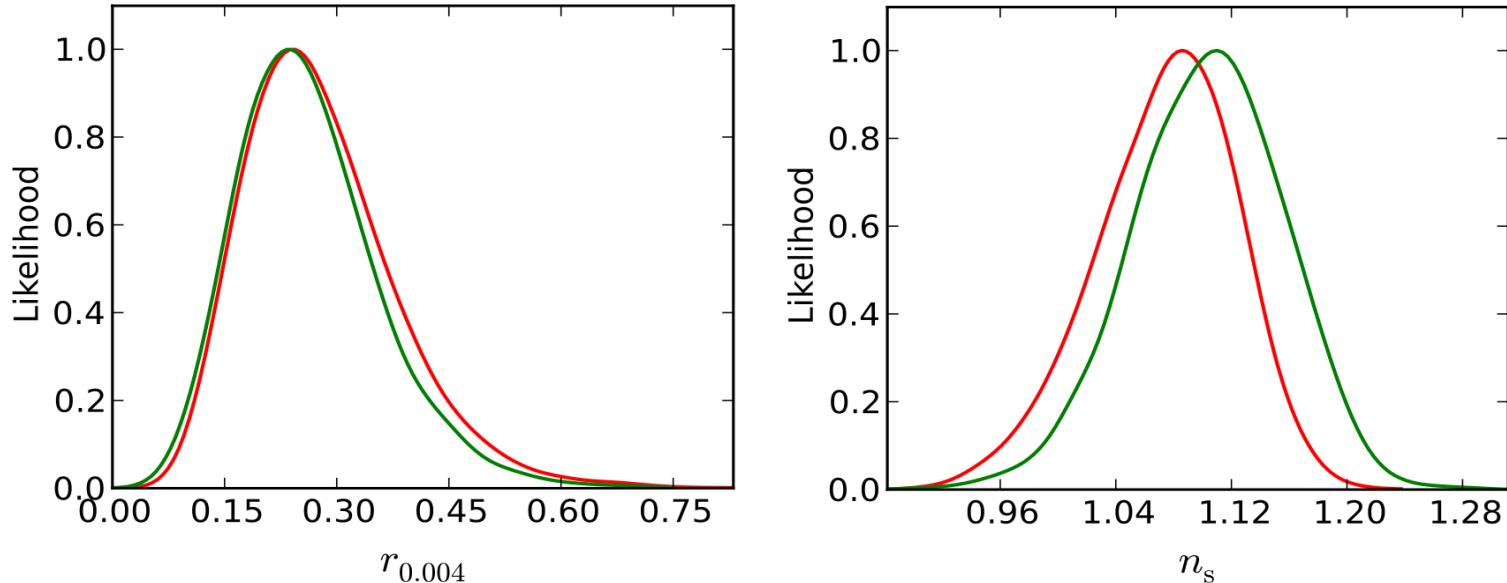
Global fitting may not be the best strategy.



- On large scales ($>1^\circ$) any causal effects have not had time to operate.
- Low- ℓ CMB power spectra are dominated by the Sachs-Wolfe effect.



B2+P13 (TT) + W9 (TE)
 B2+W9 (TT, TE)

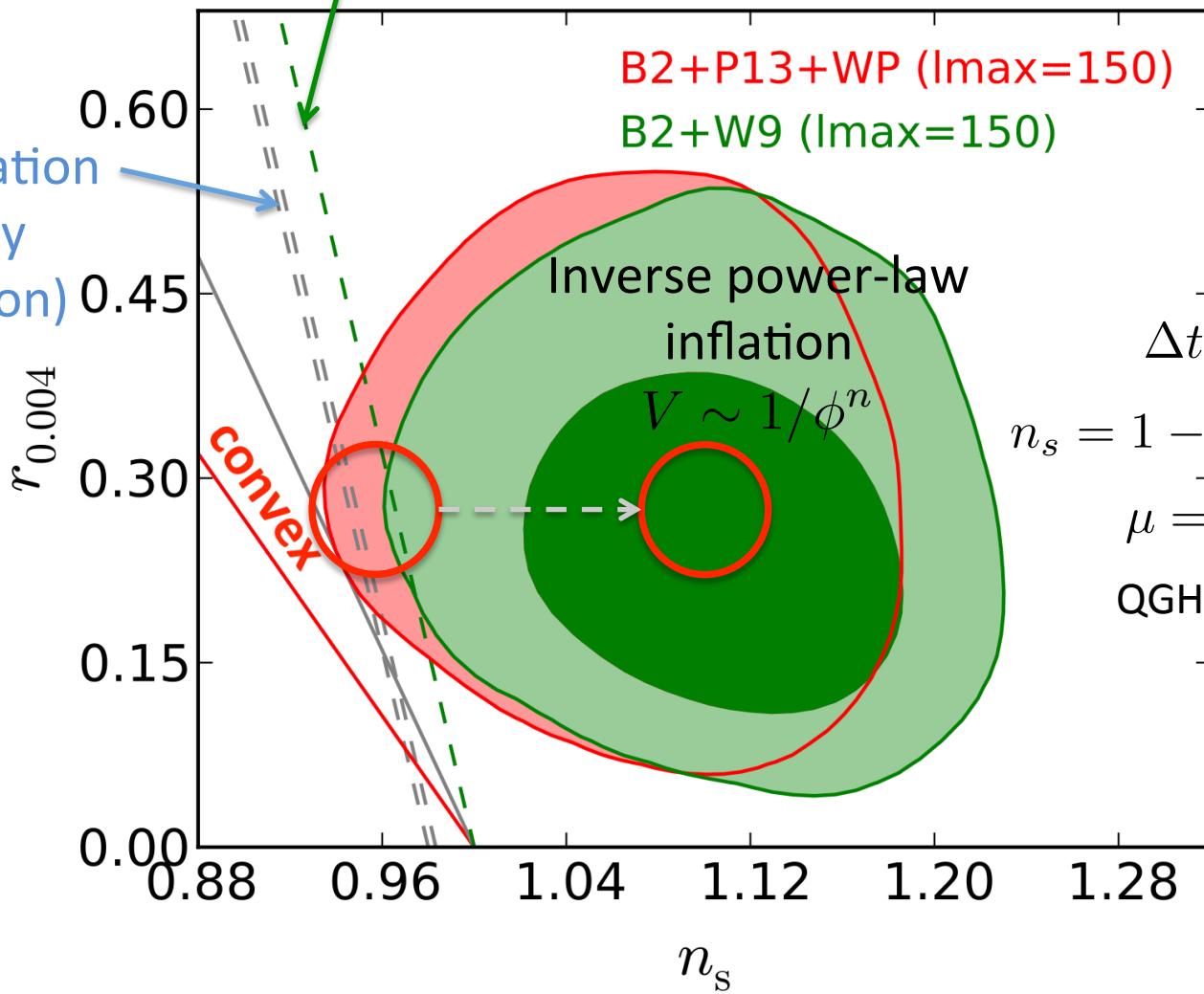


$n_t = -r/8$	B2+W9 ($\ell_{\max} = 150$)		B2+P13+WP ($\ell_{\max} = 150$)	
parameters	best fit	68% limits	best fit	68% limits
$\Omega_b h^2$	0.0192	$0.0270^{+0.0074}_{-0.0104}$	0.0209	$0.0263^{+0.0077}_{-0.0149}$
$\Omega_c h^2$	0.140	$0.166^{+0.029}_{-0.046}$	0.141	$0.141^{+0.018}_{-0.038}$
$100\theta_{\text{MC}}$	1.116	$1.104^{+0.046}_{-0.048}$	1.142	$1.098^{+0.044}_{-0.027}$
τ	0.095	$0.099^{+0.015}_{-0.018}$	0.105	$0.099^{+0.015}_{-0.018}$
$\ln(10^{10} A_s)$	3.106	$3.051^{+0.061}_{-0.054}$	3.021	$3.024^{+0.065}_{-0.057}$
n_s	1.098	$1.104^{+0.052}_{-0.051}$	1.120	$1.074^{+0.056}_{-0.042}$
r	0.19	$0.26^{+0.07}_{-0.11}$	0.23	$0.28^{+0.07}_{-0.12}$

Power-law Inflation

$$V \sim \exp(-\sqrt{2/p}\phi/M_p)$$

Chaotic Inflation
(monodromy
axion inflation)
 $V \sim \phi^n$



$$\Delta t \Delta x \gtrsim 1/M_s^2$$

$$n_s = 1 - 6\epsilon + 2\eta + r\mu$$

$$\mu = H^2 k^2 / a^2 M_s^4$$

QGH and M. Li, 2003

WMAP Cosmological Parameters

- Monte Carlo Markov Chain: [wmap_lcdm_tens_wmap9_chains_v5.tar.gz](#) (359.06 MBytes)

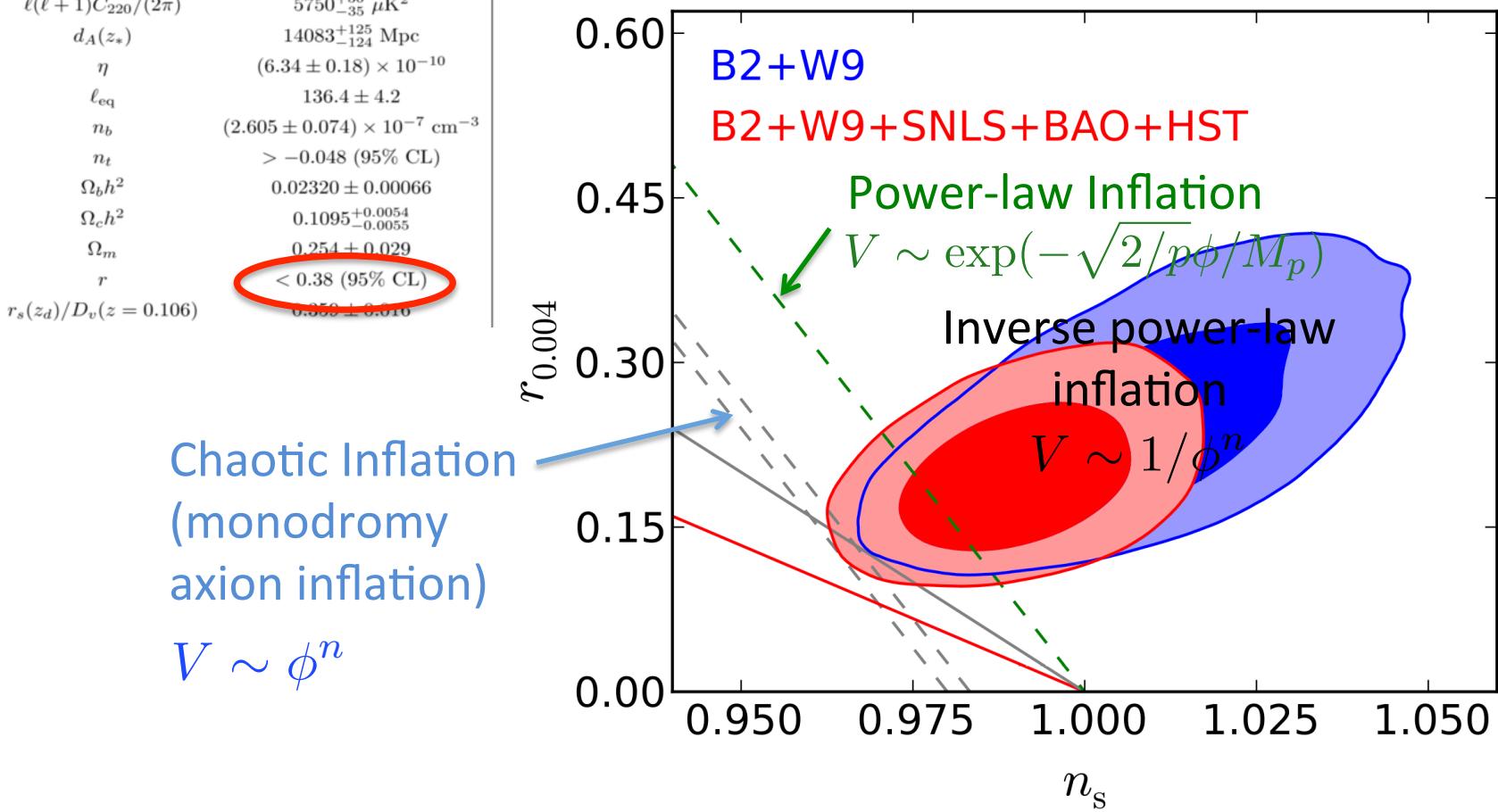
WMAP Cosmological Parameters

Model: lcdm+tens

Data: wmap9

$10^9 \Delta_{\mathcal{R}}^2$	2.26 ± 0.15
$\ell(\ell+1)C_{220}/(2\pi)$	$5750^{+36}_{-35} \mu\text{K}^2$
$d_A(z_*)$	$14083^{+125}_{-124} \text{ Mpc}$
η	$(6.34 \pm 0.18) \times 10^{-10}$
ℓ_{eq}	136.4 ± 4.2
n_b	$(2.605 \pm 0.074) \times 10^{-7} \text{ cm}^{-3}$
n_t	$> -0.048 \text{ (95% CL)}$
$\Omega_b h^2$	0.02320 ± 0.00066
$\Omega_c h^2$	$0.1095^{+0.0054}_{-0.0055}$
Ω_m	0.254 ± 0.029
r	$< 0.38 \text{ (95% CL)}$
$r_s(z_d)/D_v(z = 0.106)$	0.353 ± 0.016

H_0 $72.6 \pm 2.9 \text{ km/s/Mpc}$



How to reconcile Planck with BICEP2

NO TENSION between Planck and BICEP2 on large scales.

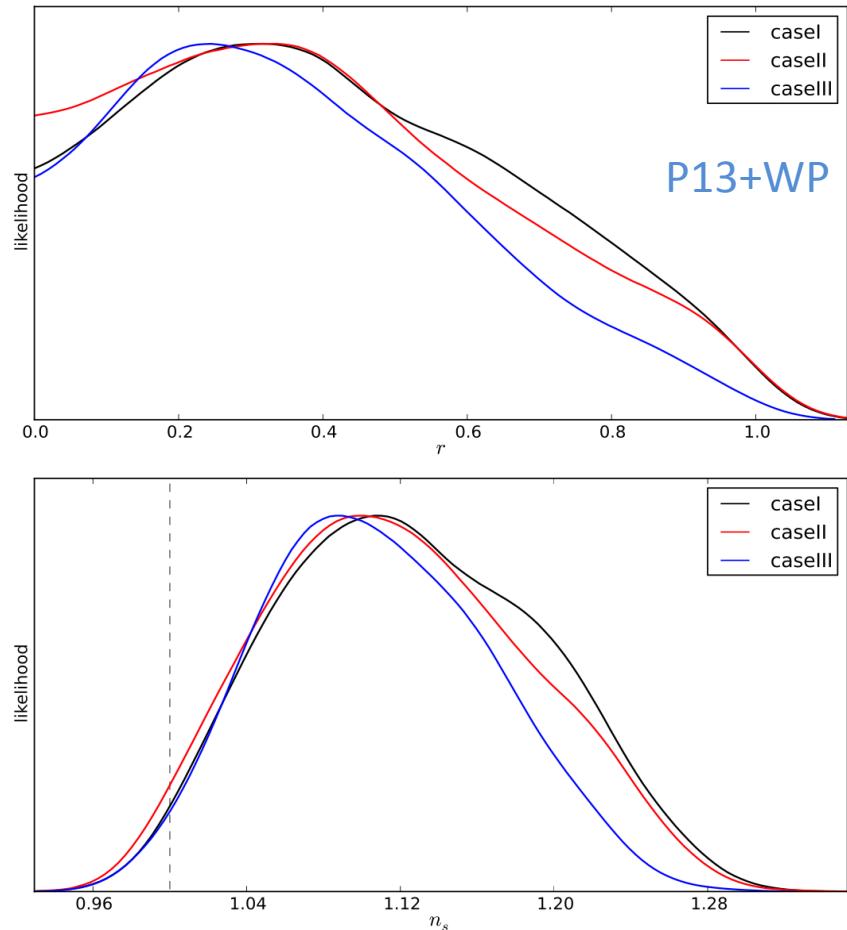
- ❑ The TT and TE power spectra generated by the relic gravitational waves are significant only the large scales. We take $\ell_{\text{max}}=100$.
- ❑ We fix the background parameters ($\Omega_b h^2$, $\Omega_c h^2$, $100 \theta_{\text{MC}}$, τ) at their best-fit values in the Λ CDM model from Planck, and the free running parameters are A_s , n_s and r .

$$C_\ell^{TT} = C_{\ell,s}^{TT} + C_{\ell,t}^{TT}$$

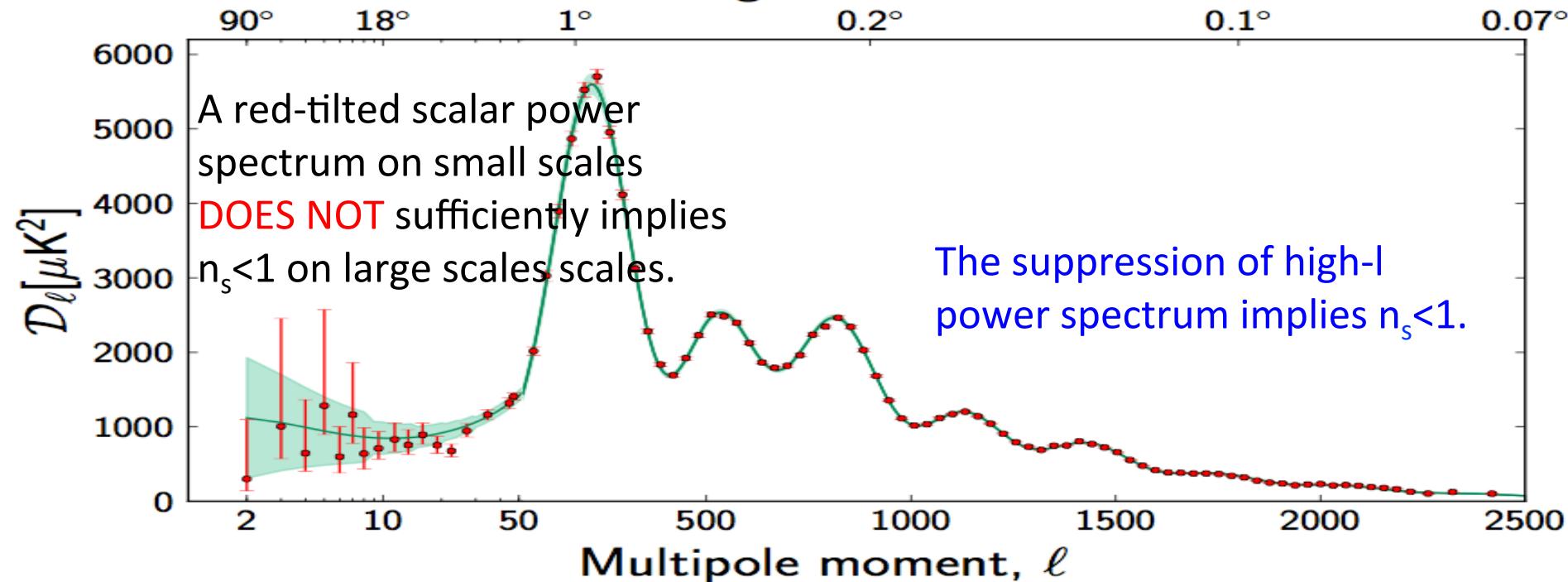
$$C_\ell^{TE} = C_{\ell,s}^{TE} + C_{\ell,t}^{TE}$$

$$C_{\ell,t}^{TT} > 0, \quad C_{\ell,t}^{TE} < 0$$

- ❑ The tensor-to-scalar ratio is peaked at around 0.2.
- ❑ The spectral index $n_s > 1$.



Angular scale

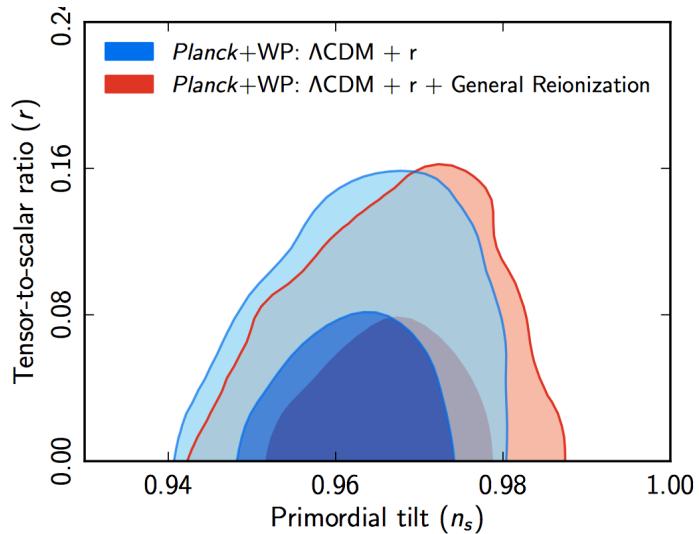


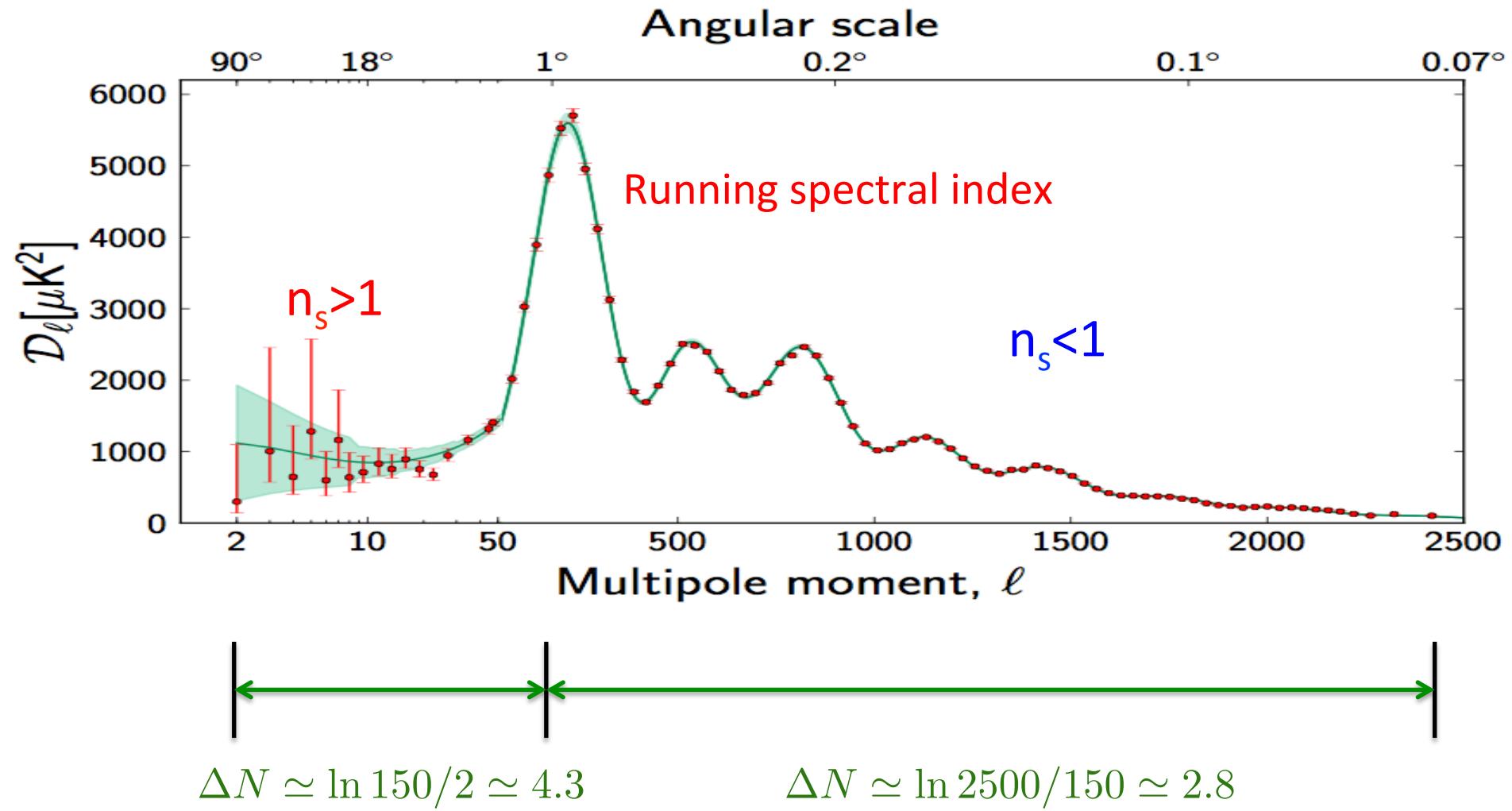
$$n_s = 0.9650 \pm 0.0080$$

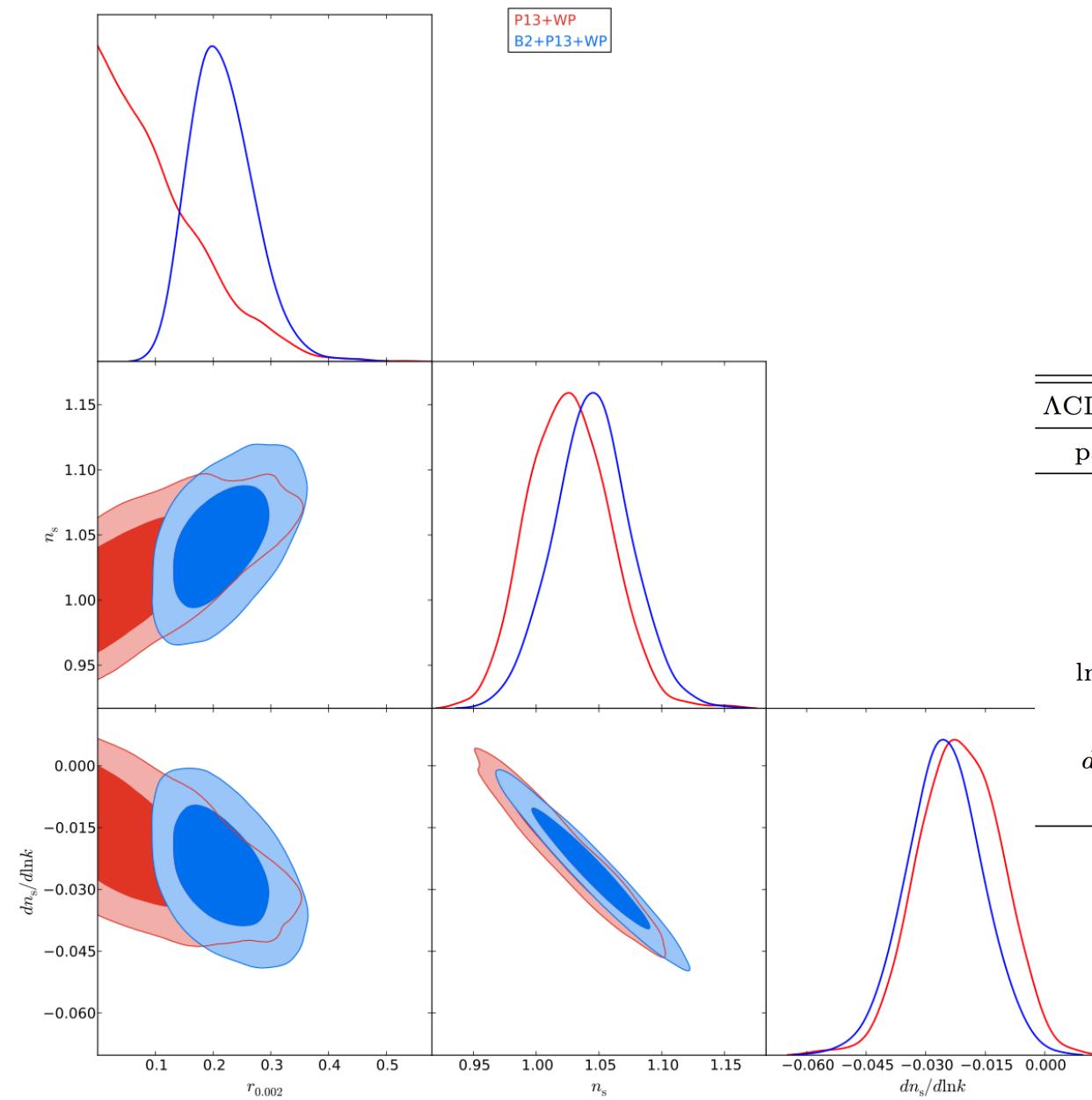
$$C_\ell^{TT} = C_{\ell,s}^{TT} + C_{\ell,t}^{TT}$$

$$r_{0.002} < 0.13, \quad @ 95\% CL$$

The apparent tension comes from the assumption of the base six-parameter Λ CDM model with a power-law scalar power spectrum.



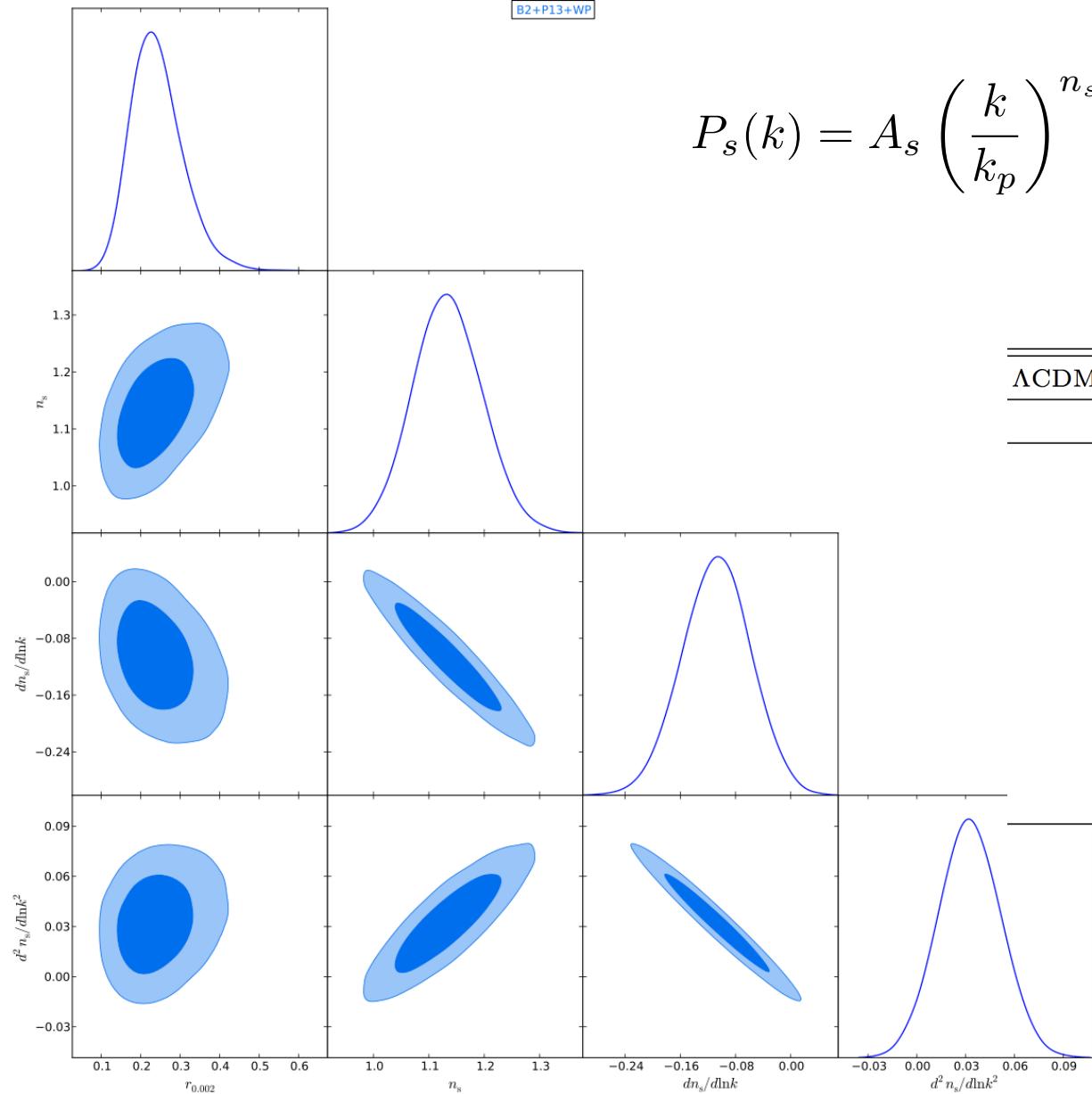




+nrun

Λ CDM+nrun+r	B2+P13+WP	
parameters	Best fit	68% limits
$\Omega_b h^2$	0.02229	$0.02246^{+0.00030}_{-0.00032}$
$\Omega_c h^2$	0.1187	$0.1173^{+0.0022}_{-0.0021}$
$100\theta_{MC}$	1.04154	$1.04162^{+0.00061}_{-0.00062}$
τ	0.0991	$0.1011^{+0.0137}_{-0.0161}$
$\ln(10^{10} A_s)$	3.117	$3.098^{+0.045}_{-0.041}$
n_s	1.0336	$1.0447^{+0.0295}_{-0.0297}$
$dn_s/d\ln k$	-0.0228	-0.0253 ± 0.0093
$r_{0.002}$	0.18	$0.22^{+0.04}_{-0.07}$

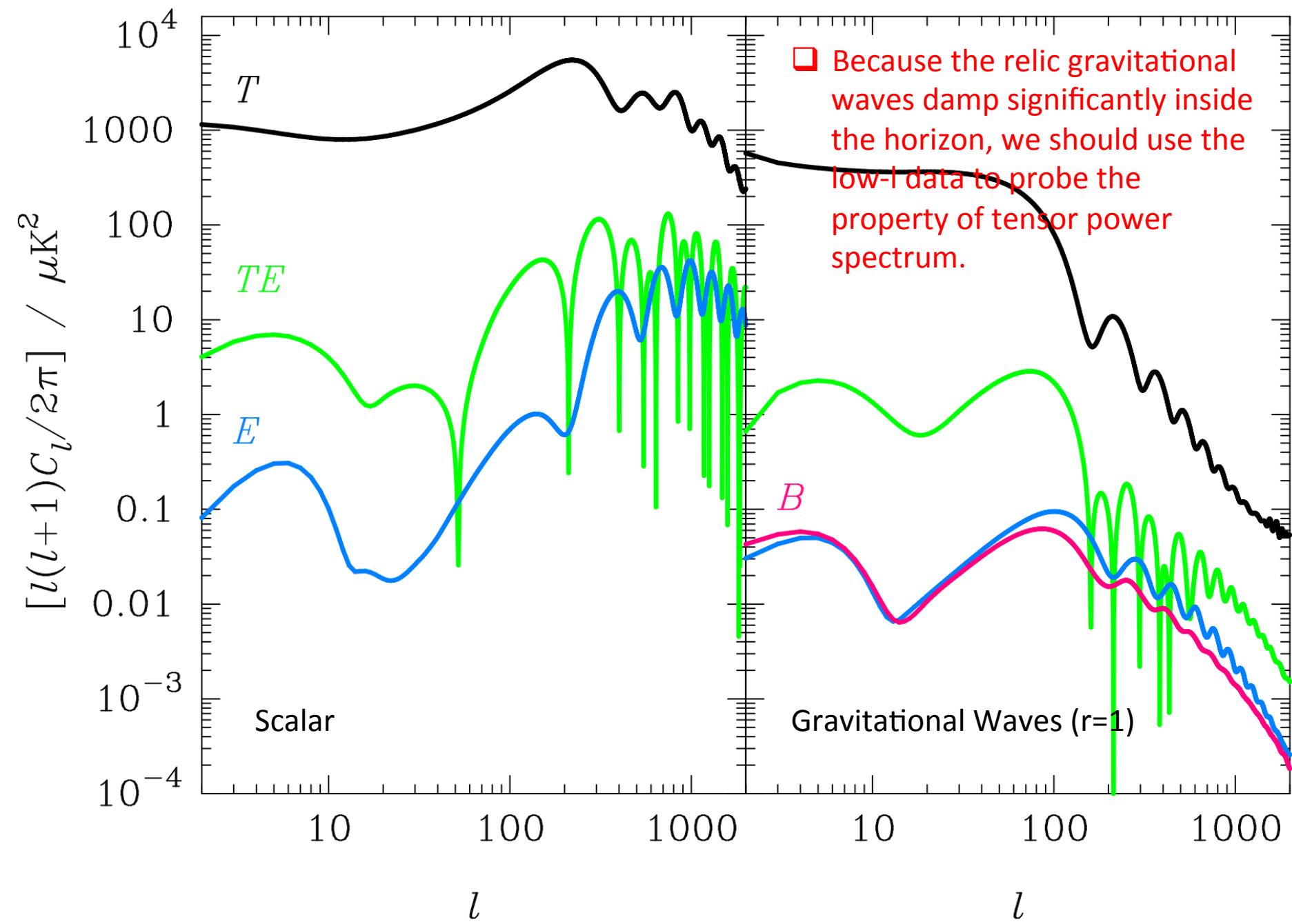
$$P_s(k) = A_s \left(\frac{k}{k_p} \right)^{n_s - 1 + \frac{1}{2} \frac{dn_s}{d \ln k} \ln \frac{k}{k_p} + \frac{1}{6} \frac{d^2 n_s}{d \ln k^2} \ln^2 \frac{k}{k_p}}$$

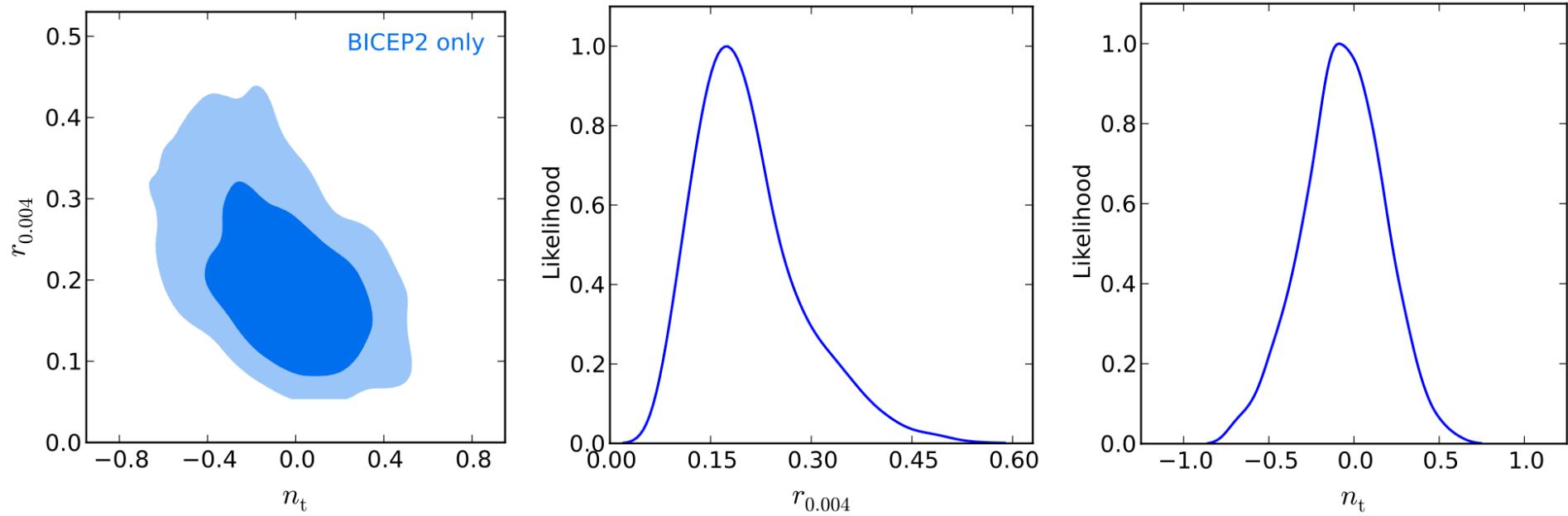


Λ CDM+nrun+nrunrun+r	B2+P13+WP	
parameters	Best fit	68% limits
$\Omega_b h^2$	0.02221	0.02217 ± 0.00035
$\Omega_c h^2$	0.1203	0.1184 ± 0.0023
$100\theta_{\text{MC}}$	1.04145	$1.04142^{+0.00064}_{-0.00063}$
τ	0.0983	$0.1054^{+0.0142}_{-0.0168}$
$\ln(10^{10} A_s)$	3.047	$3.063^{+0.066}_{-0.050}$
n_s	1.1656	$1.1344^{+0.0612}_{-0.0608}$
$dn_s/d \ln k$	-0.139	$-0.108^{+0.049}_{-0.048}$
$d^2 n_s/d \ln k^2$	0.045	$0.033^{+0.018}_{-0.016}$
$r_{0.002}$	0.22	$0.24^{+0.05}_{-0.07}$

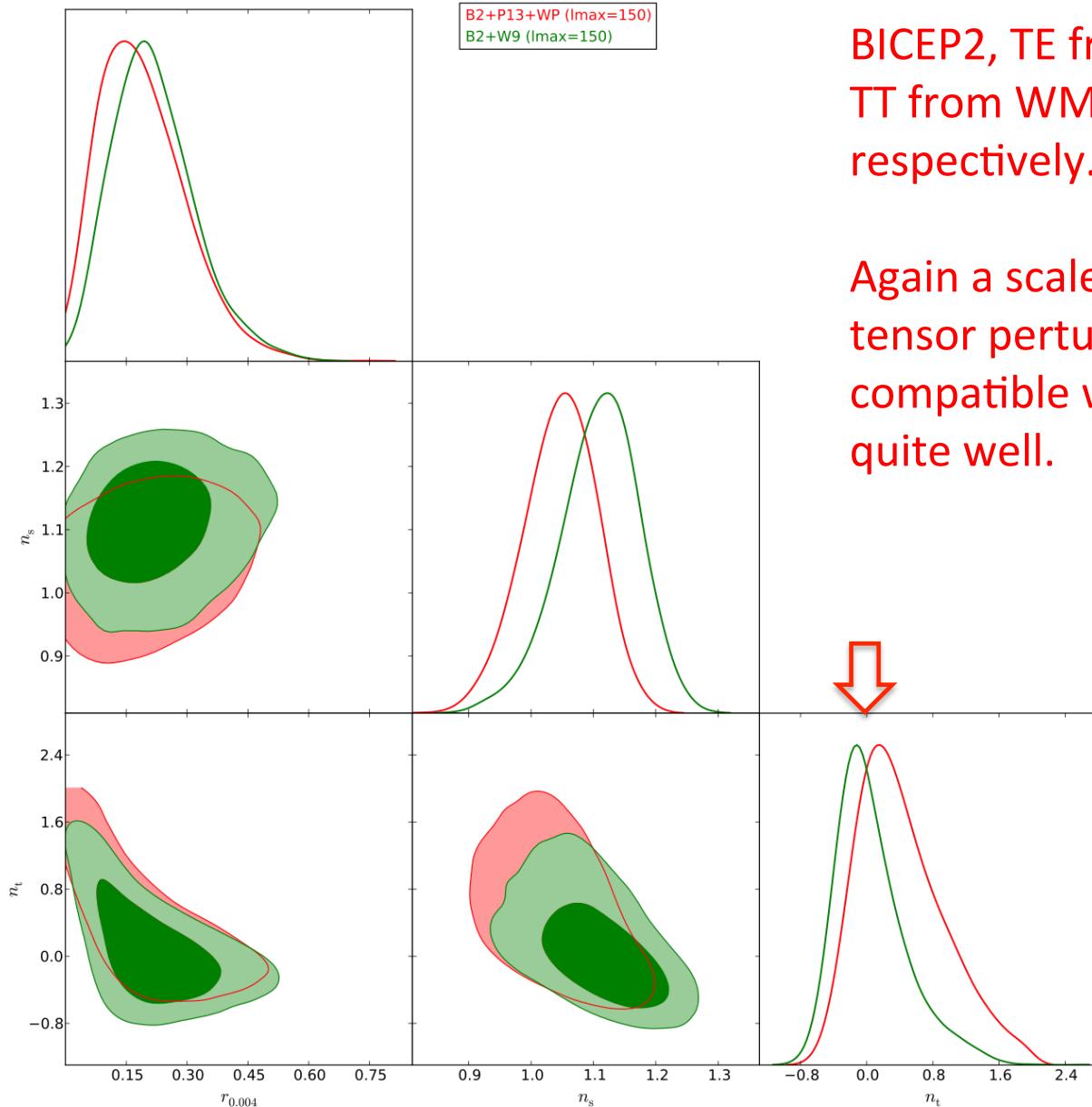
$$\Delta\chi^2 = -3.12$$

The tilt of relic gravitational waves power spectrum





$$P_t = A_t \left(\frac{k}{k_p} \right)^{n_t} \quad r = 0.21^{+0.04}_{-0.10} \quad n_t = -0.06^{+0.25}_{-0.23}$$



BICEP2, TE from WMAP, and TT from WMAP and Planck respectively. ($\text{l_max}=150$)

Again a scale-invariant tensor perturbation is compatible with the data quite well.



Summary

- A red-tilt tensor power spectrum is compatible with the data, and the simplest version of inflation is consistent with the data.
- A blue-tilted scalar power spectrum is preferred on the large scales (e.g. $|l| < 150$).
- The inflation model with inverse power-law potential can fit the data quite well.
- The space-time non-commutativity can help chaotic inflation and power-law inflation to fit the data.

- A negative running of spectral index is favored at around 3 sigma level.
- Furthermore, a positive running of running is preferred at around 1.7 sigma level.

Thank You!