



A more attractive scheme for radion stabilization and supercooled phase transition

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Based on K. Fujikura (TITech), YN and M. Yamada (MIT), arXiv:1910.07546.

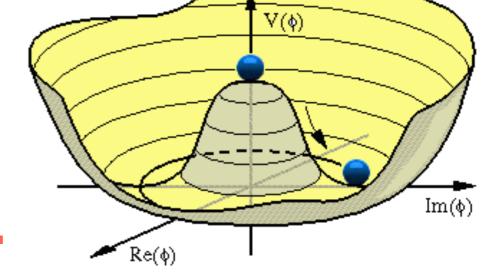
HKUST IAS, January 2020

The Naturalness Problem

The Higgs potential (and the weak scale) is unstable under quantum effects.

$$V(\phi) = -\mu^2 |\phi|^2 + \lambda |\phi|^4$$

~100 GeV



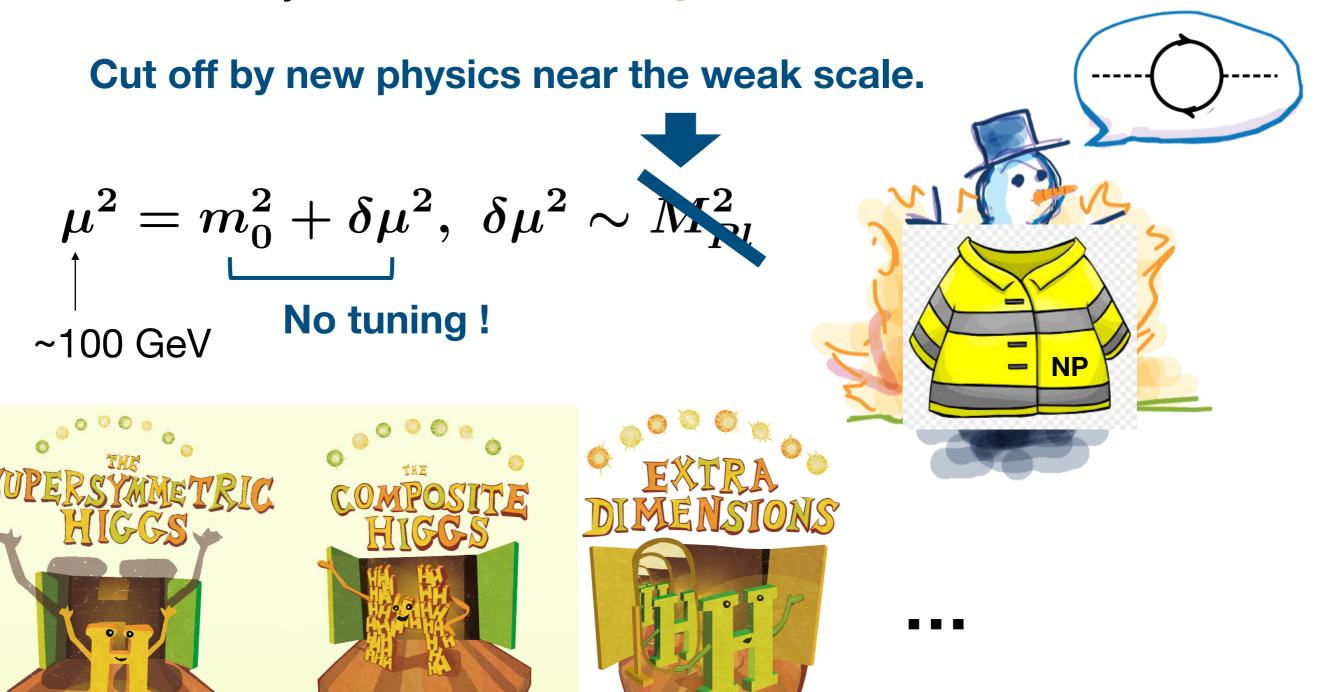
Higgs

Severe fine-tuning is needed.

$$\mu^{2} = m_{0}^{2} + \delta\mu^{2}, \ \delta\mu^{2} \sim M_{Pl}^{2}$$
Tuning
$$\mu^{2} = \frac{\mu^{2}}{M_{Pl}^{2}} \sim 10^{-32} \,!$$

New Physics Candidates

Many new physics models have been considered, motivated by the naturalness problem.



Randall-Sundrum Model

- 5D universe bounded by two branes: Higgs located on IR (TeV) brane and gravity localized toward UV (Planck) brane.
- 5th dimension highly curved

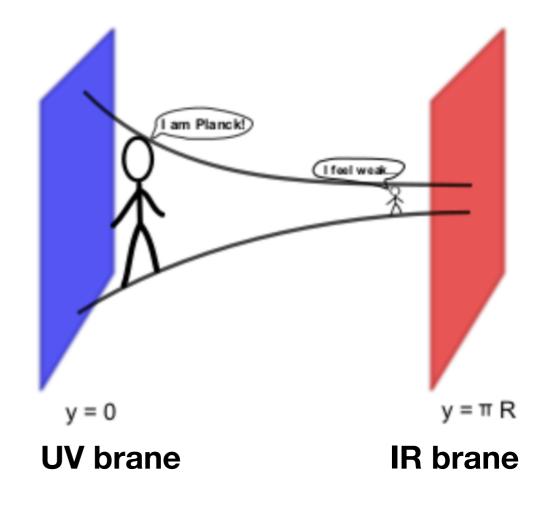
→ Anti-de-Sitter (AdS) space

Metric :
$$ds^2 = e^{-k\,|y|} \eta_{\mu
u} dx^\mu dx^
u - dy^2$$

Warp factor
(4D flat : $ds^2 = \eta_{\mu
u} dx^\mu dx^
u$)



All fundamental mass parameters on the IR brane are exponentially redshifted.

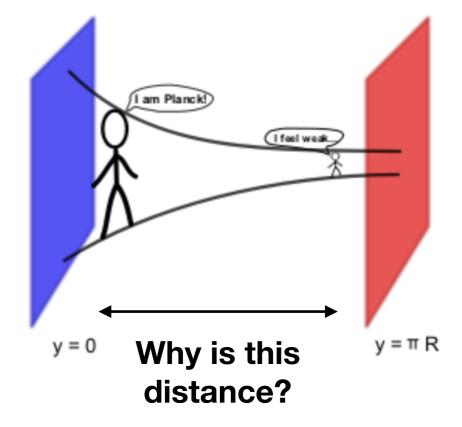


Radion

- A modulus field, called radion, parameterizes the distance between the IR and UV branes.
- In the original RS model, its vacuum expectation value is fixed <u>by hand</u> to realize an adequate redshift factor.

To solve the naturalness problem completely ...

We need a mechanism that stabilizes the radion VEV without fine-tuning.



Goldberger-Wise mechanism Goldberger, Wise (1999)

introduces a bulk scalar field with brane-localized potentials.

Radion potential

Radion

HEP 88 records found 1 - 25 ▶ Jump to record: 1

1. Modulus stabilization with bulk fields

(1320) Walter D. Goldberger, Mark B. Wise (Caltech). Jul 1999. 8 pp. Published in Phys.Rev.Lett. 83 (1999) 4922-4925 CALT-68-2232 DOI: <u>10.1103/PhysRevLett.83.4922</u> e-Print: <u>hep-ph/9907447 | PDF</u> <u>References | BibTeX | LaTeX(US) | LaTeX(EU) | Harvmac | EndNote ADS Abstract Service</u>

Detailed record - Cited by 1320 records 1000+

2. Phenomenology of a stabilized modulus

 (429) Walter D. Goldberger, Mark B. Wise (Caltech). Nov 1999. 9 pp. Published in Phys.Lett. B475 (2000) 275-279 CALT-68-2250 DOI: <u>10.1016/S0370-2693(00)00099-X</u> e-Print: <u>hep-ph/9911457 | PDF</u> <u>References | BibTeX | LaTeX(US) | LaTeX(EU) | Harvmac | EndNote ADS Abstract Service</u>
 <u>Detailed record - Cited by 429 records</u> 250+

3. Comments on the holographic picture of the Randall-Sundrum model

(427) R. Rattazzi (INFN, Pisa & Pisa, Scuola Normale Superiore), A. Zaffaroni (INFN, Milan & Milan Bicocca U.). Dec 2000. 26 pp. Published in JHEP 0104 (2001) 021

SNS-PH-00-21, BICOCCA-FT-00-25 DOI: <u>10.1088/1126-6708/2001/04/021</u> e-Print: **hep-th/0012248 | PDF**

> <u>References | BibTeX | LaTeX(US) | LaTeX(EU) | Harvmac | EndNote</u> ADS Abstract Service; AMS MathSciNet

Detailed record - Cited by 427 records 250+

4. Radion dynamics and electroweak physics

(424) Csaba Csaki (Los Alamos), Michael L. Graesser (UC, Santa Cruz), Graham D. Kribs (Carnegie Mellon U.). Aug 2000. 41 pp. Published in Phys.Rev. D63 (2001) 065002
 SCIPP-00-27
 DOI: <u>10.1103/PhysRevD.63.065002</u>
 e-Print: <u>hep-th/0008151 | PDF</u>
 <u>References | BibTeX | LaTeX(US) | LaTeX(EU) | Harvmac | EndNote</u>
 ADS Abstract Service; OSTI.gov Server

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Cosmological History

If the RS model is realized in nature, it must predict a consistent cosmological history of our Universe.

Fujikura

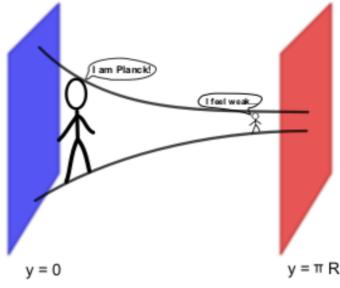
At low temperature ...

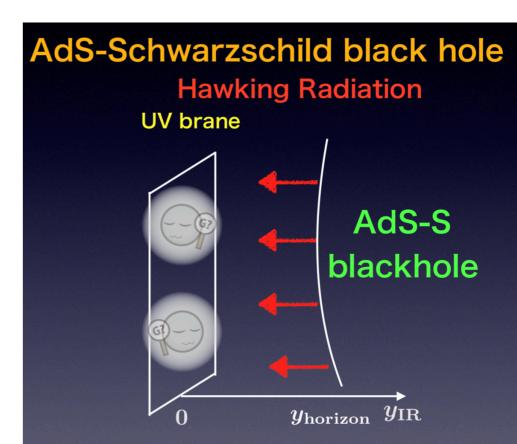
The Universe is described by the compact RS model.

At high temperature ...

The system is described by <u>the de-</u> <u>compactified AdS-Schwarzschild (AdS-S)</u> <u>black hole with the IR brane replaced by</u> <u>an event horizon</u>.

Creminelli, Nicolis, Rattazzi (2001)





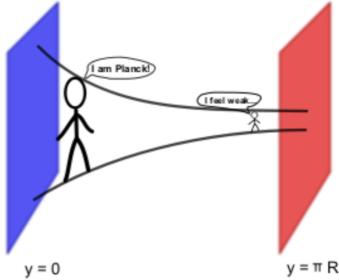
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Phase transition

At low temperature ...

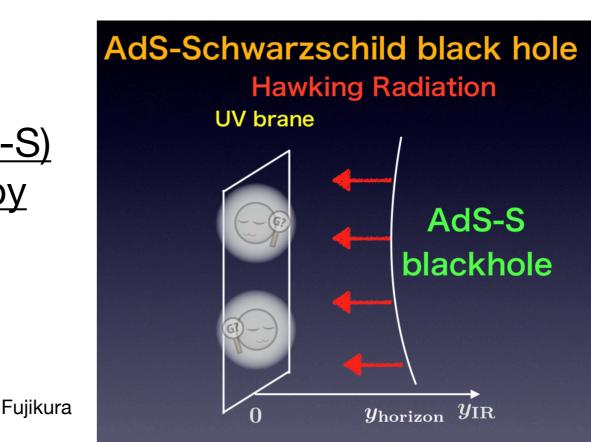
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Eternal Inflation

- ✓ The phase transition is of <u>the first order</u>, takes place via <u>a supercooling</u> <u>phase</u> and proceeds via <u>nucleation of true vacuum bubbles</u>.
- ✓ In the Goldberger-Wise mechanism, the supercooling phase lasts very long and the phase transition is never completed in most of the region where <u>a classical treatment of the gravity is meaningful</u>.



Creminelli, Nicolis, Rattazzi (2001)

✓ Even in the remaining parameter space, the brane-localized potentials of the bulk scalar field give <u>a non-negligible back-reaction</u> to the gravitational action and the analysis without including the backreaction is not trustable.

We propose a new mechanism of radion stabilization with no issue in completion of the phase transition !

Radion Effective Action

The geometry of the RS spacetime :

$$ds^{2} = G_{AB}dx^{A}dx^{B} = e^{-2kT(x)|y|}g_{\mu\nu}dx^{\mu}dx^{\nu} - T^{2}(x)dy^{2}$$

 $y \in (-1/2, 1/2)$, UV and IR branes are placed at y = 0 and y = 1/2 respectively

T(x) determines the size of the extra dimension and is a modulus field associated with a fluctuation along the extra dimension.

A pure gravity action of RS :

$$S = \int d^4x dy \left[\sqrt{G} \left(rac{1}{2} M_5^3 R - \Lambda_{
m bulk}
ight) - \Lambda_{
m IR} \sqrt{-g_{
m IR}} \, \delta(y-y_{
m IR}) - \Lambda_{
m UV} \sqrt{-g_{
m UV}} \, \delta(y)
ight]$$

Abulk: bulk cosmological constant, AIR, AUV: IR and UV brane tensions

The RS geometry is realized when $\Lambda_{\text{bulk}}|_{\text{RS}}/k = \Lambda_{\text{IR}}|_{\text{RS}} = -\Lambda_{\text{UV}}|_{\text{RS}} = -6M_5^3k$ But, in general...

$$\Lambda_{
m IR} = -6M_5^3k + \delta\Lambda_{
m IR}, \quad \Lambda_{
m UV} = 6M_5^3k + \delta\Lambda_{
m UV}$$

Radion Effective Action

The Kaluza-Klein (KK) reduction of the pure gravity action

> 4D effective action of radion $\mu \equiv k e^{-kT(x)/2}$

$$S_{
m radion} = \int d^4x \left[rac{3N^2}{4\pi^2} \left(\partial \mu(x)
ight)^2 - V(\mu)
ight]
onumber V(\mu) = \delta \Lambda_{
m UV} + \mu^4 \delta \Lambda_{
m IR}/k^4$$

The radion kinetic term is not canonically normalized.

$$N\equiv 2\pi (M_5/k)^{3/2}$$

Terms with higher powers of the Ricci scalar coming from <u>quantum gravity</u> <u>effects</u> can be neglected for

$$N\gtrsim 4\cdot 5^{3/4}/\sqrt{3\pi}\simeq 4.4$$
 Harling and G. Servant (2018)

Radion Stabilization

Introduce a SU(NH) pure Yang-Mills field in the bulk of the extra dimension.

$$S_{
m Yang-Mills} = \int d^5x \sqrt{G} \left(-rac{1}{4g_5^2} F_{AB} F^{AB}
ight)$$

KK decomposition and integrating over the extra dimension

4D effective action for the zero-mode gauge field

RGE of 4D gauge coupling:

Radion

Gauge coupling becomes strong at low-energies and the theory confines !

Radion Stabilization

The confinement scale is naturally at the TeV scale.

(i) $\Lambda_H(\mu) < m_{KK} = \pi \mu$

Confinement scale: $\Lambda_H(\mu) = \Lambda_{H,0} \left(\frac{\mu}{\mu_{\min}}\right)^n$ $n = \frac{8\pi^2}{b_{\rm YM} \cdot kg_5^2}$

(ii) $\Lambda_H(\mu) > m_{KK} = \pi \mu$

The description of the 4D effective theory breaks down.

The confinement scale is independent of the radion VEV.

Confinement scale: $\Lambda_{H}(\mu) = \Lambda_{H}(\mu_{c}) \equiv \gamma_{c}\mu_{c}$ $\gamma_{c} = \pi$

Confinement scale of (i) and (ii) are the same at $\,\mu=\mu_c$

Radion Stabilization

The confinement generates a vacuum energy.

$$V_H = rac{1}{4} \langle T^{\mu}_{\mu}
angle \simeq -rac{b_{
m YM}}{8} \left(\Lambda_H(\mu)
ight)^4$$

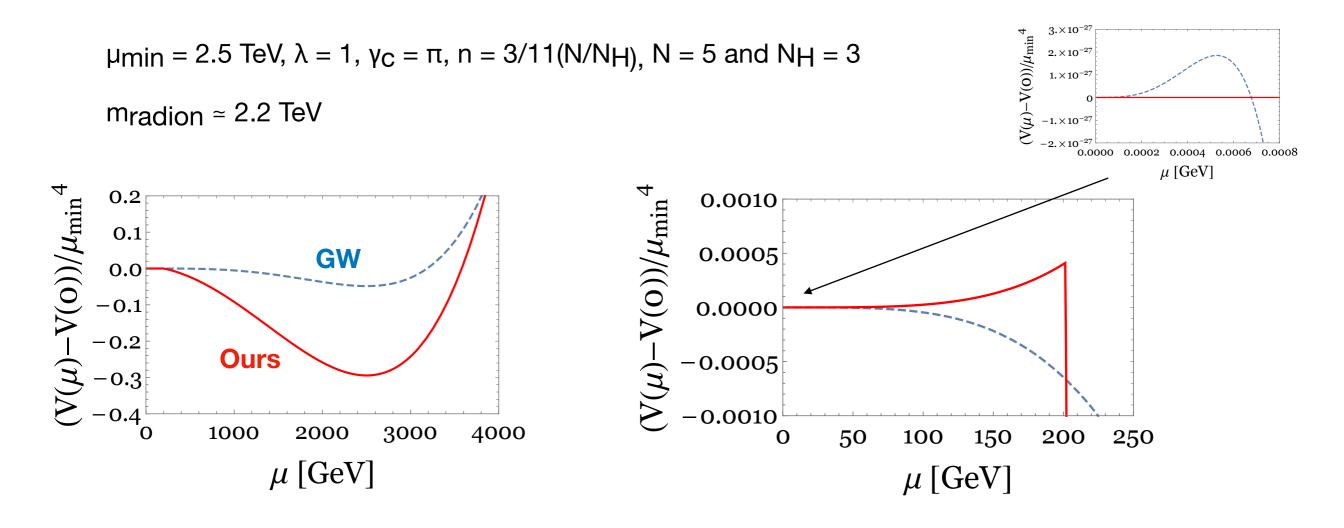
Radion can be stabilized by the balance between the vacuum energy and the IR brane tension.

$$\begin{split} V_{r,\mathrm{eff}}(\mu) &= \begin{cases} V_0 + \frac{\lambda}{4} \mu^4 - \frac{b_{\mathrm{YM}}}{8} \Lambda_{H,0}^4 \left(\frac{\mu}{\mu_{\min}}\right)^{4n} & \text{for } \mu > \mu_c , \\ V_0 + \frac{\lambda}{4} \mu^4 - \frac{b_{\mathrm{YM}}}{8} \gamma_c^4 \mu_c^4 & & \text{for } \mu < \mu_c \end{cases} \\ \lambda &= 4\delta \Lambda \mathrm{IR}/\mathrm{k}^4 & & \mathrm{n} < 1 \text{ is required.} \end{cases} \end{split}$$

 $V_0 = \delta \Lambda UV$ determined by the condition that the potential energy at the minimum is vanishingly small.

$$\blacktriangleright \mu_{
m min} = \left(rac{nb_{
m YM}}{2\lambda}
ight)^{rac{1}{4}} \Lambda_{H,0}$$

Radion Potential



✓ Our radion potential has a deeper minimum than the Goldberger-Wise.

- \checkmark The origin is a local minimum.
- ✓ Not smooth at $\mu = \mu_c$, reflecting our ignorance of the precise radion potential around this point.

AdS-S Spacetime

At high temperature, the system is described by the AdS-S spacetime with the IR brane replaced by the event horizon.

$$ds^{2} = k^{2}\rho^{2}\left(1 - \frac{\rho_{H}^{4}}{\rho^{4}}\right)dt^{2} - k^{2}\rho^{2}\sum_{i=1}^{3}dx_{i}^{2} - \frac{d\rho^{2}}{k^{2}\rho^{2}\left(1 - \frac{\rho_{H}^{4}}{\rho^{4}}\right)}$$

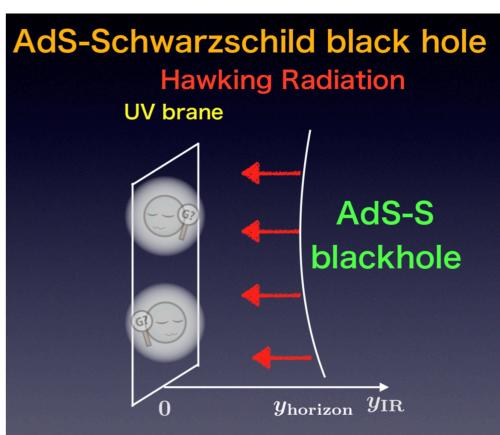
TH (= $k^2 \rho H/\pi$): the Hawking temperature parameterized by the position of the event horizon

The free energy of the AdS-S spacetime :

$$F_{
m AdS-S}(T_{H}) = rac{3}{8} \pi^{2} N^{2} T_{H}^{4} - rac{1}{2} \pi^{2} N^{2} T_{H}^{3} T$$

Creminelli, Nicolis, Rattazzi (2001)

The minimum is given by TH = T.



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Phase Transition

As the temperature cools down, the phase transition from the AdS-S spacetime to the RS spacetime can take place.

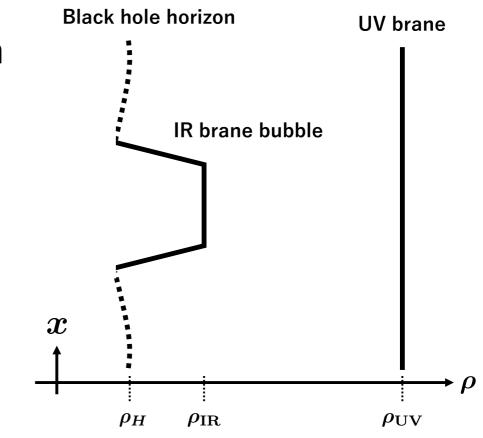
Both the AdS-S spacetime and the RS spacetime are locally stable.

The phase transition occurs via the decay of the false vacuum and the phase transition is expected to be of the first order.

As the temperature decreases, the event horizon moves toward TH = 0.

The phase transition proceeds via the "IR brane bubble nucleation"

Spherical brane patches on the horizon appear and are combined to form the IR brane.



Transition Rate

• The rate of the phase transition per unit volume per unit time :

 $\Gamma \propto e^{-S}$

• The phase transition can be completed only when the bubble nucleations are not diluted by the cosmic expansion :

 $\Gamma > H^4$

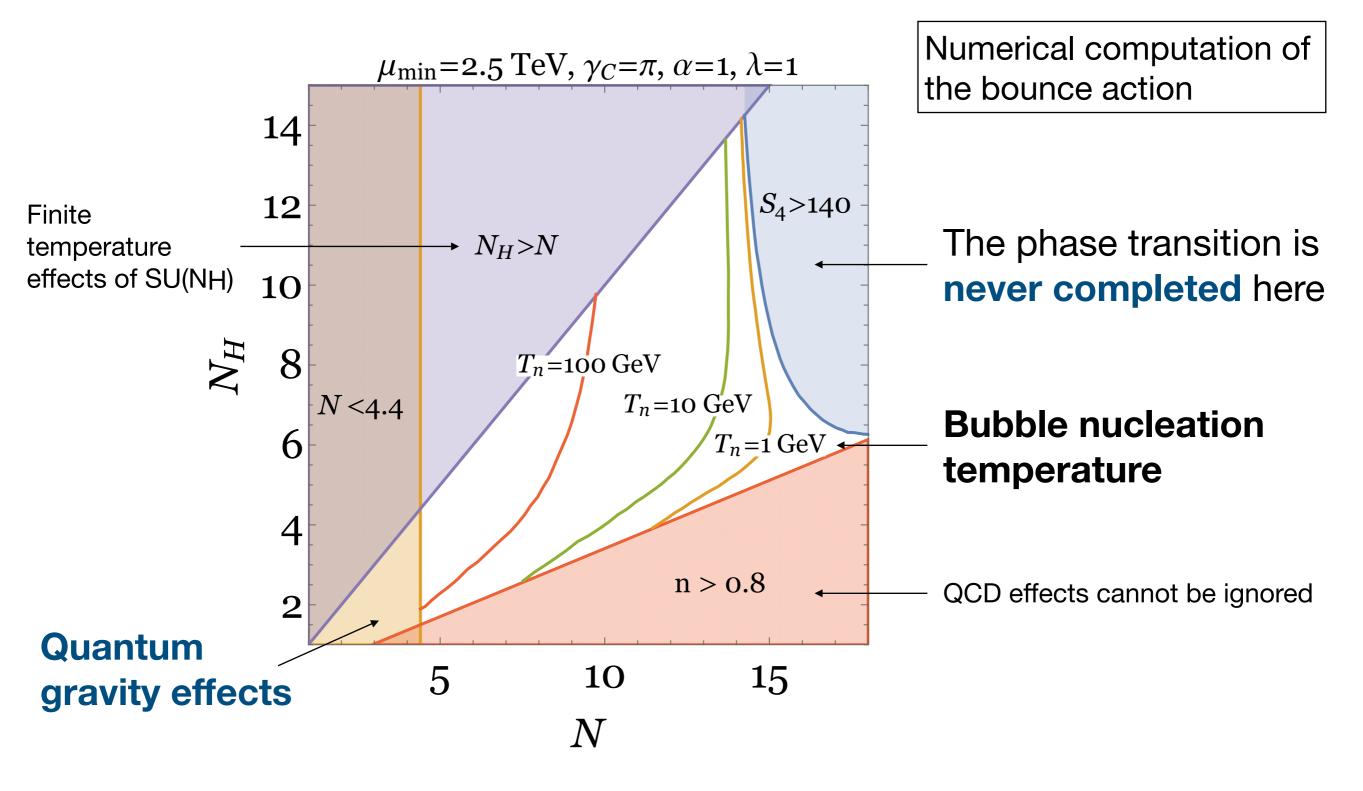
 The O(4)-symmetric bounce action after <u>canonically normalizing</u> the radion kinetic term :

$$S_4 \sim rac{9N^4}{8\pi^2} rac{\mu_t^4}{V(\mu_{
m min}) \left(rac{T}{T_c}
ight)^4 - V(\mu_t)} \quad rac{\partial S_4}{\partial \mu_t} = 0$$

Tunnaling naint

- ✓ A large N dependence.
- ✓ A shallower potential leads to a larger bounce action.

Transition Rate



The phase transition can be completed for N < 16 !

Supercooling

The phase transition is completed, but there is still a supercooling phase.

The vacuum energy dominates the energy density of the Universe and **mini-inflation** takes place before the phase transition is completed.

The e-folding number of mini-inflation :

$$N_e \simeq \log\left(rac{T_c}{T_n}
ight) \qquad N_e \lesssim \log(1\,{
m TeV}/1\,{
m GeV}) \simeq 7$$

Dilution of dark matter and baryon asymmetry if they are produced before the phase transition.

The dilution factor $\sim 10^{-9}$

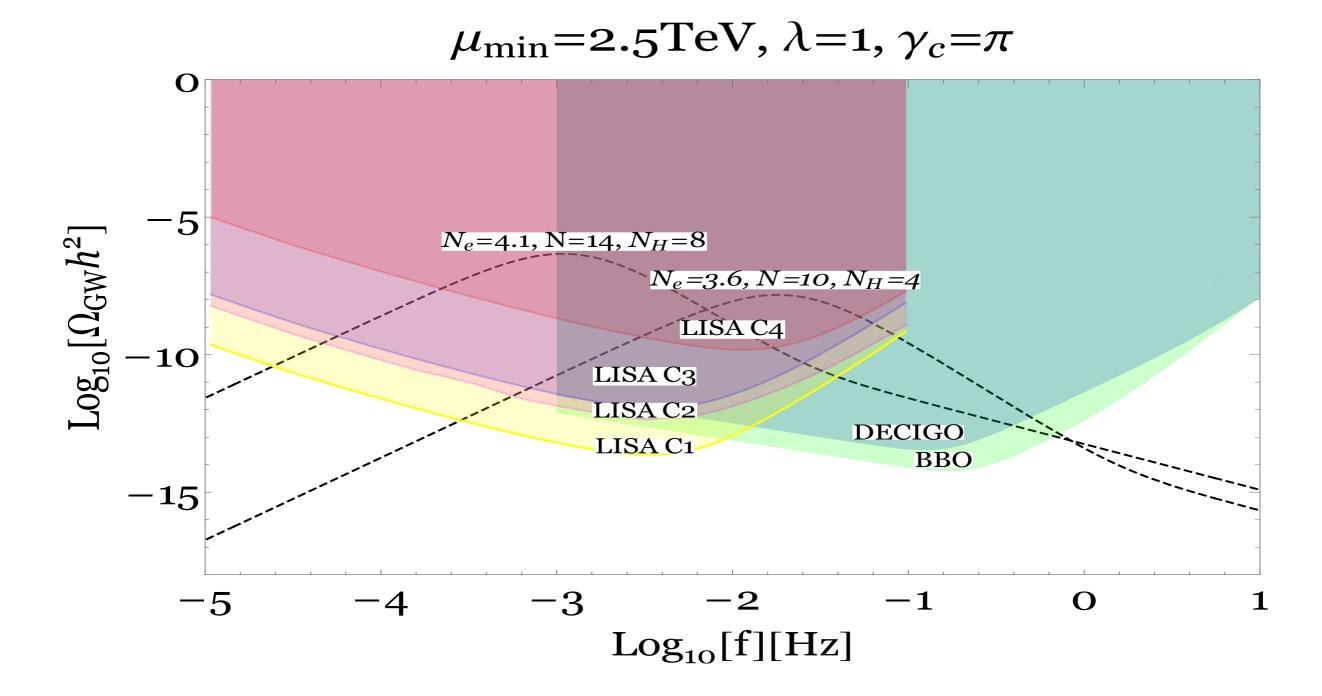
We need a very large amount of dark matter and baryon asymmetry before the phase transition or need to produce them after the phase transition.



QCD axion, Affleck-Dine baryogenesis, ...

Gravitational Waves

A long supercooling epoch results in an almost maximal GW amplitude detected by future experiments !



AdS/CFT

According to the AdS/CFT correspondence...

The RS model is dual to a nearly-conformal strongly-coupled 4D field theory.

 \checkmark The number of colors in the 4D CFT : $N\equiv 2\pi (M_5/k)^{3/2}$

Quantum gravity effects are neglected \rightarrow Large N

✓ The existence of the IR brane (in absence of its stabilization mechanism)

 ← Dilation invariance of the CFT is spontaneously broken (Scale)

✓ Radion → A massless Nambu-Goldstone boson called dilaton

✓ The RS picture provides calculable models of composite Higgs.

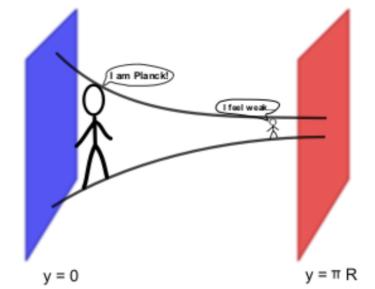
AdS/CFT

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At low temperature ...

The confined phase of the CFT

← The compact RS model

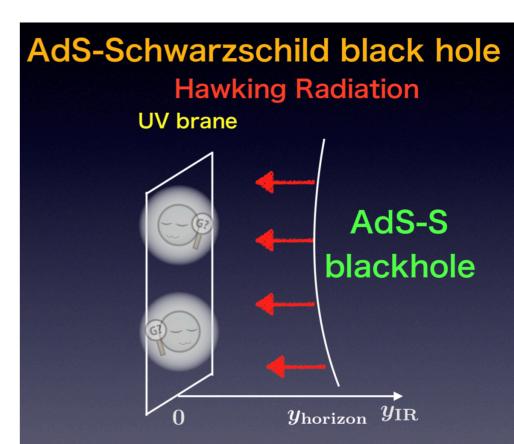




At high temperature ...

The de-confined phase of the CFT

 ← The AdS-Schwarzschild (AdS-S) black hole

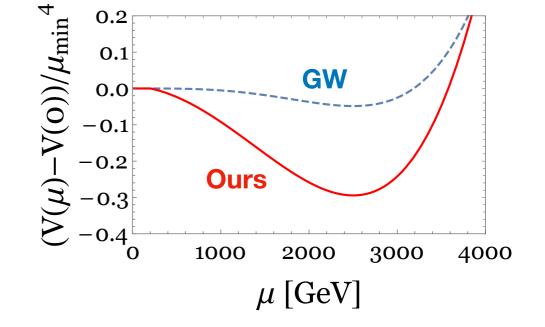


AdS/CFT

Scale invariance of the CFT suppresses the phase transition.

The Goldberger-Wise mechanism

A **small** deformation of the CFT to explicitly break the scale invariance.



<u>Our mechanism</u>

The scale invariance is broken by the quantum effect of a dark gauge.

Asymptotic freedom assures that the effect is only important near the confinement scale.



Summary

- ✓ A new radion stabilization mechanism in the RS model, introducing <u>a bulk SU(N_H) gauge field</u> which confines at a TeV scale.
- ✓ The radion potential can be stabilized by <u>the balance between the</u> <u>vacuum energy from the confinement and the IR brane tension</u>.
- ✓ Asymptotic freedom makes the vacuum energy irrelevant at the Planck scale and <u>the back-reaction to the gravitational action is negligible</u>.
- \checkmark The phase transition from the AdS-S spacetime is of the first order.
- ✓ The phase transition is completed even when the 5D Planck scale is much larger than the AdS curvature scale.
- \checkmark <u>A mini-inflation</u> occurs before the phase transition is completed.
- ✓ <u>The produced GW can be detected</u> by future experiments.

Thank you.