

2020 IAS program on High Energy physics

Higgs self-coupling prospect

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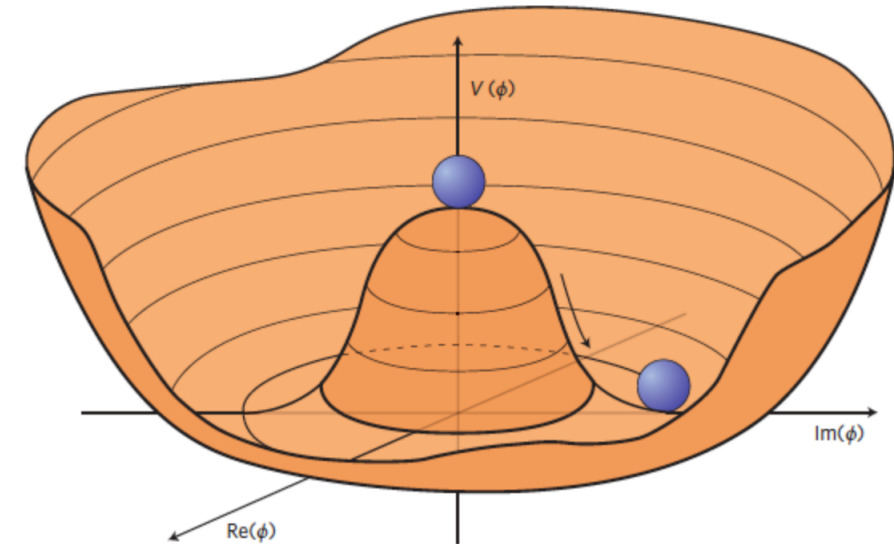
Introduction

- ◆ The Higgs particle is responsible for the masses of elementary particles.

	I	II	III	
mass →	2.4 MeV	1.27 GeV	171.2 GeV	0
charge →	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0
spin →	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1
name →	u up	c charm	t top	γ photon
	4.8 MeV	104 MeV	4.2 GeV	0
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	0
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1
Quarks	d down	s strange	b bottom	g gluon
	<2.2 eV	<0.17 MeV	<15.5 MeV	91.2 GeV
	0	0	0	0
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	Z⁰ Z boson
	0.511 MeV	105.7 MeV	1.777 GeV	80.4 GeV
	-1	-1	-1	± 1
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1
Leptons	e electron	μ muon	τ tau	W[±] W boson
				125 GeV/c ²
				H Higgs boson

$$\mathcal{L} = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} + i\bar{\Psi}\not{D}\psi + \boxed{D_{\mu}\Phi^{\dagger}D^{\mu}\Phi} - V(\Phi) + \boxed{\bar{\Psi}_L\hat{Y}\Phi\Psi_R} + h.c.$$

Gauge coupling Yukawa coupling



- ◆ Higgs potential approximation:

$$V(h) = \frac{1}{2}m_H^2h^2 + \boxed{\lambda_3vh^3 + \frac{1}{4}\lambda_4h^4}$$

Self-coupling

with $\lambda_3^{\text{SM}} = \lambda_4^{\text{SM}} = \frac{m_H^2}{2v^2}$
 $K_{\lambda} = K_3 = \frac{\lambda_{\text{HHH}}}{\lambda_{\text{HHH}}^{\text{SM}}}$

The measurement of Higgs self-coupling is a high priority goal for all the future colliders

How to measure the tri-linear self-coupling

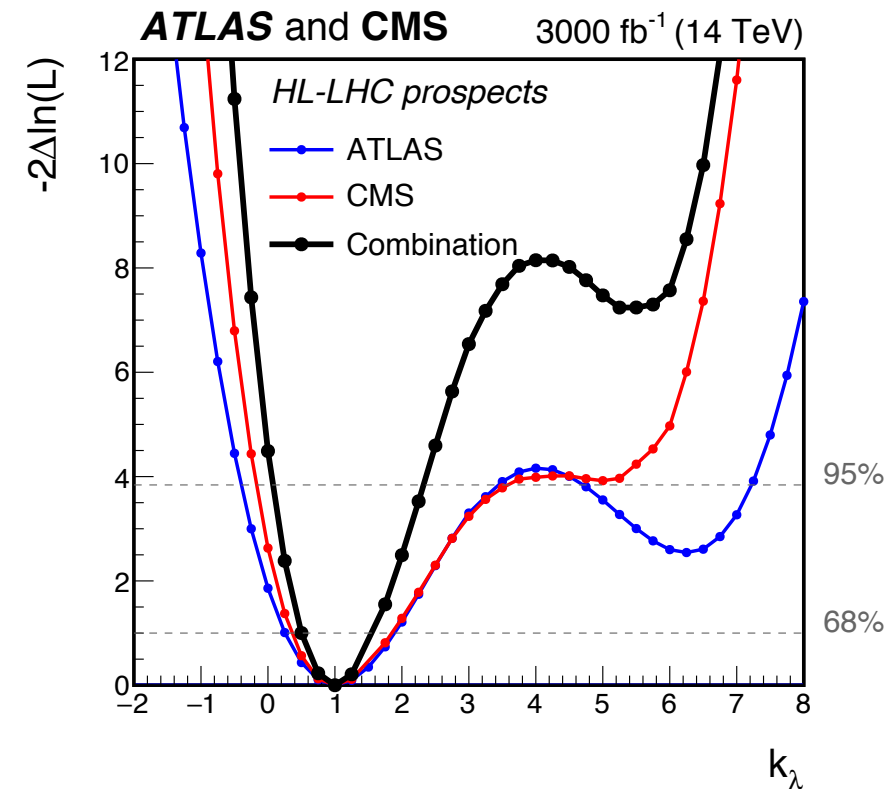
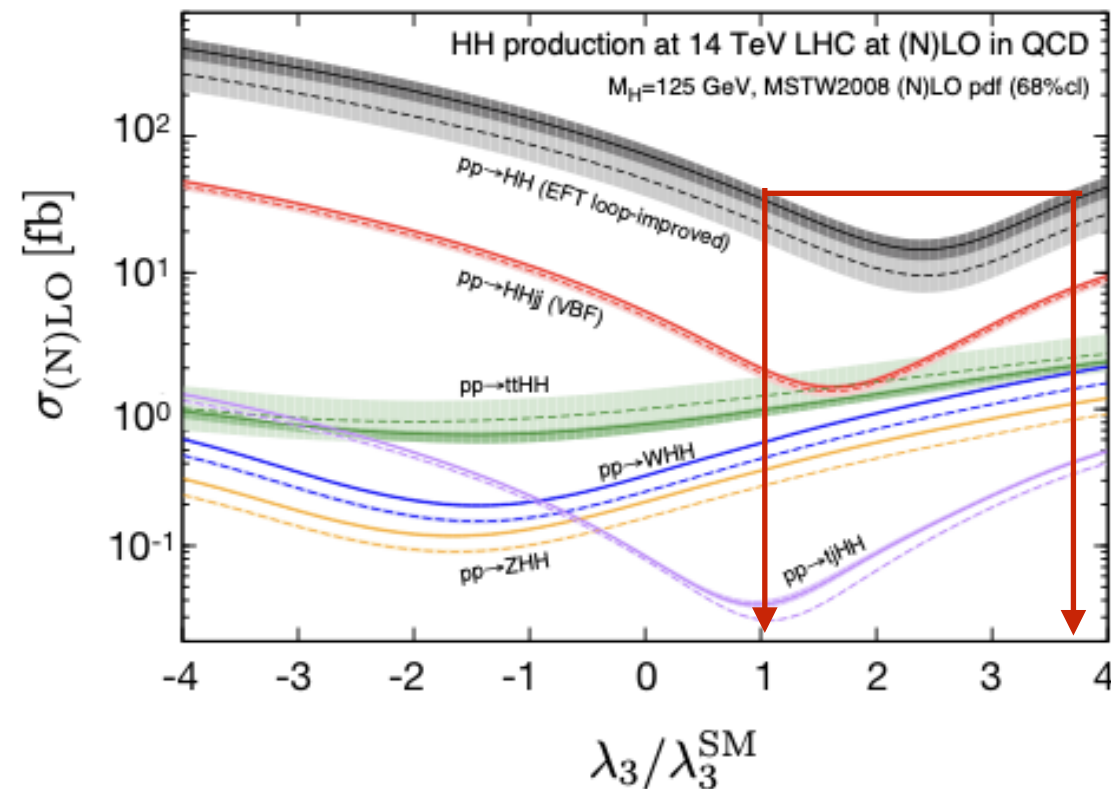
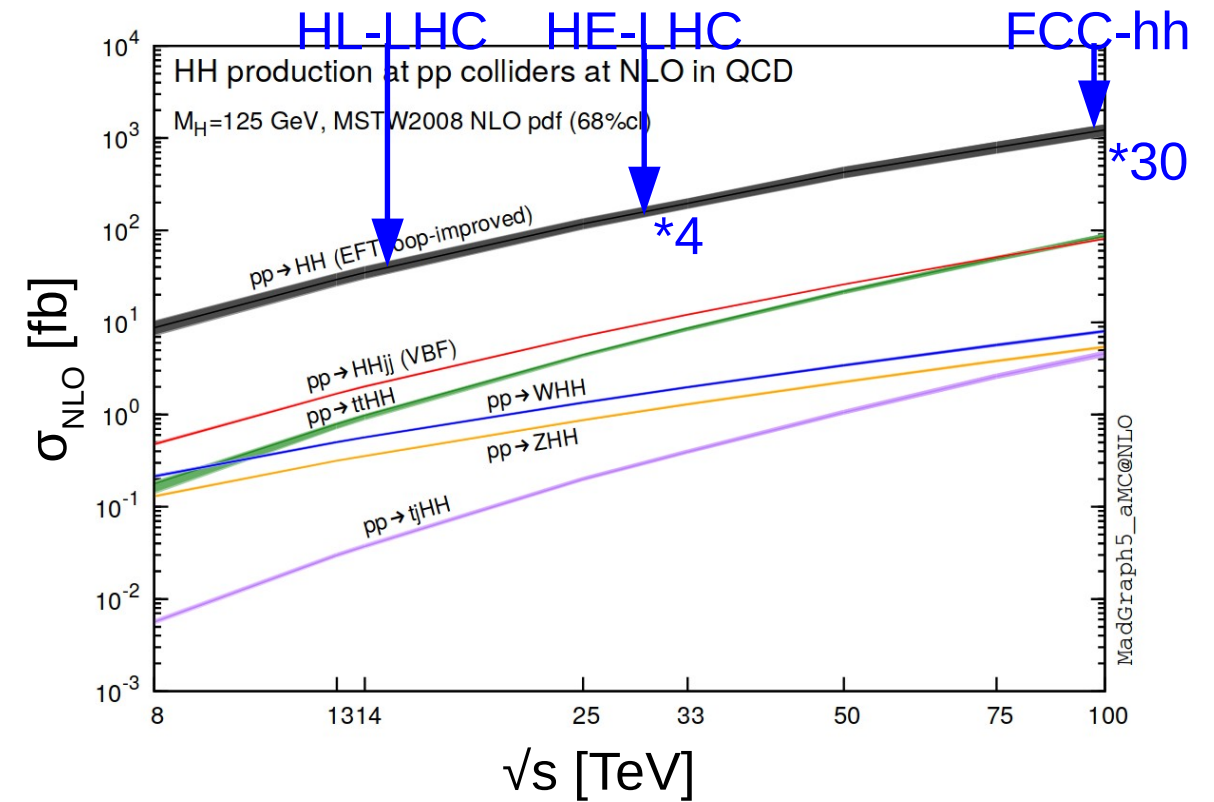
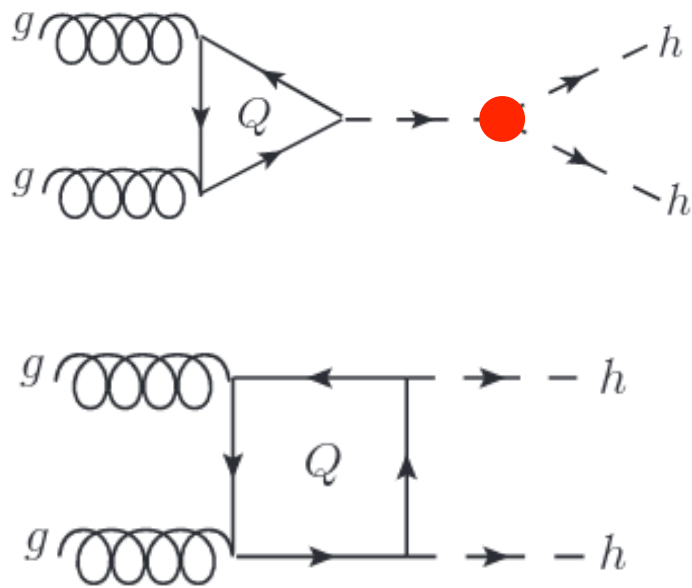
Timeline of various collider projects

	T ₀				+5					+10					+15					+20			...	+26
ILC	0.5/ab 250 GeV					1.5/ab 250 GeV					1.0/ab 500 GeV				0.2/ab 2m _{top}	3/ab 500 GeV								
CEPC	5.6/ab 240 GeV						16/ab M _Z	2.6 /ab 2M _W											SppC =>					
CLIC	1.0/ab 380 GeV								2.5/ab 1.5 TeV							5.0/ab => until +28 3.0 TeV								
FCC	150/ab ee, M _Z		10/ab ee, 2M _W		5/ab ee, 240 GeV			1.7/ab ee, 2m _{top}														hh.eh =>		
LHeC	0.06/ab					0.2/ab				0.72/ab														
HE-LHC	10/ab per experiment in 20y																							
FCC eh/hh	20/ab per experiment in 25y																							

- ◆ Hadron colliders: **double Higgs production**, **Single Higgs production with NLO-EW correction**
- ◆ Low-energy lepton colliders: **Single Higgs production with NLO-EW correction**
- ◆ High-energy lepton colliders: **double Higgs-strahlung**, **vector boson fusion**

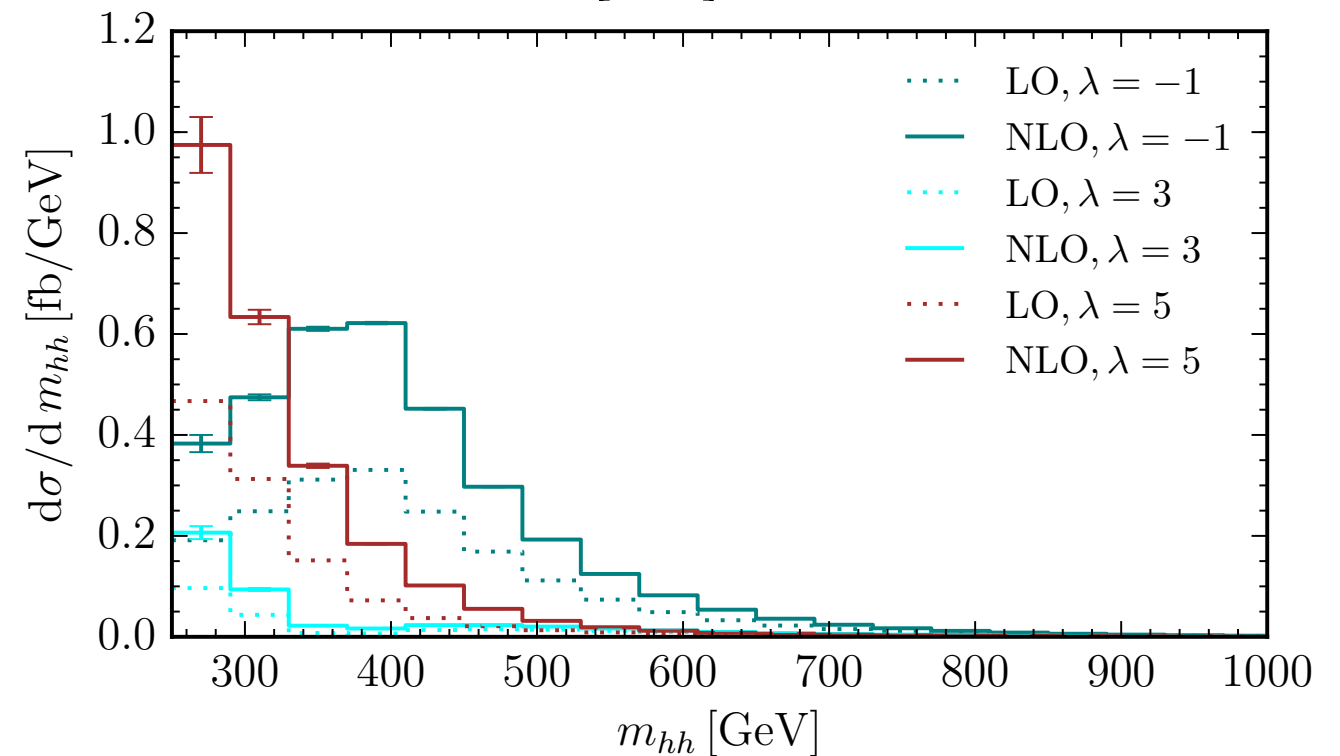
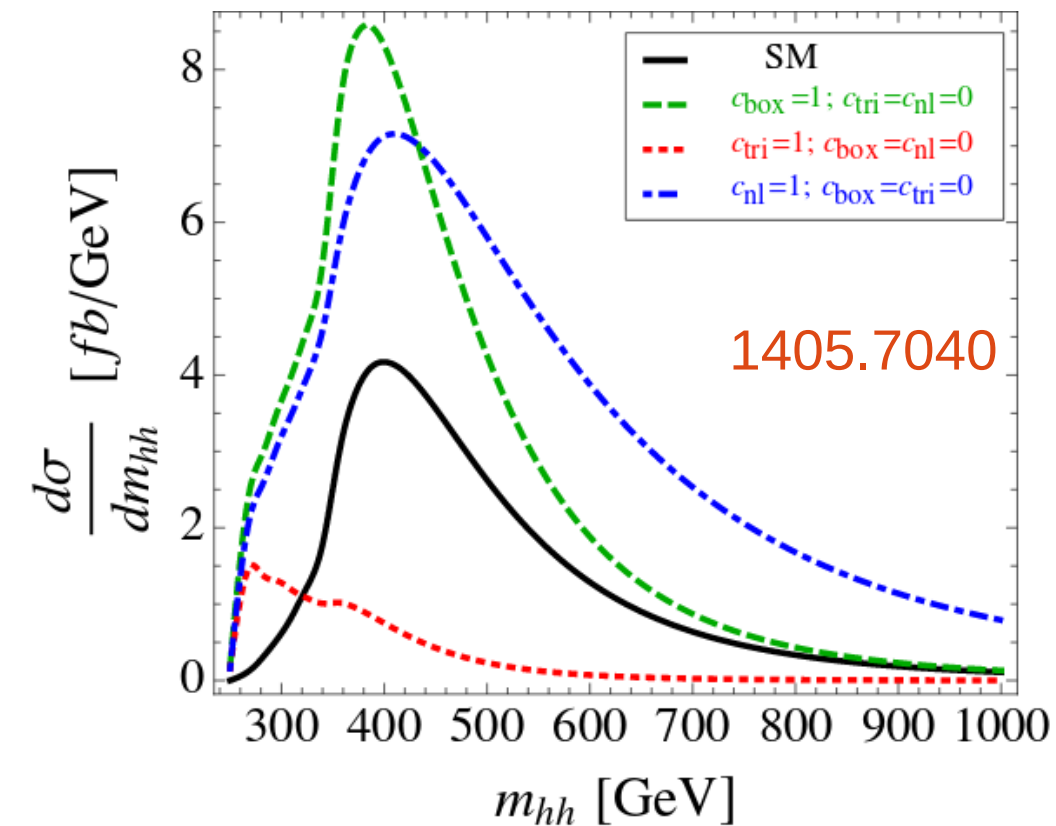
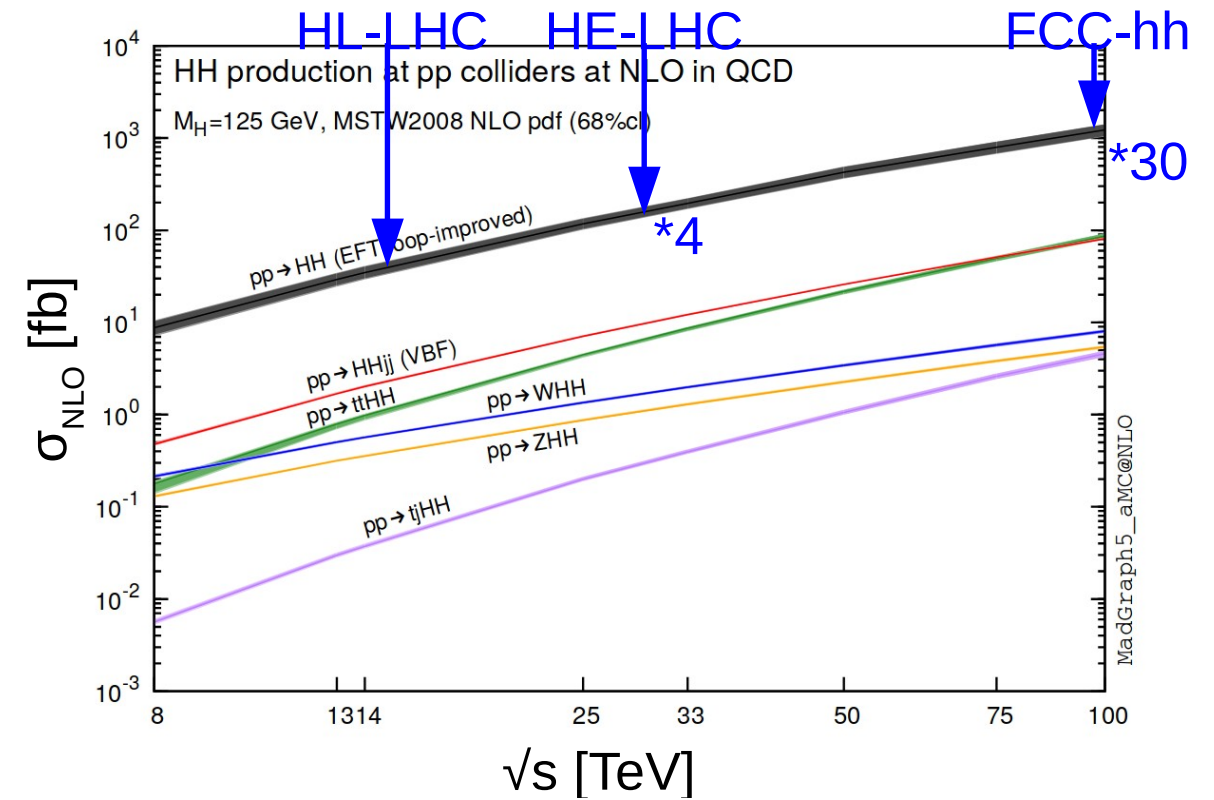
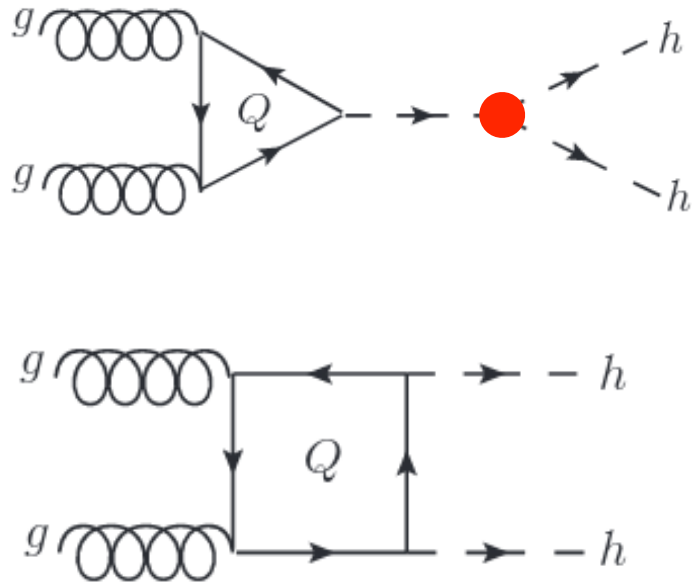
Hadron collider: Di-Higgs production

Destructive interference between triangle- and box- diagrams ($\sigma(HH)/\sigma(H)=0.1\%$)



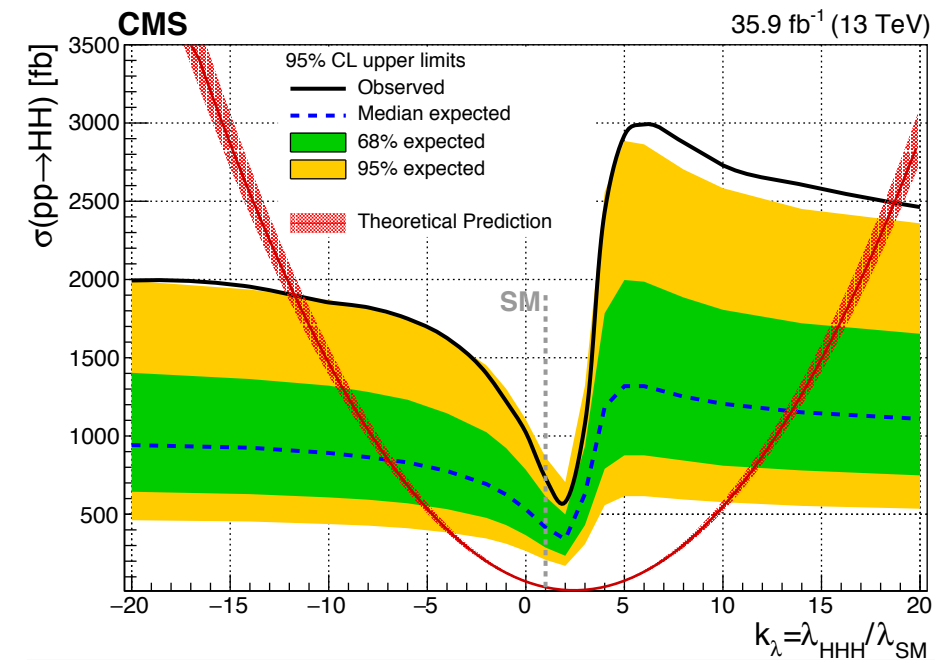
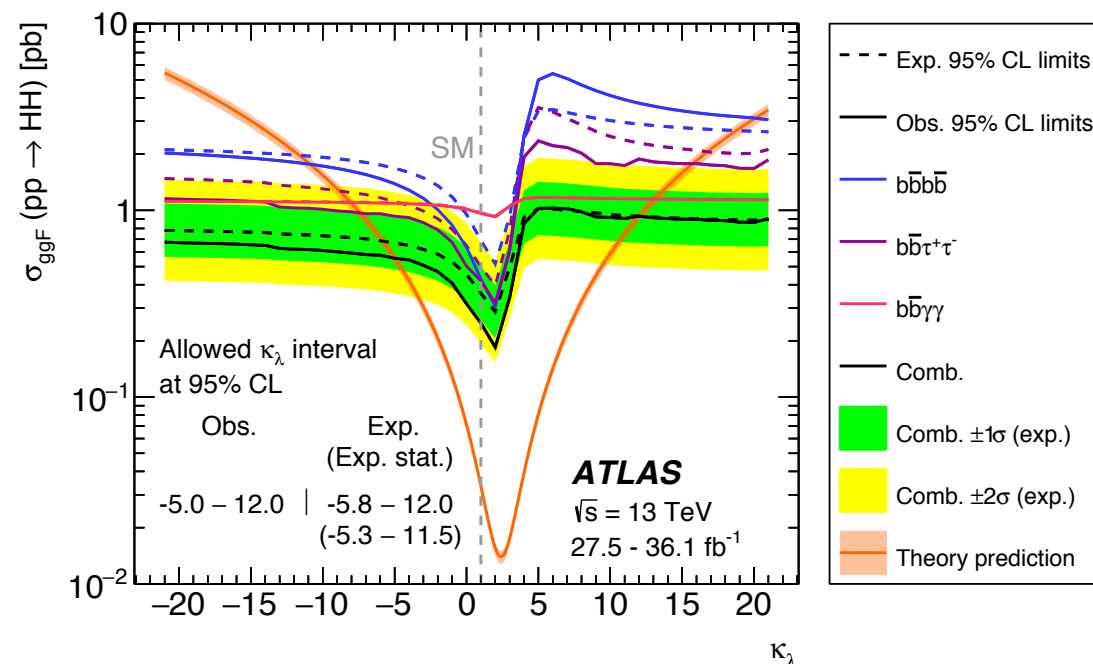
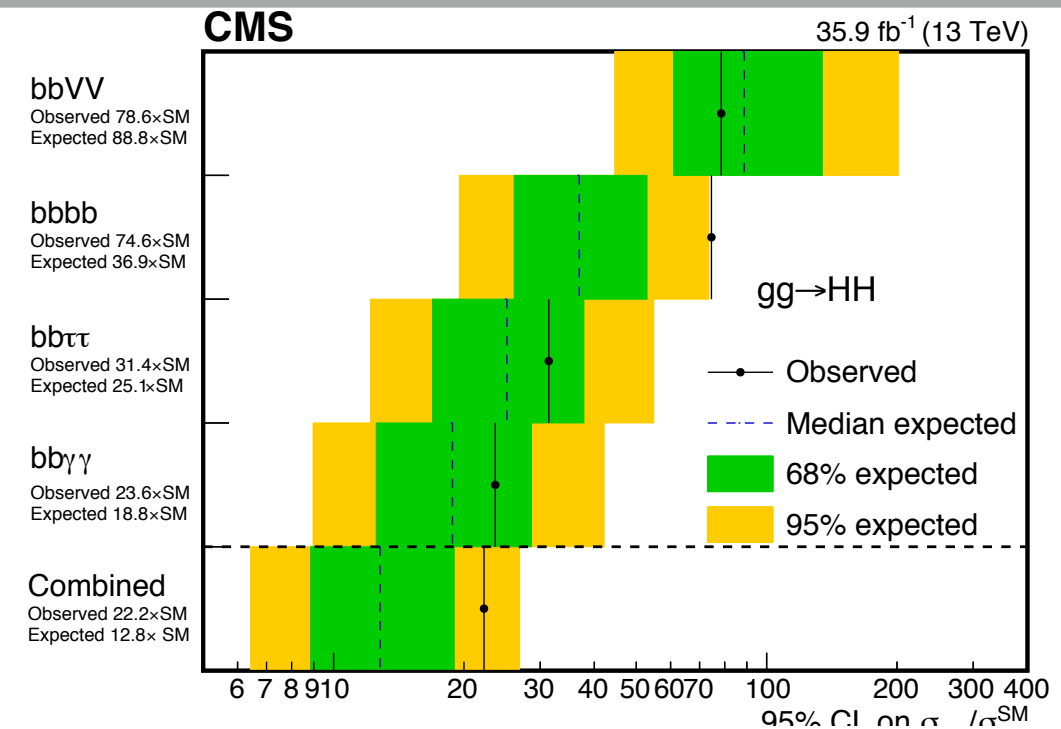
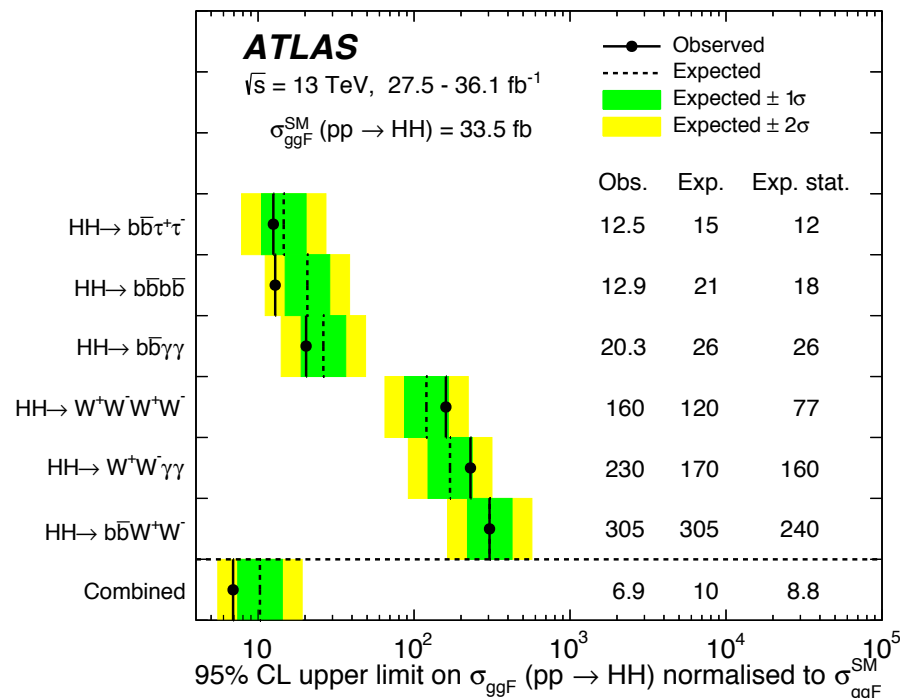
Hadron collider: Di-Higgs production

Destructive interference between triangle- and box- diagrams ($\sigma(HH)/\sigma(H)=0.1\%$)



Current measurement

Assume all kinematic properties of HH pair are same as SM prediction, and only ggF XS can deviate from SM (the cross section uncertainty $\sim 10\%$ was not included in the fitting.)

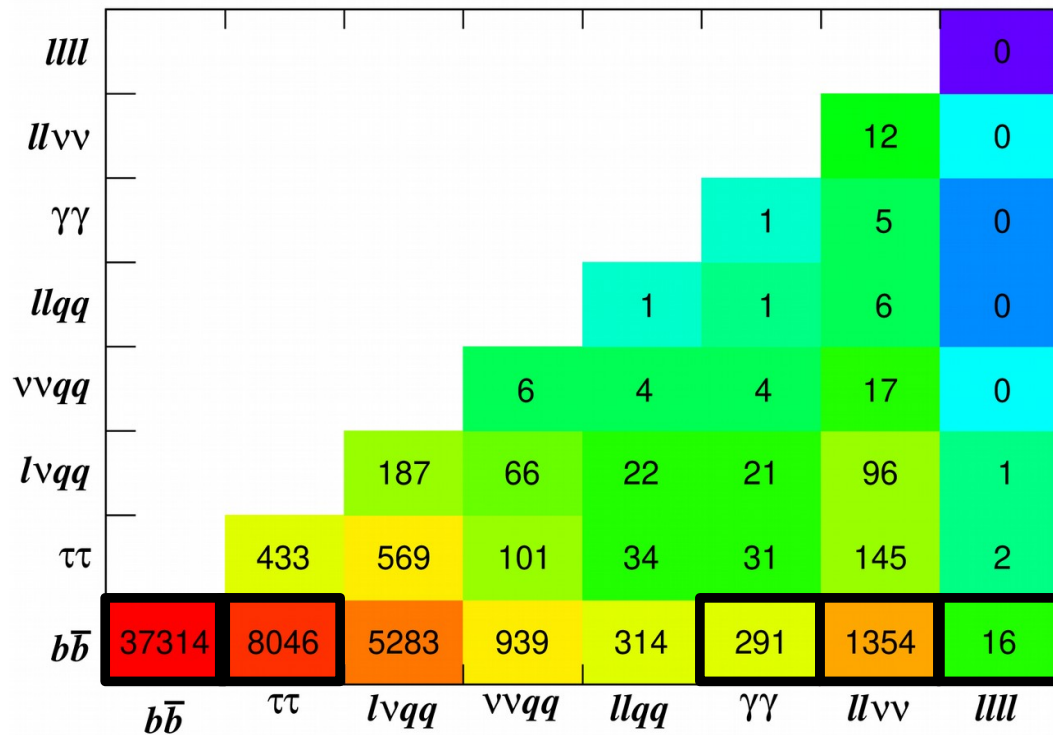


Getting close to **10*SM** rate for Di-Higgs production

Obs (Exp) κ_λ @ 95% CL: [-5.0,12.0] ([-5.8, 12.0]) for ATLAS , [-11.8, 18.8](-7.1, 13.6) for CMS

Prospect @ HL-LHC

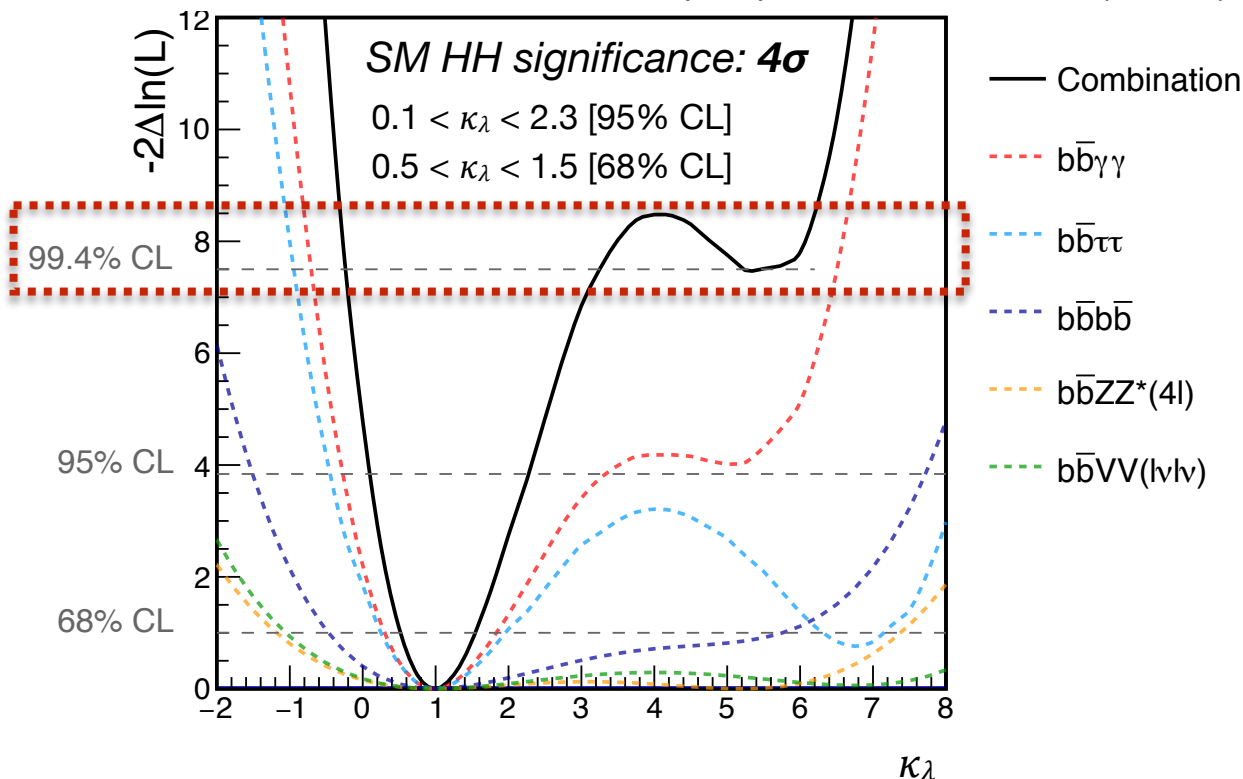
Expected SM HH events for 3000 fb⁻¹



	ATLAS	CMS	
bbbb	extrapolation	parametric	Largest BR 😊 Large multijet and tt bkg 😞
bbττ	extrapolation	parametric	Sizeable BR 😊 Relatively small bkg 😊
bbyy	smearing	parametric	Small BR 😞 Good diphoton resolution 😊 Relatively small bkg 😊
bbVV (→lvlv)		parametric	Large BR 😊 Large bkg 😞
bbZZ (→4l)		parametric	Very small BR 😞 Very small bkg 😊

ATLAS and CMS HL-LHC prospects

3 ab⁻¹ (14 TeV)

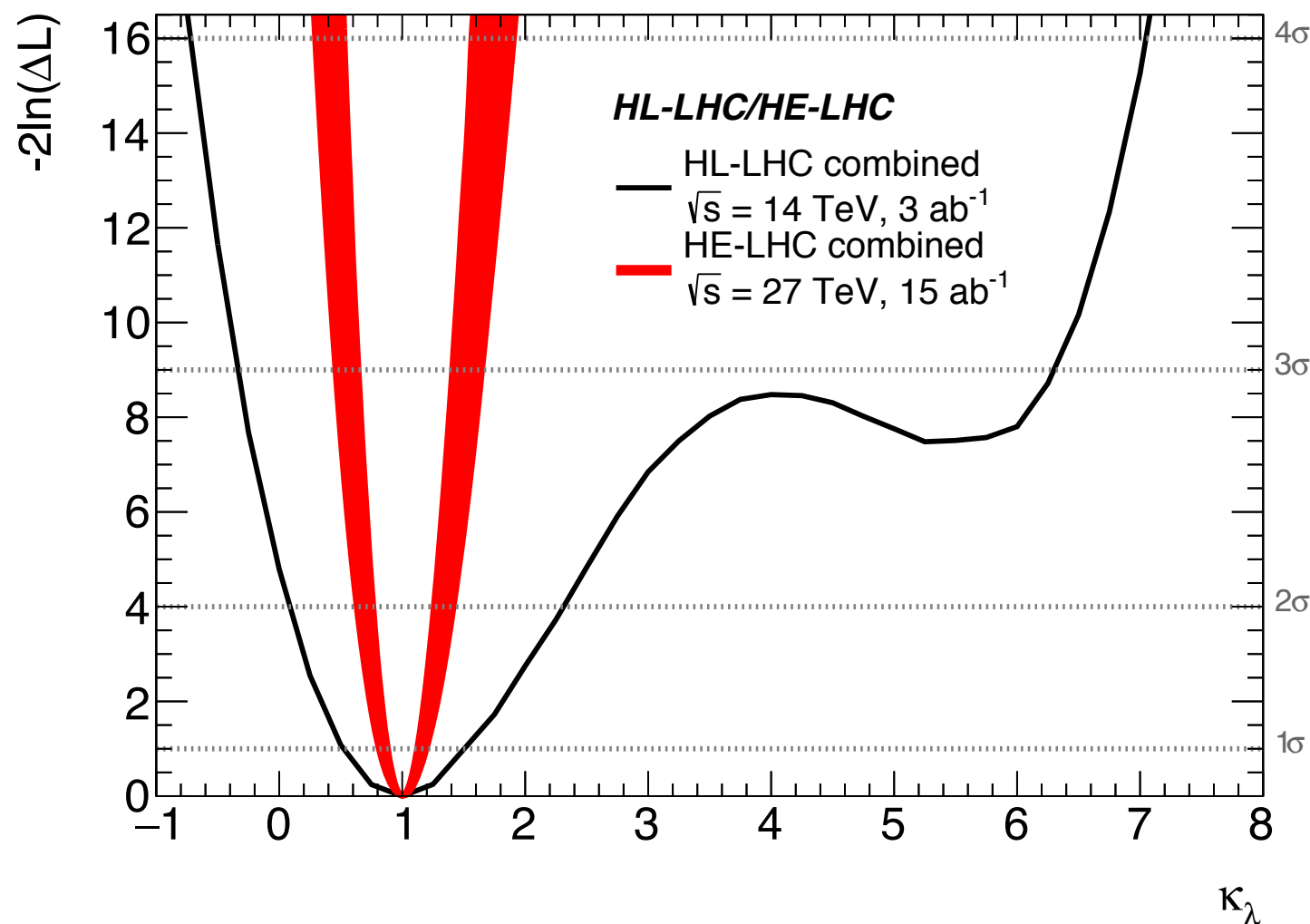


	Statistical-only		Statistical + Systematic	
	ATLAS	CMS	ATLAS	CMS
$HH \rightarrow b\bar{b}b\bar{b}$	1.4	1.2	0.61	0.95
$HH \rightarrow b\bar{b}\tau\tau$	2.5	1.6	2.1	1.4
$HH \rightarrow b\bar{b}\gamma\gamma$	2.1	1.8	2.0	1.8
$HH \rightarrow b\bar{b}VV(ll\nu\nu)$	-	0.59	-	0.56
$HH \rightarrow b\bar{b}ZZ(4l)$	-	0.37	-	0.37
combined	3.5	2.8	3.0	2.6
	Combined		Combined	
	4.5		4.0	

**Room with the exploration
of the dependence on κ_λ**

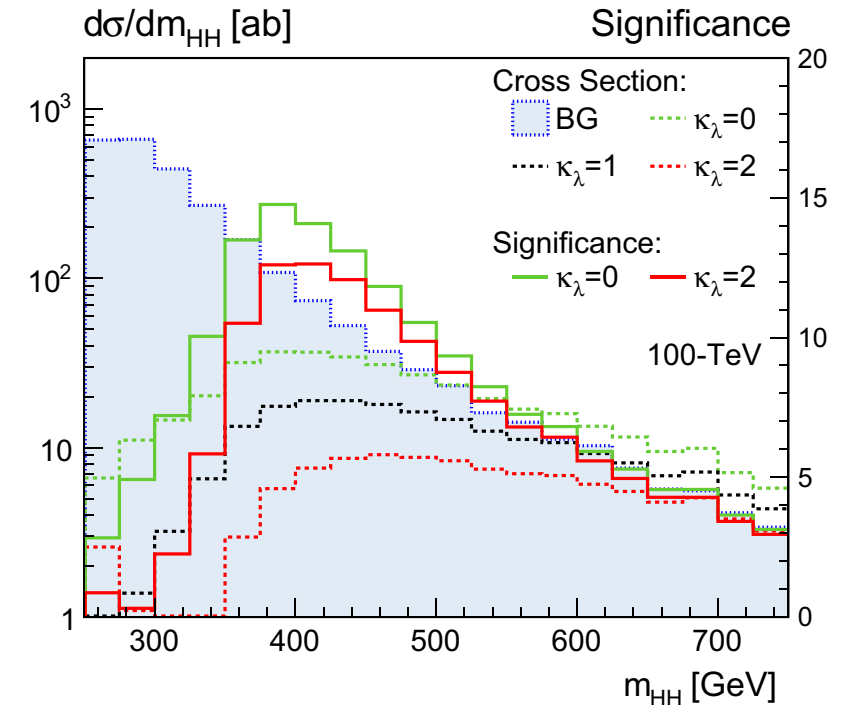
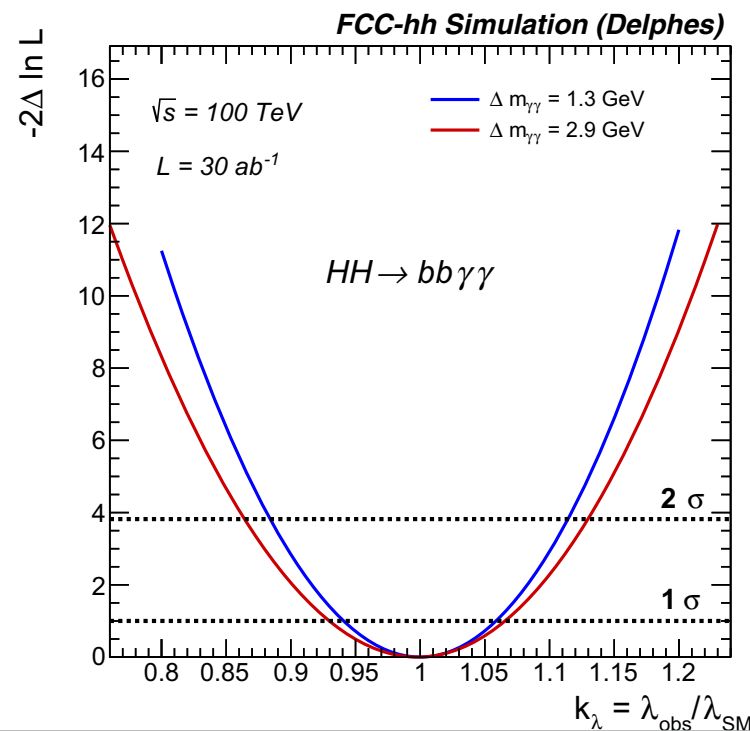
Prospect @ HE-LHC

- ◆ Extrapolate ATLAS HL-LHC results to HE-LHC:
 - scale **cross-section (*4)** from 14TeV to 27TeV and **luminosity (*5)** to 15ab-1
 - **bb $\gamma\gamma$** : 7.1 σ with the precision on κ_λ of $\sim 20\%$
 - **bb $\tau\tau$** : 10.7 σ with the precision on κ_λ of $\sim 40\%$
 - **Combination**: the precision on κ_λ of 10-20%



Prospect @ FCC-hh

	$\sigma[100 \text{ TeV}](\text{fb})$	$\sigma[27 \text{ TeV}](\text{fb})$
$gg \rightarrow HH$	$1.22 \times 10^3 {}^{+0.9\%}_{-3.2\%} \pm 2.4\% \pm 4.5\%_{m_t}$	$140 {}^{+1.3\%}_{-3.9\%} \pm 2.5\% \pm 3.4\%_{m_t}$
$HHjj$	$80.5 \pm 0.5\% \pm 1.8\%$	$1.95 \pm 2\% \pm 2.4\%$
W^+HH	$4.7 \pm 1\% \pm 1.8\%$	$0.37 \pm 0.4\% \pm 2.1\%$
W^-HH	$3.3 \pm 4\% \pm 1.9\%$	$0.20 \pm 1.3\% \pm 2.7\%$
ZHH	$8.2 \pm 5\% \pm 1.7\%$	$0.41 \pm 3\% \pm 1.8\%$
$t\bar{t}HH$	$82.1 \pm 8\% \pm 1.6\%$	$0.95 {}^{+1.7\%}_{-4.5\%} \pm 3.1\%$

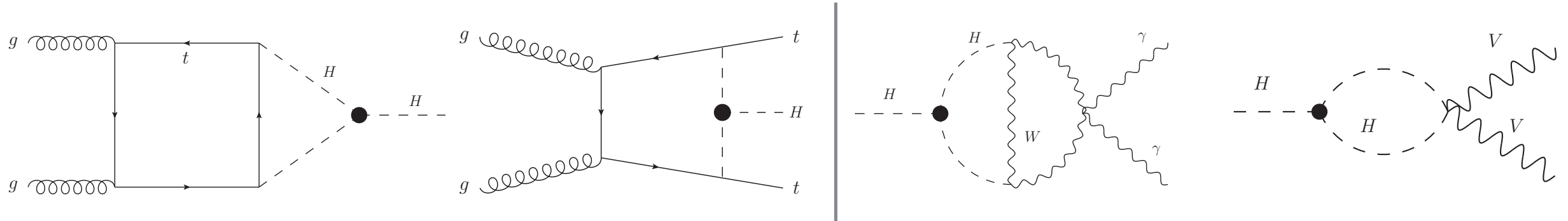


- ◆ Most sensitivity from $b\bar{b}\gamma\gamma$ channel: different variation scenarios on photon efficiency, resolution, background level etc $\rightarrow$ 5-7% uncertainty on κ_λ .
- ◆ More sensitivity can be achieved via kinematic exploration: m_{HH} , Higgs p_T and various angular correlation

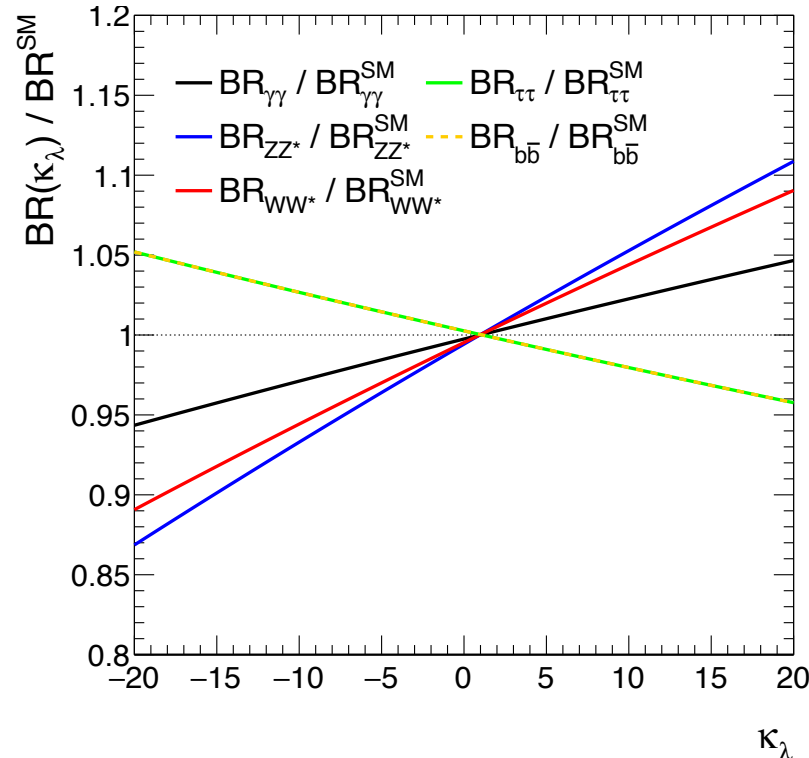
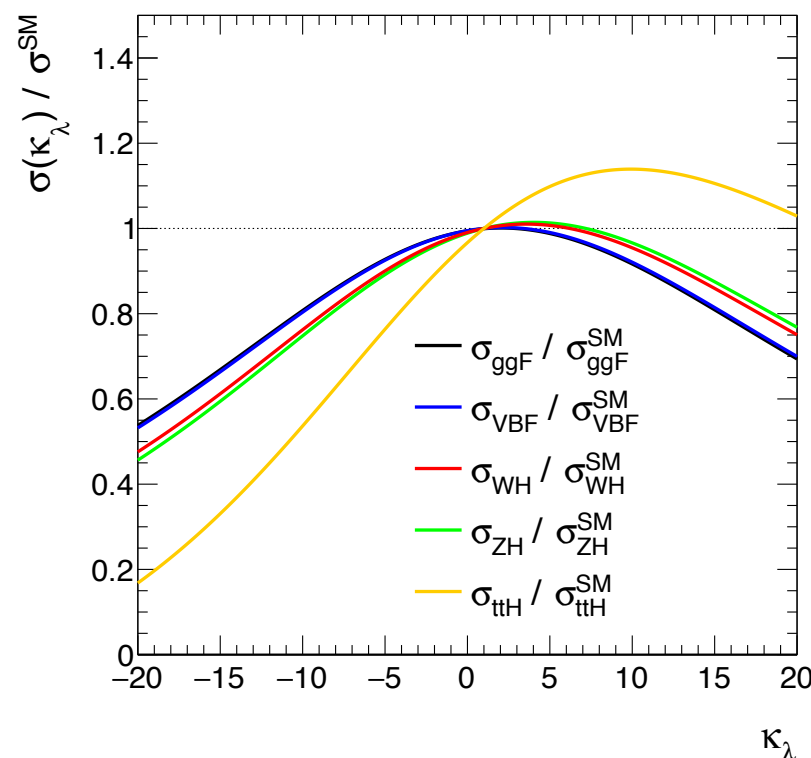
	$b\bar{b}\gamma\gamma$	$b\bar{b}ZZ^*[\rightarrow 4\ell]$	$b\bar{b}WW^*[\rightarrow 2j\ell\nu]$	$4b + \text{jet}$
$\delta\kappa_\lambda$	6.5%	14%	40%	30%

Indirect measurement from single Higgs processes

All the single Higgs production and decay processes are affected by an anomalous trilinear (**not quartic**) Higgs self coupling, parametrized by κ_λ .



All the different signal strengths μ_i^f have a different dependence on a single parameter κ_λ , which can thus be constrained via a global fit.



$$\mu_i(\kappa_\lambda, \kappa_i) = \frac{\sigma^{\text{BSM}}}{\sigma^{\text{SM}}} = Z_H^{\text{BSM}}(\kappa_\lambda) \left[\kappa_i^2 + \frac{(\kappa_\lambda - 1)C_1^i}{K_{\text{EW}}^i} \right]$$

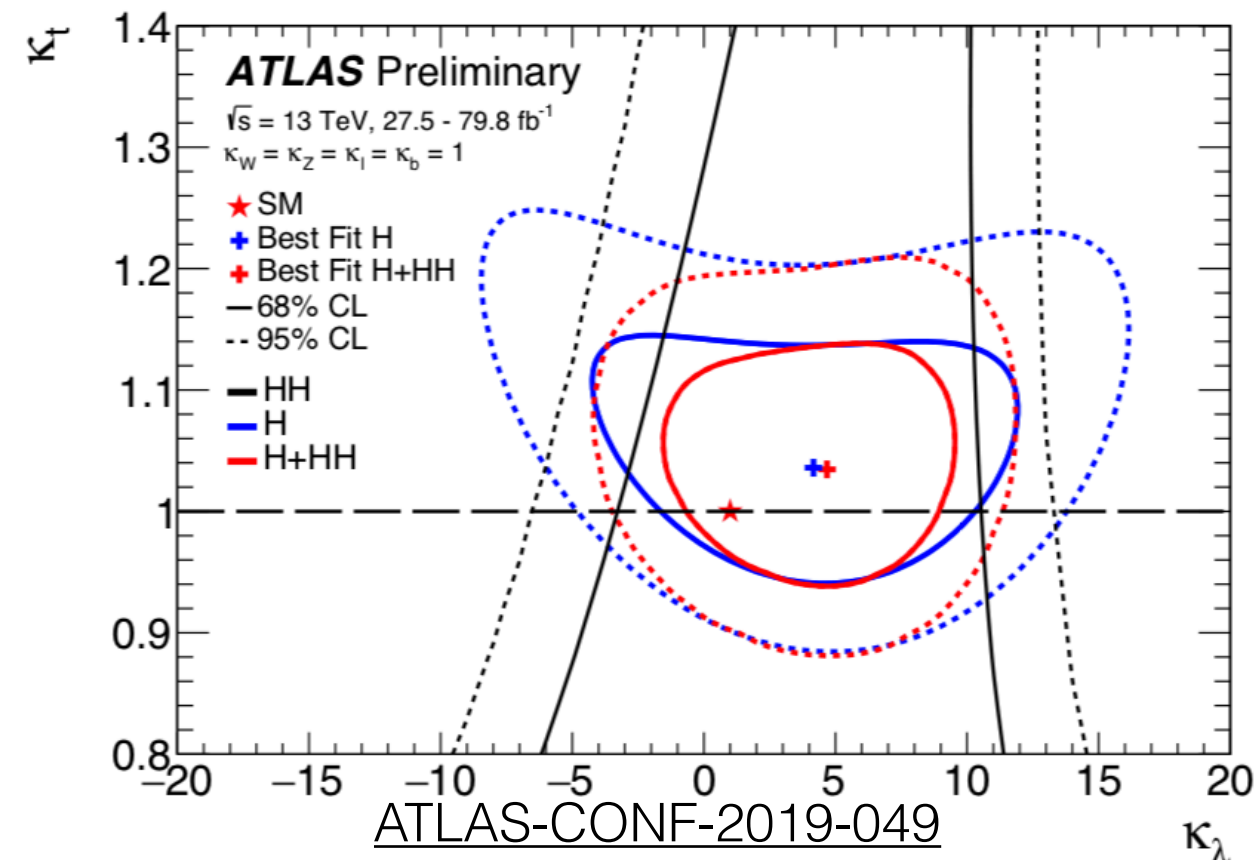
production mode	ggF	VBF	ZH	WH	$t\bar{t}H$
$C_1^i \times 100$	0.66	0.63	1.19	1.03	3.52
K_{EW}^i	1.049	0.932	0.947	0.93	1.014
κ_i^2	κ_F^2	κ_V^2	κ_V^2	κ_V^2	κ_F^2

$$\mu_f(\kappa_\lambda, \kappa_f) = \frac{\text{BR}_f^{\text{BSM}}}{\text{BR}_f^{\text{SM}}} = \frac{\kappa_f^2 + (\kappa_\lambda - 1)C_1^f}{\sum_j \text{BR}_j^{\text{SM}} \left[\kappa_j^2 + (\kappa_\lambda - 1)C_1^j \right]}$$

decay mode	$H \rightarrow \gamma\gamma$	$H \rightarrow WW^*$	$H \rightarrow ZZ^*$	$H \rightarrow b\bar{b}$	$H \rightarrow \tau\tau$
$C_1^f \times 100$	0.49	0.73	0.82	0	0
κ_f^2	$1.59\kappa_V^2 + 0.07\kappa_F^2 - 0.67\kappa_V\kappa_F$	κ_V^2	κ_V^2	κ_F^2	κ_F^2

Constraint Higgs trilinear self-coupling

- ◆ Using STXS framework, constrain Higgs boson self-coupling using NLO EW corrections on the single Higgs boson production and decay.
- ◆ Complement direct measurement from HH channels and provide more stringent constraint.



Constraint on **self-coupling (obs/exp) @ 95% CL:**

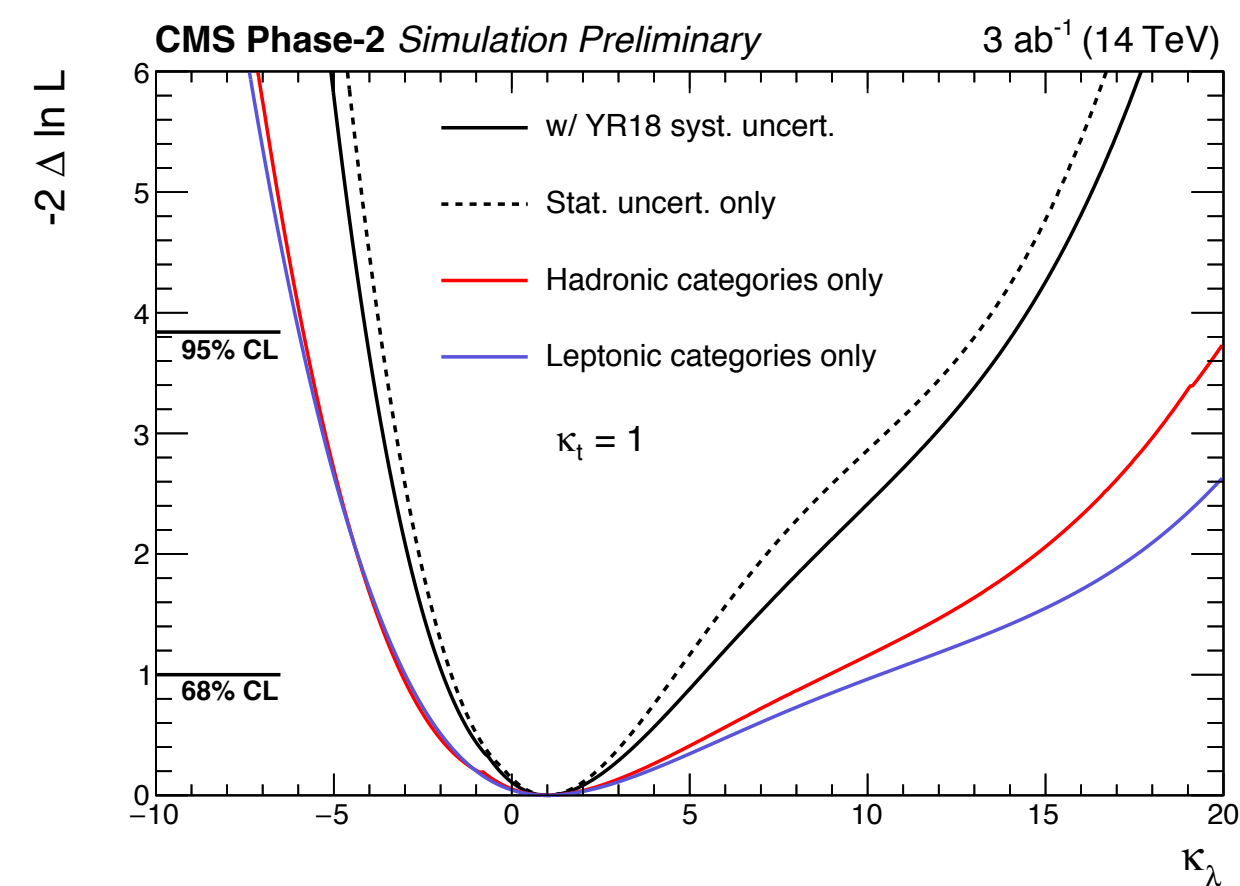
- **ATLAS (H):** $-3.2 < \kappa_\lambda < 11.9$ / $-6.2 < \kappa_\lambda < 14.4$
- **ATLAS (HH):** $-5.0 < \kappa_\lambda < 12.0$ / $-5.8 < \kappa_\lambda < 12.0$
- **ATLAS (H+HH):** $-2.3 < \kappa_\lambda < 10.3$ / $-5.1 < \kappa_\lambda < 11.2$
- **CMS(HH):** $-5.8 < \kappa_\lambda < 12.0$ / $-5 < \kappa_\lambda < 12.1$

◆ Limited access to possible BSM effect

- No consideration of the kinematic dependence on $k\lambda$ in the single Higgs process
- No consistent EFT predicts only SM coupling variation without new contact interactions.
- Combine LO and NLO effects in the two measurements with a k-framework

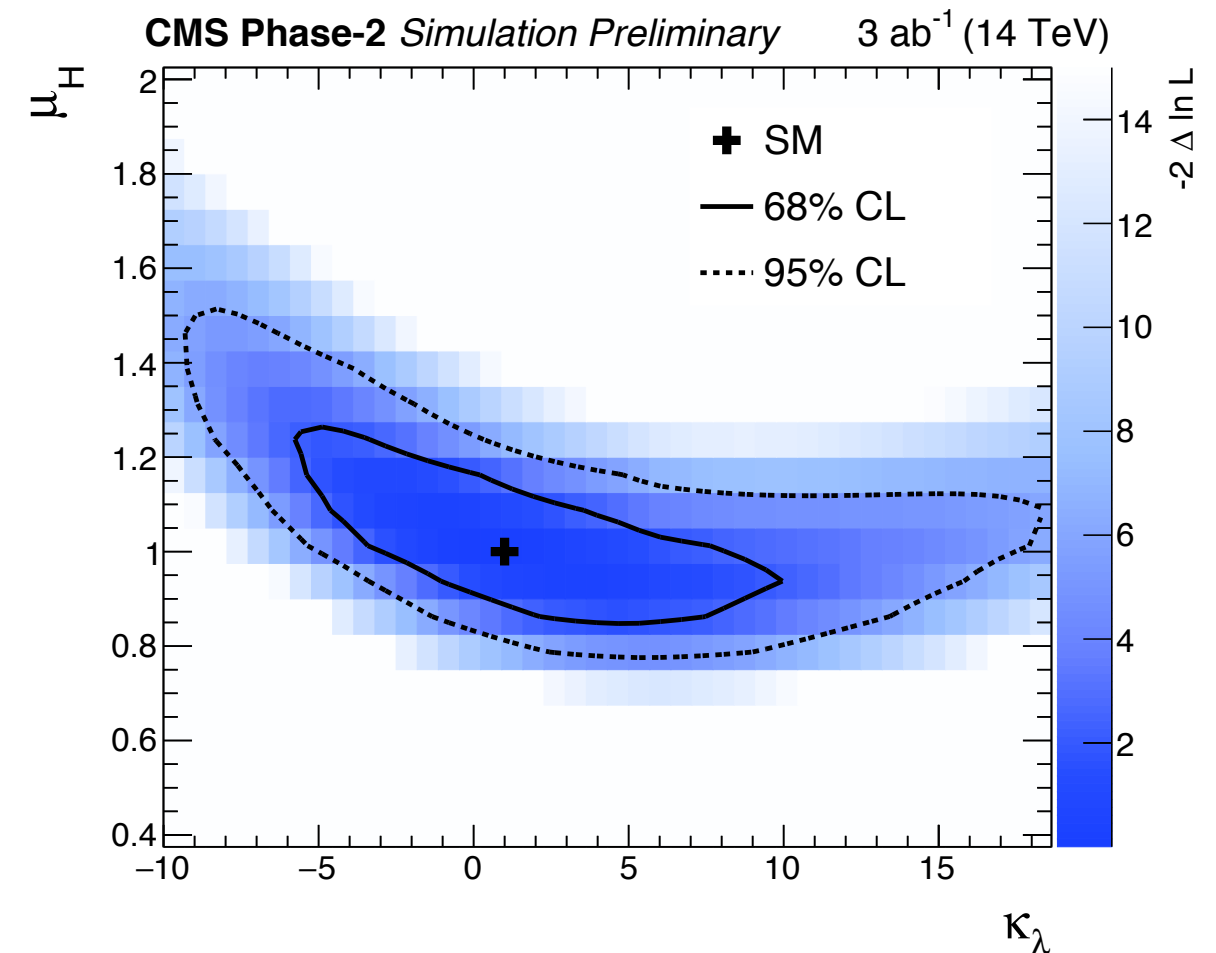
Indirect probes through differential distributions of single Higgs processes

$p_T(H)$ [GeV]	[0, 45]	[45, 80]	[80, 120]	[120, 200]	[200, 350]	> 350
ttH	5.31	4.73	3.92	2.79	1.42	0.42
tH	1.32	1.19	1.00	0.75	0.40	0.06
VH	1.66	1.23	0.77	0.35	0.02	-0.09



Constraint on **self-coupling (exp) @ 95% CL:**

- **-4.1 < κ_λ < 14.1**

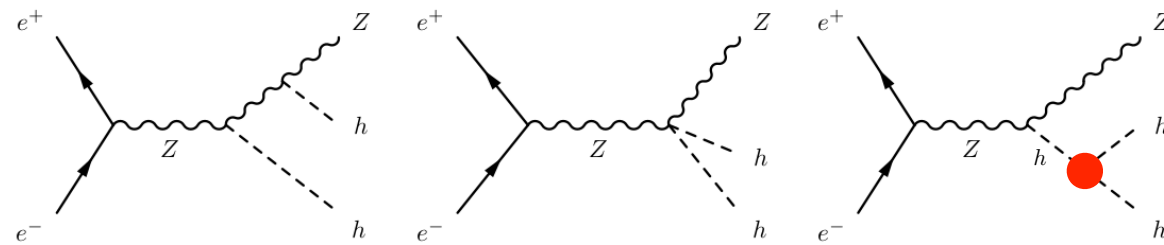


Constraint on **self-coupling (exp) @ 95% CL:**

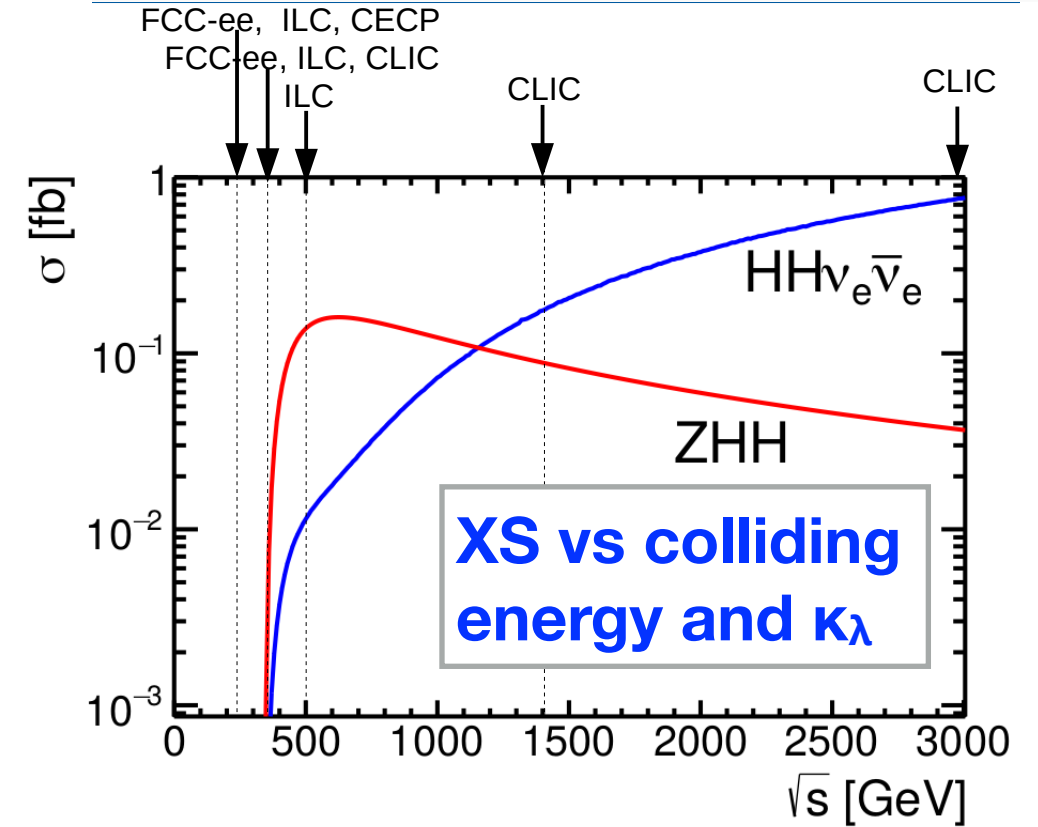
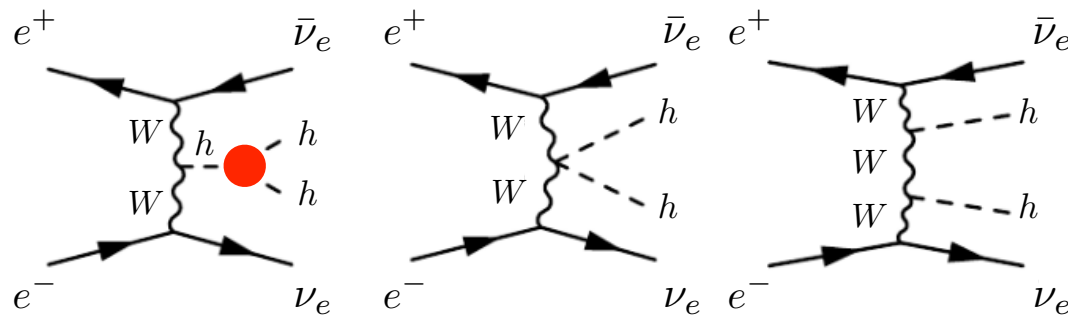
- **-7.1 < κ_λ < 14.1**

Lepton collider: Di-Higgs production

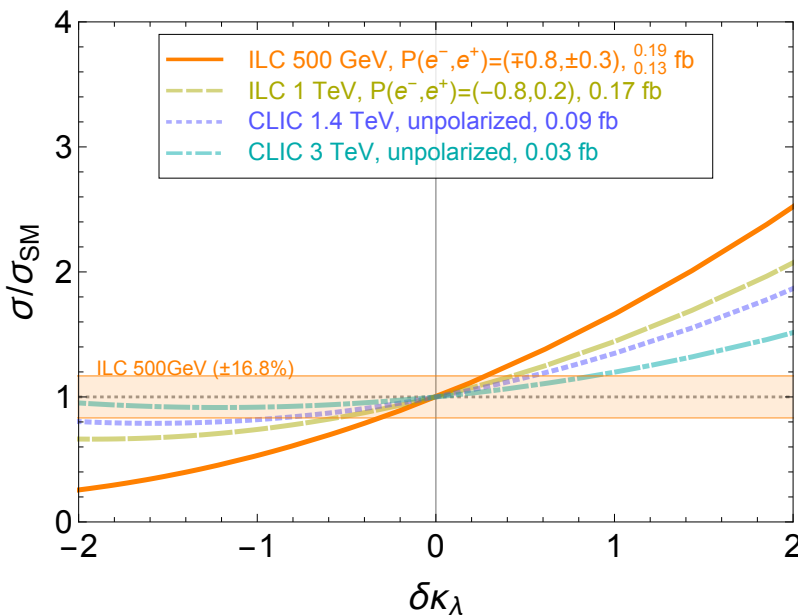
◆ Higgs-strahlung: $ee \rightarrow ZHH$



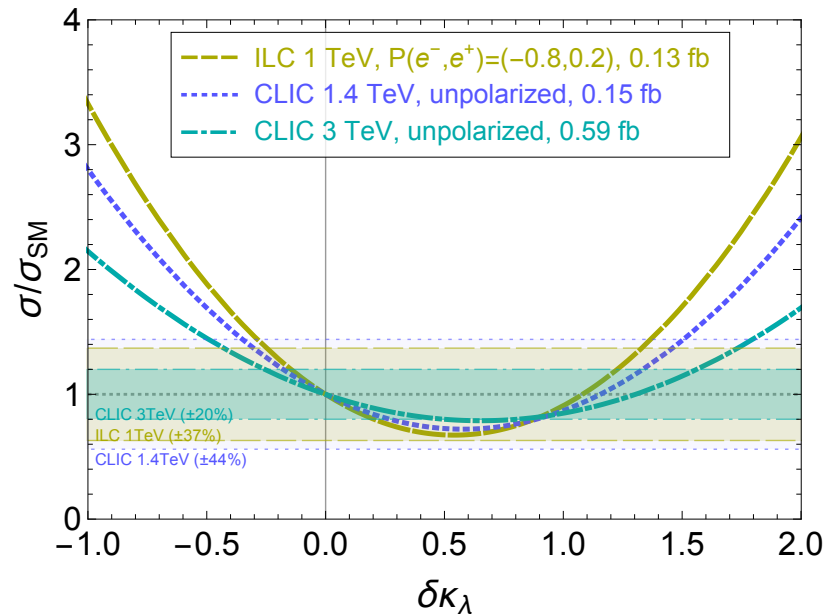
◆ VBF: $ee \rightarrow \nu\nu HH$



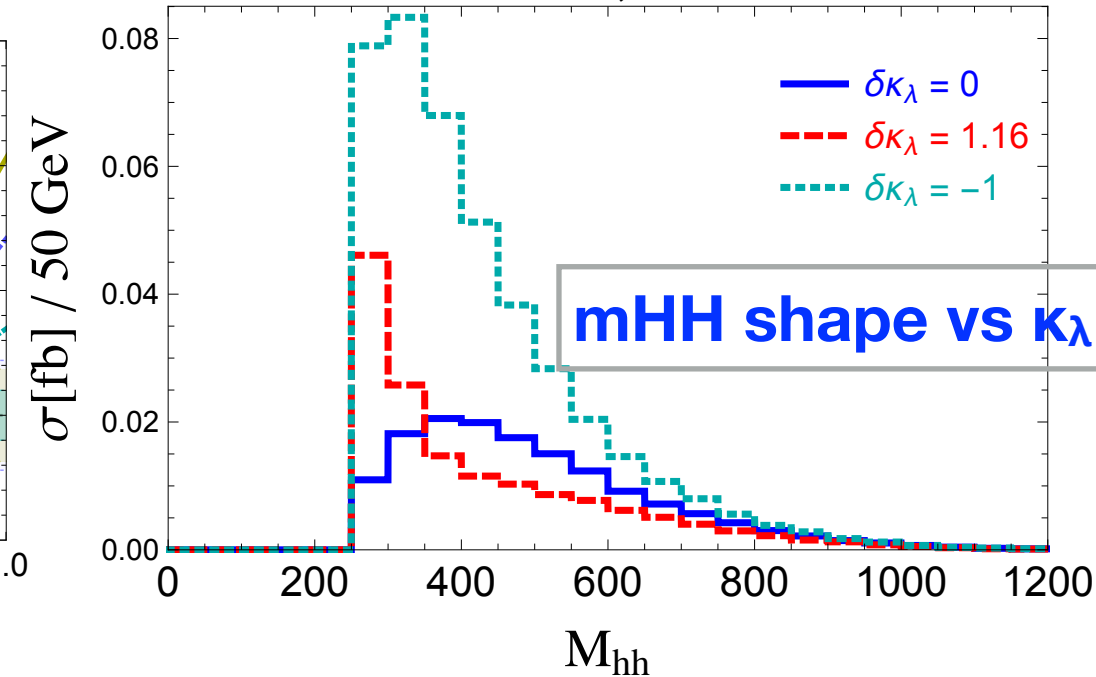
$e^+e^- \rightarrow Zhh$



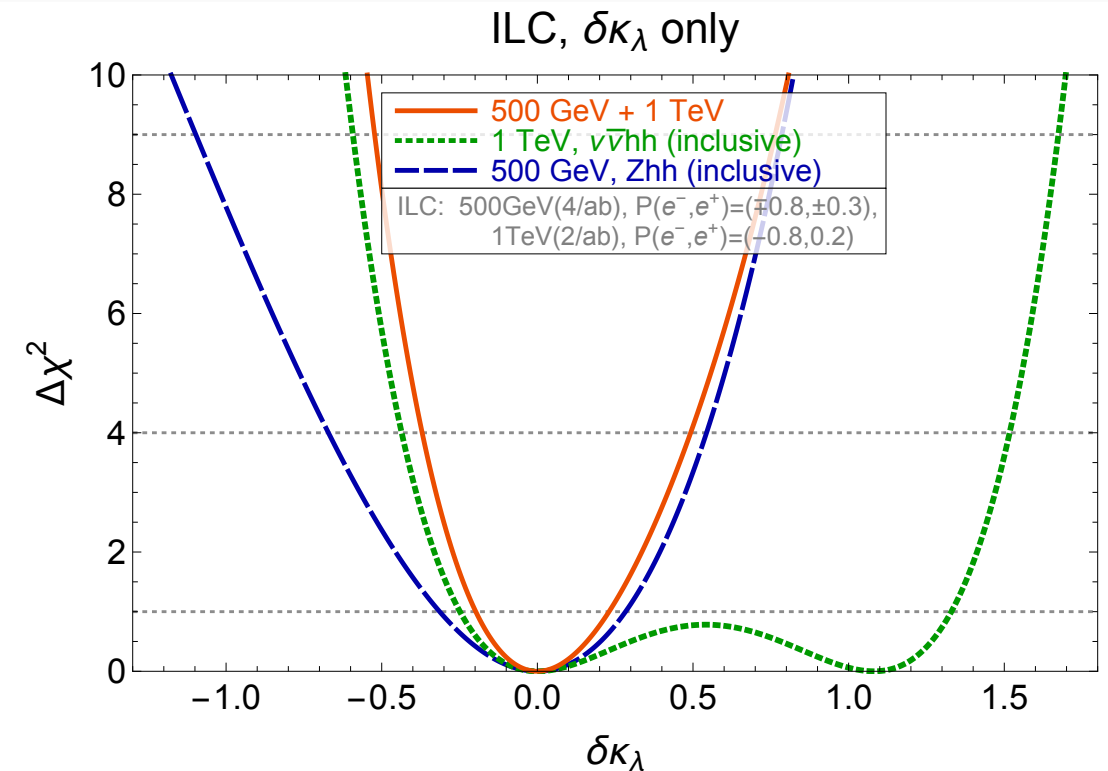
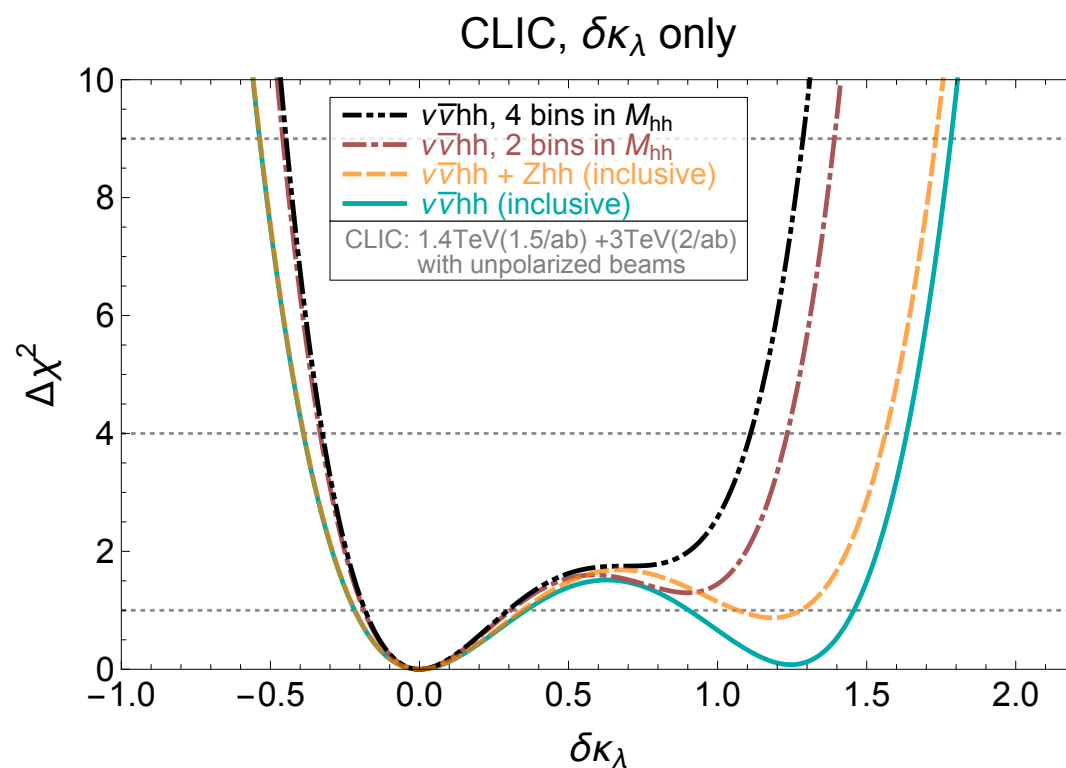
$e^+e^- \rightarrow \nu\bar{\nu}hh$



CLIC 1.4 TeV, $e^+e^- \rightarrow \nu\bar{\nu}hh$



Exclusive measurement for high-energy lepton colliders

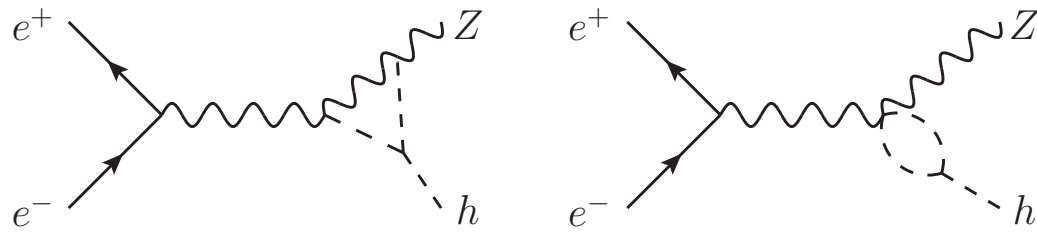


	68 %CL	95%CL
ILC 500 GeV	$[-0.31, 0.28]$	$[-0.67, 0.54]$
ILC 1 TeV	$[-0.25, 1.33]$	$[-0.44, 1.52]$
ILC combined	$[-0.20, 0.23]$	$[-0.37, 0.49]$
CLIC 1.4 TeV	$[-0.35, 1.51]$	$[-0.60, 1.76]$
CLIC 3 TeV	$[-0.26, 0.50] \cup [0.81, 1.56]$	$[-0.46, 1.76]$
CLIC combined	$[-0.22, 0.36] \cup [0.90, 1.46]$	$[-0.39, 1.63]$
+ Zhh	$[-0.22, 0.34] \cup [1.07, 1.28]$	$[-0.39, 1.56]$
2 bins in $\nu\bar{\nu}hh$	$[-0.19, 0.31]$	$[-0.33, 1.23]$
4 bins in $\nu\bar{\nu}hh$	$[-0.18, 0.30]$	$[-0.33, 1.11]$

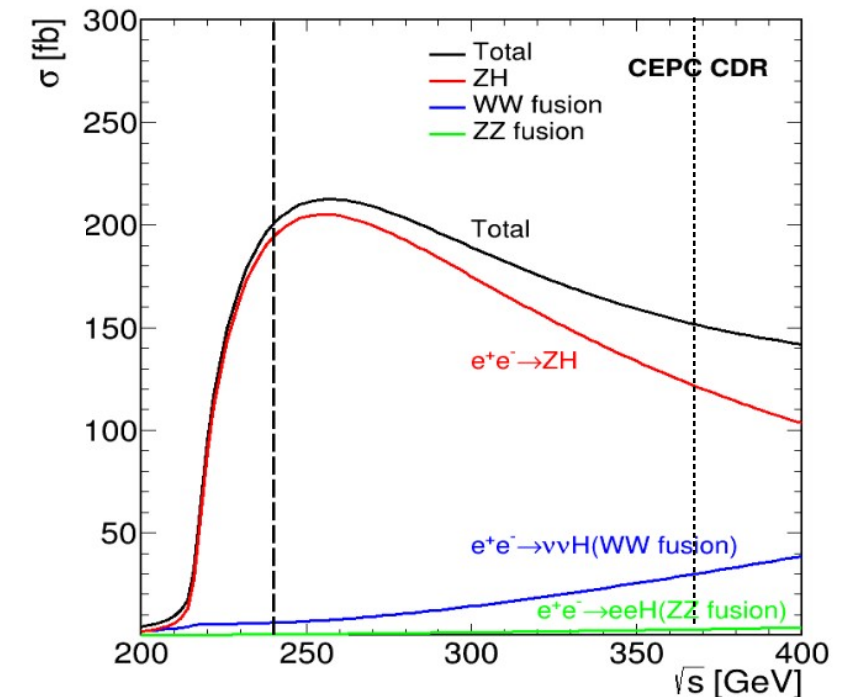
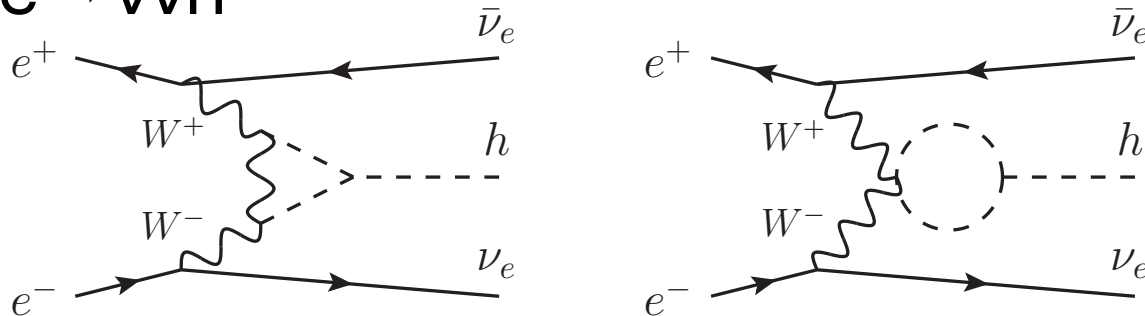
- ◆ Secondary solution @ $\delta\kappa_\lambda \sim 1$ for the $\nu\bar{\nu}HH$ process
- ◆ m_{HH} differential analysis can help for the exclusion of the secondary solution
- ◆ Zhh is useful to enhance the precision

Indirect measurement from single Higgs processes

◆ $ee \rightarrow hZ$



◆ $ee \rightarrow \nu\nu h$



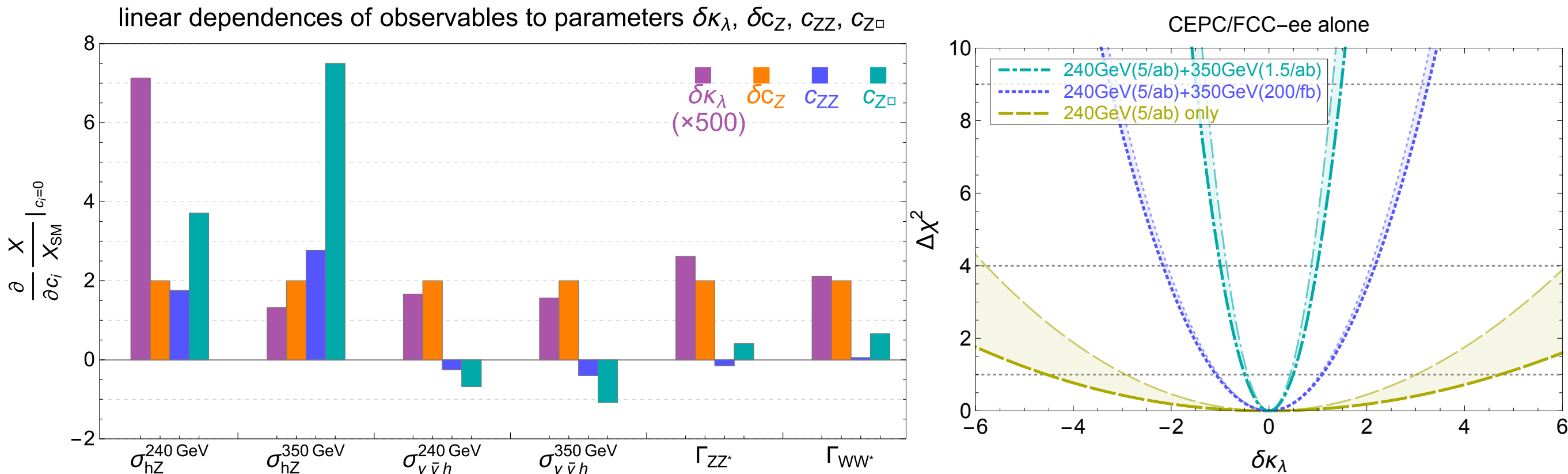
◆ Processes for the global fit :

- ◆ Higgsstrahlung production: $ee \rightarrow hZ$
- ◆ WW-fusion production: $ee \rightarrow \nu\nu h$
- ◆ Weak boson pair production: $ee \rightarrow WW$

◆ Parameter list with new physics parametrization through dimension-6 operators with EFT framework and simplicity assumption (CP-conserving, theory uncertainty etc.)

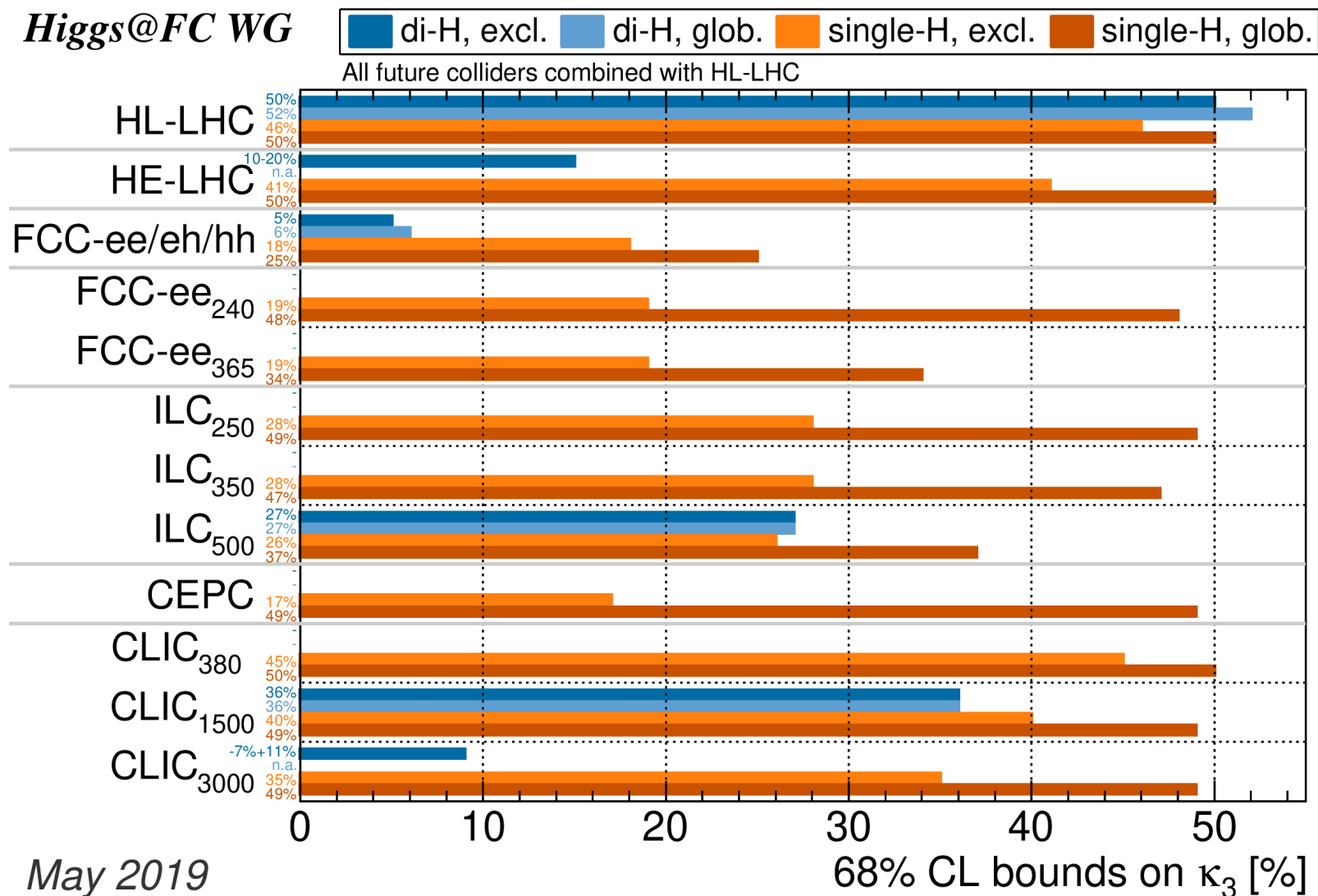
- ◆ Higgs couplings to the gauge bosons: $\delta c_Z, c_{ZZ}, c_{Z\Box}, c_{\gamma\gamma}, c_{Z\gamma}, c_{gg}$
- ◆ Yukawa couplings: $\delta y_t, \delta y_c, \delta y_b, \delta y_\tau, \delta y_\mu$
- ◆ Trilinear gauge couplings: λ_Z
- ◆ Trilinear Higgs self-coupling: $\delta\kappa_\lambda$

Indirect measurement from single Higgs processes



- ◆ Based on very **good precision on cross section** eg CEPC / FCC-ee:
 - ◆ $\sigma(ZH) : \sim 0.5\%$, $\sigma(vvH) : 2\text{-}3\%$
 - ◆ The potential of constraining κ_λ with a precision better than $O(1)$

Comparison



- ◆ Constraint set by the HH production has a small impact from global analysis
- ◆ Single Higgs analysis can complement the results from HH analysis and global analysis is important to get robust results
- ◆ FCC-ee / CEPC can reach a sensitivity of ~20%, CLIC3000 / FCC-hh can reach a sensitivity of ~10%/5%.

Summary

- ◆ Prospective measurement of the tri-linear coupling at Future Colliders through the HH and single-Higgs production
- ◆ HL-LHC: 4σ evidence of the HH process with ATLAS and CMS combination. More room for the further improvement by exploring the kinematic dependence on κ_λ
- ◆ Sensitivity from Future colliders and combination with HL-LHC: 40% for CEPC/FCC-ee, further improvement to $\sim 20\%$ with the increasing of the collider energy, 2-5% for FCC-hh.

