# Dynamic Aperture of CEPC

Y. Zhang, D. Wang, Y. Wang, H. Geng

IAS Program on High Energy Physics (22-25 Jan, 2018), Hongkong Many thanks: K. Oide(KEK), Y. Cai(SLAC)

### Outline

- Introduction
- Dynamic Aperture
  - $\beta_y^*$  (2mm, 1.5mm, 1mm)
  - More knobs
  - Combined Function Dipole(+Sextupole)
  - Beam-Beam Effect
- Summary

### MODE:

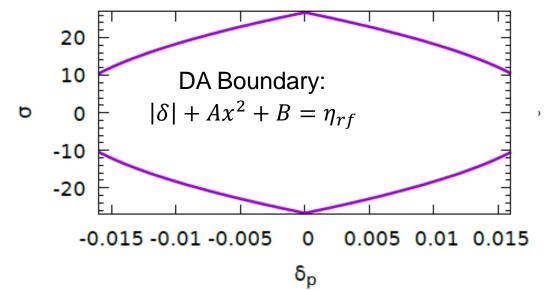
### Multi-Objective optimization by Differential Evolution

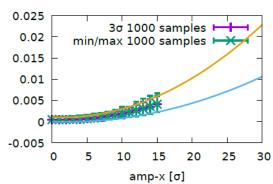
The parallel algorithm is referencing to J. Qiang(IPAC'13)

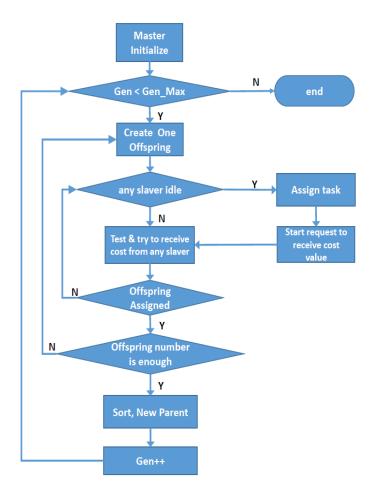
#### High Parallel + High Scalability

- Even the time taken by different task is different
- Even some node is very busy

The difference between the DA boundary and real DA is defined as the objective cost value







## DownhillSimplex in SAD

Try to optimize the total DA

$$F = -\sum_{j=1}^{6} \left( \sum_{i} w(i) * DA_{j}(i) \right) \qquad w(i) = \exp \left[ 2* \left( \frac{|i*\sigma_{\delta}|}{m*\sigma_{\delta}} \right) \right] \qquad (i = -m, ..0, ..m.)$$

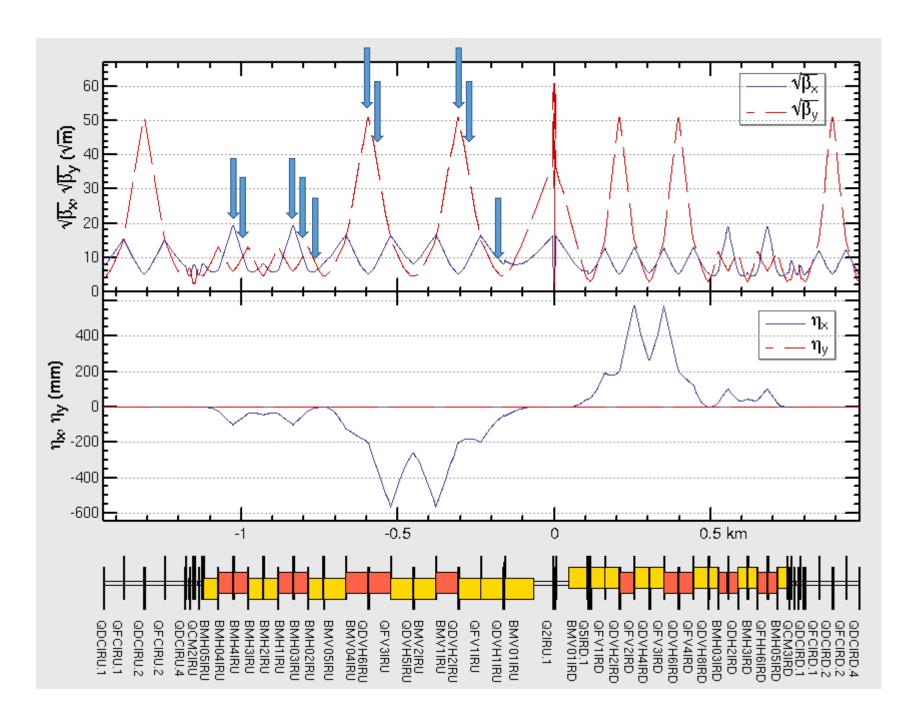
- --  $DA_j(i)$ : DA for  $i^*\sigma_\delta$  energy deviation with the j<sup>th</sup> initial phase (totally 6 phases)
- -- w(i): DA weight for  $i^*\sigma_{\delta}$  energy deviation
  - 1. Scan the strength of sextupoles;
  - 2. DA tracking for the energy list
  - 3. Calculate the objective function (DA)
  - 4. Find the minimum of the objective function by the downhill simplex method
  - 5. Go to 1.
  - 6. Optimization stop when

(fmax-fmin)/(abs(fmax)+abs(fmin)) < Tolerance

## **CEPC DA Optimization Knobs**

### 50(234) knobs in total

- IR sextupoles: (10)
- Arc Sextupole (32) (or 56\*4)
- Phase advance (8)

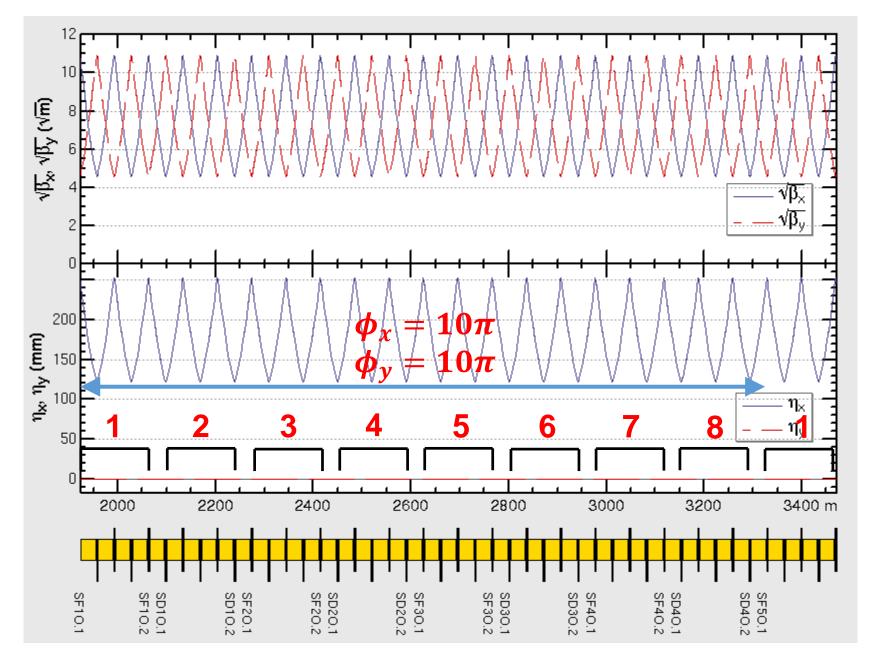


### IR knobs

- Main Chromaticity Sextupoles (2)
- Neighbor weaker sextupole to correct finite length effect (2)
- A. Bogomyagkov, ArXiv:0909.4872
- Sextupole to correct higher order chromaticity in vertical direction (1)
- Y. Cai, PRAB.19.111006

Different strength between Upstream and Downstream of IP.

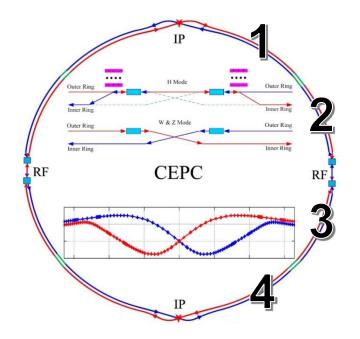
10 knobs in IR.



# Arc sextupole

- 90/90 FODO
- Non-interleave sextupole scheme
- 4 SF + 4 SD sextupole configurations in one arc section
- 7 sub-period in in one arc section,
- 4 arc section in half ring

Total knobs: 32

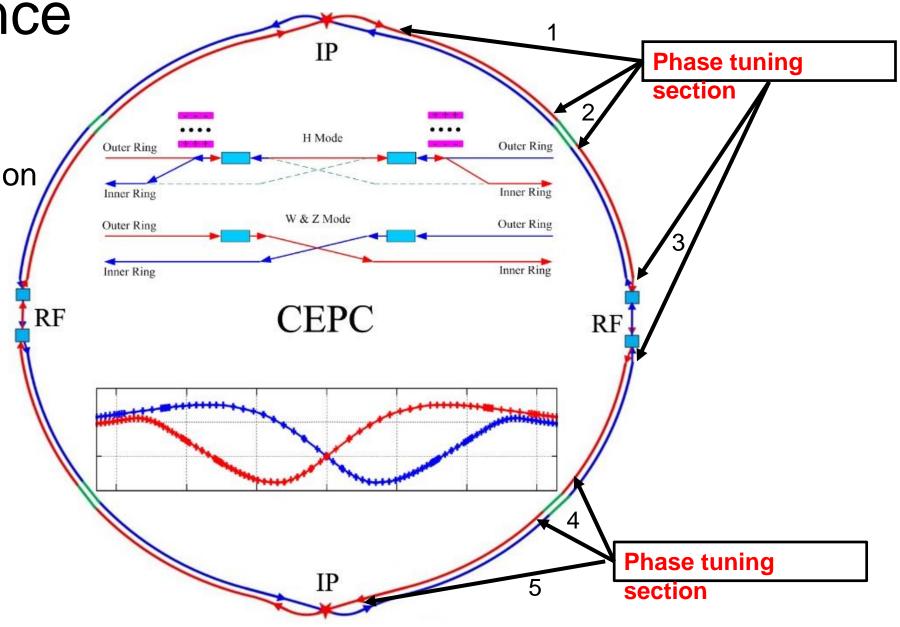


Phase Advance Tuning

10 knobs in x/y direction

Keep tune fixed

• Only 8 free knobs

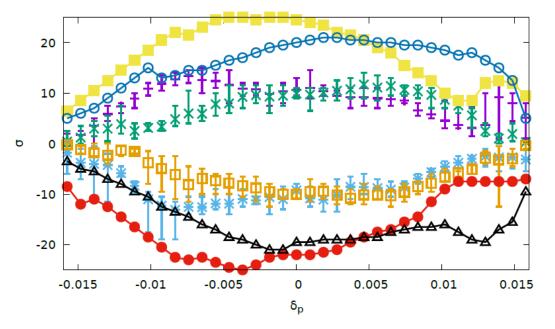


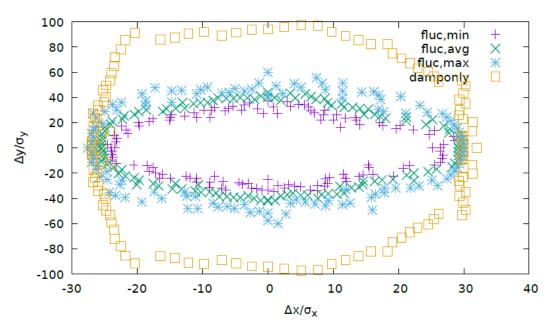
## Model used in DA tracking

#### SAD:

Synchrotron motion, synchrotron radiation in dipoles, quads and sextupoles, tapering, Maxwellian fringes, kinematical terms, crab waist are included.

#### DAMPONLY vs SR Fluctuation





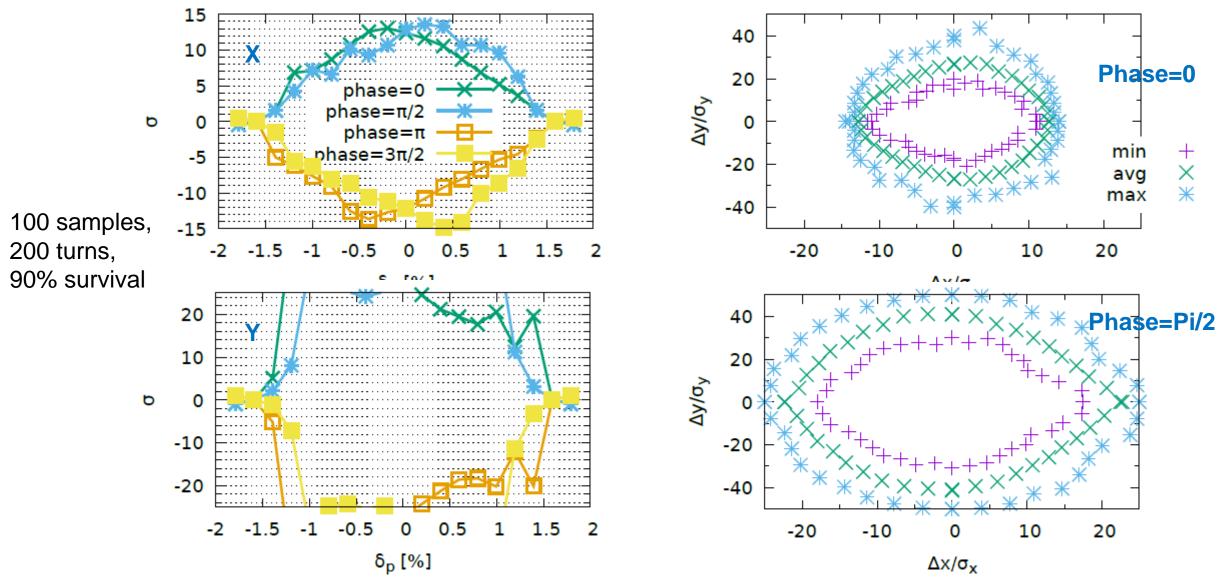
## Suppress noise of DA with SR fluctuation

Χ

- DA is tracked with different initial phase:  $\left(0, \frac{\pi}{2}, \pi, \frac{3\pi}{2}\right)$  for different energy
- 10 more times survey for on-momentum particle is tracked, and the minimum value is treated as the onmomentum DA
- Tracked DA result will be clipped to ensure DA at large momentum deviation will be less than that at small deviation
- Only two objective: min-DA of  $(0,\pi)$  and min-DA of  $\left(\frac{\pi}{2},\frac{3\pi}{2}\right)$

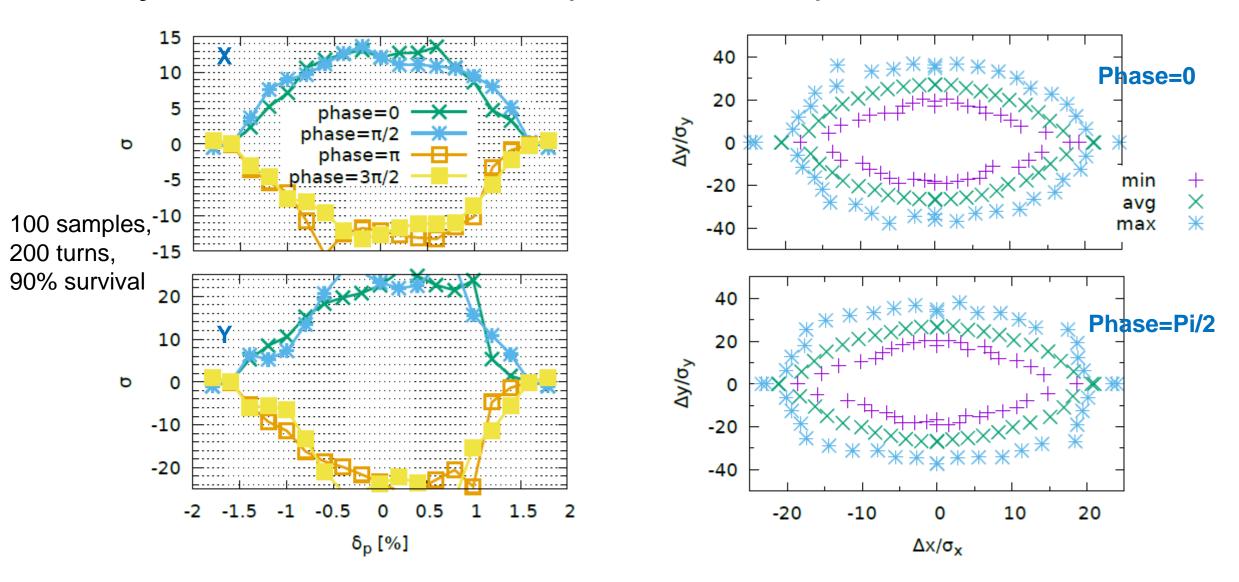
#### Optimized at IP. DA at INJ shown.

## By=2mm, DownhillSimplex (234 knobs)



## By=2mm, MODE (50 knobs)

Optimized at INJ.

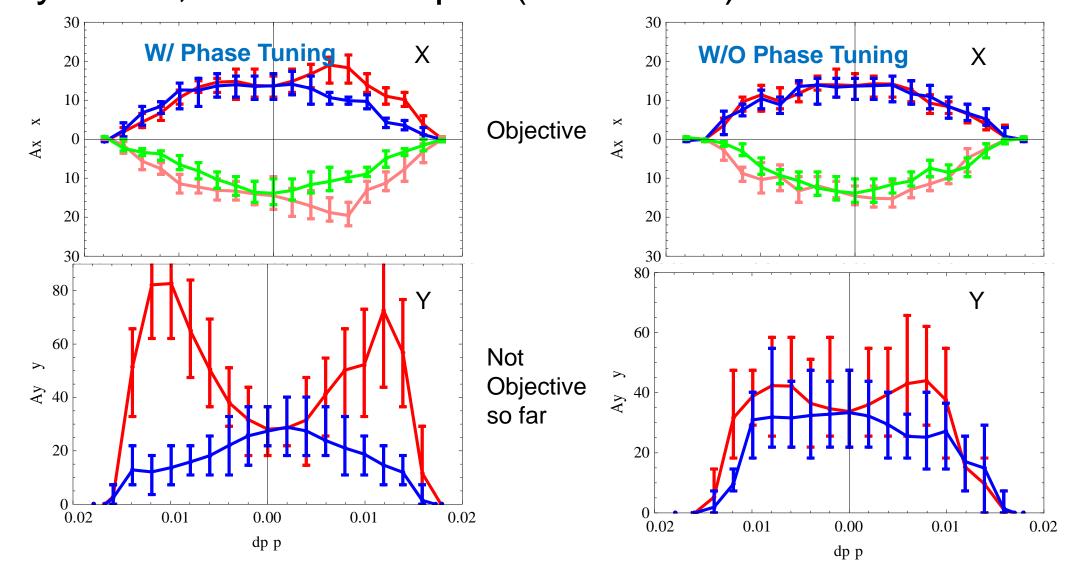


Optimized at IP. DA at INJ shown. Older version lattice, By=2mm, MODE (50 knobs) **INJ** 40 40 20 20 Phase=0 -20 -20 min -40 -40 avg max 40 40 Phase= $\pi/2$ 20 20 -20 -20 -40 -40 10 20 -20 -10 10 20 -10

 $\Delta x/\sigma_x$ 

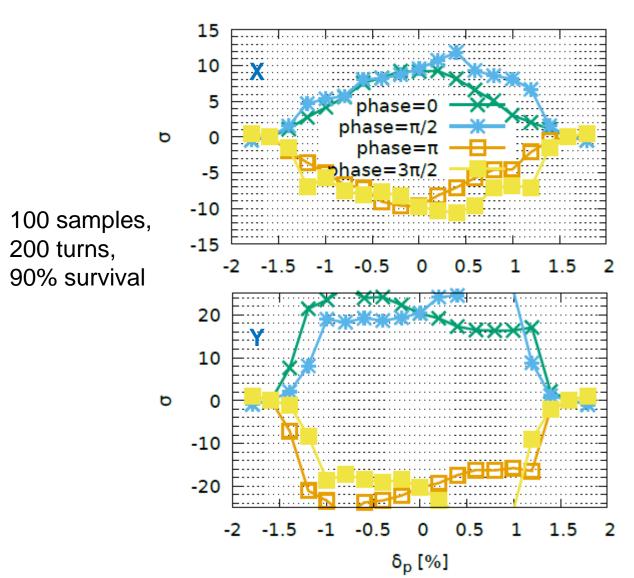
 $\Delta x/\sigma_x$ 

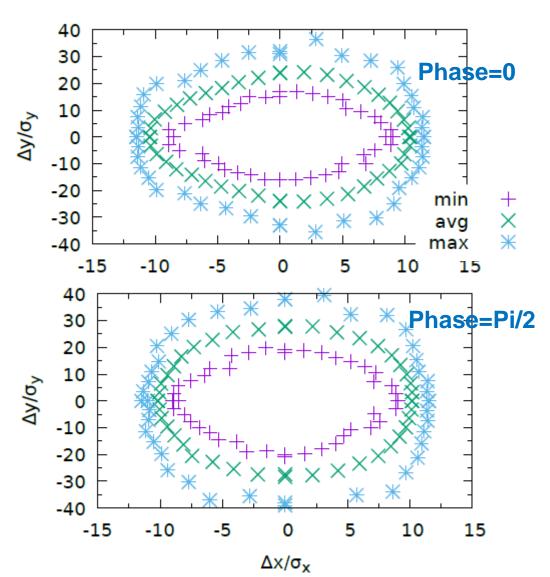
# Arc Phase Tuning by=2mm, DownhillSimplex(234 knobs)



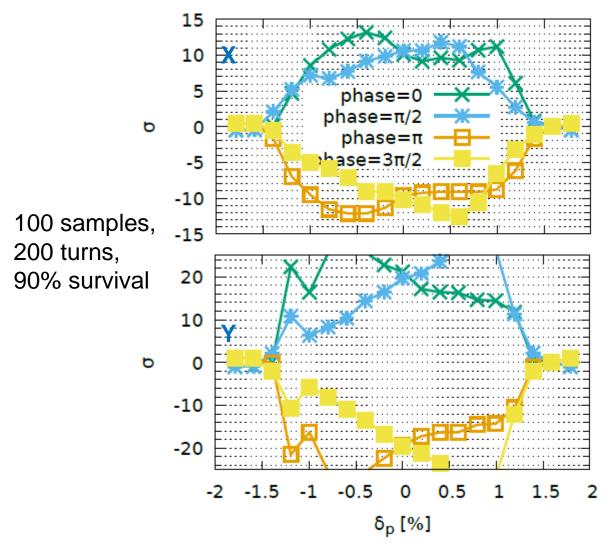
#### Optimized at IP. DA at INJ shown.

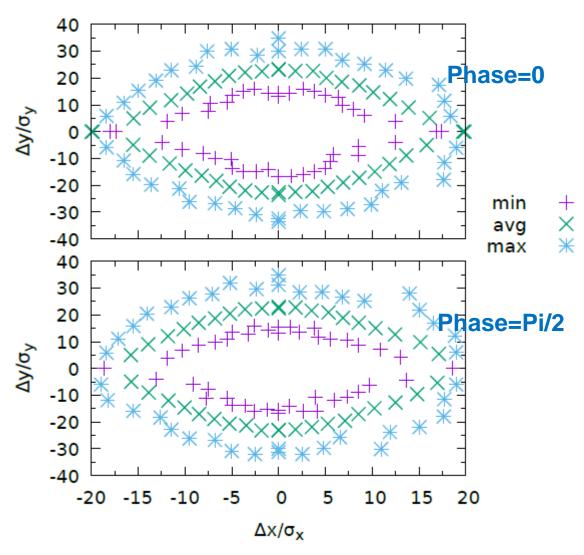
# By=1.5mm, DownhillSimplex (234 knobs)





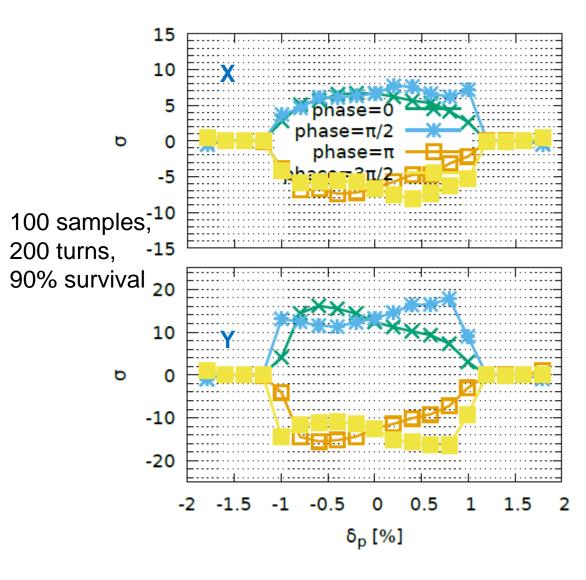
## By=1.5mm, MODE (50 knobs) Optimized at INJ.

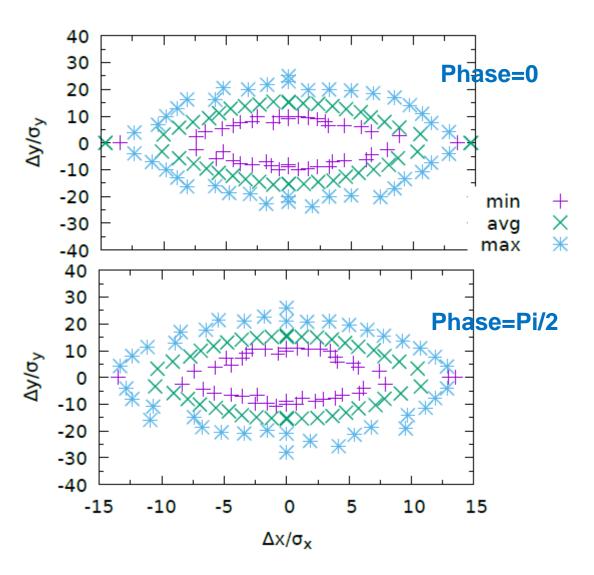




#### Optimized at IP. DA at INJ shown.

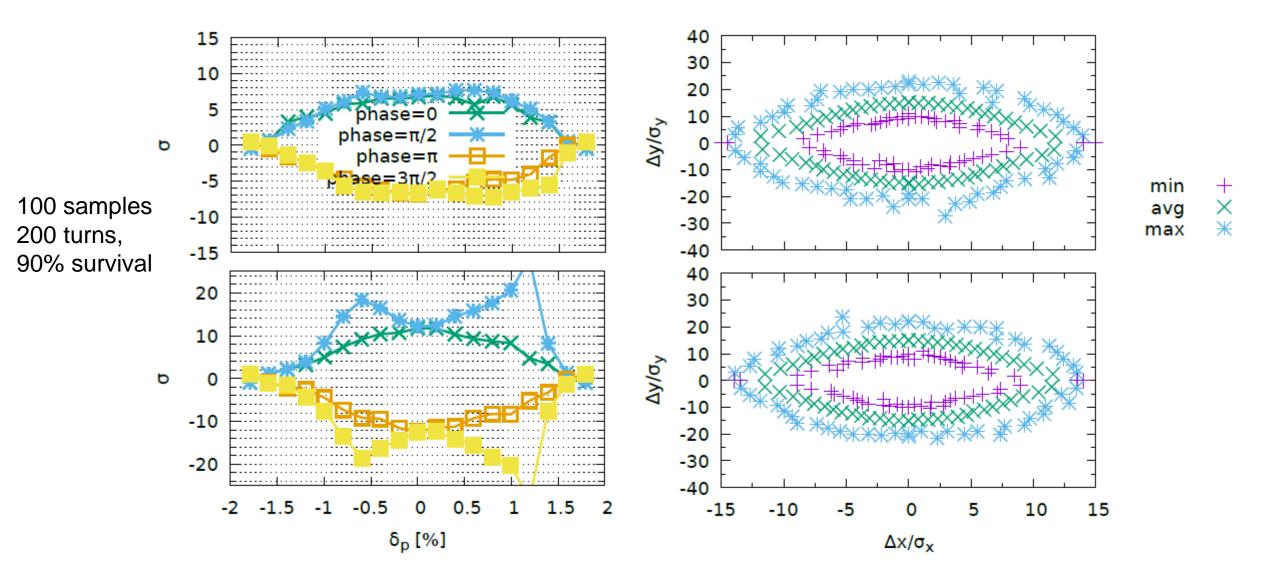
## By=1mm, DownhillSimplex (234 knobs)





## By=1mm, MODE (50 knobs)

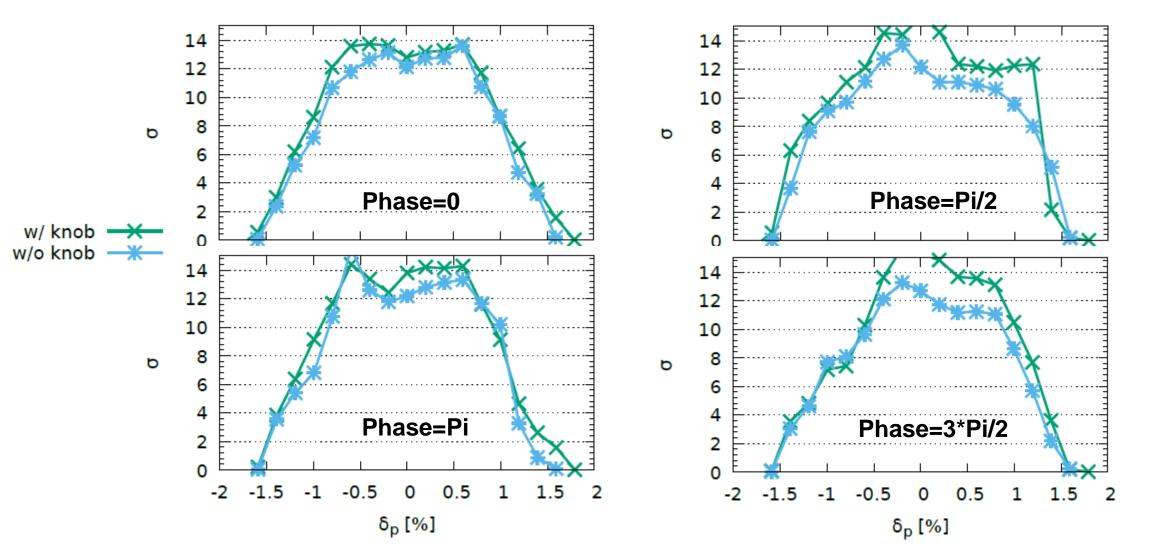
Optimized at INJ.



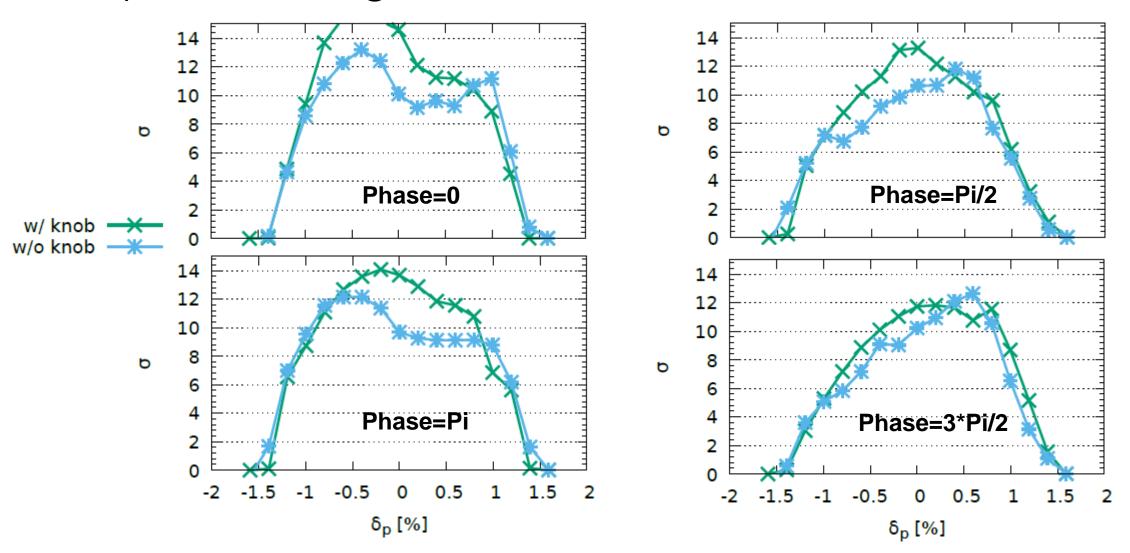
## More knobs (20)

- The octupole magnets in the immediate vicinity of the FF quadrupoles (QD0 and QF0) (4) slac-pub-12716
- Octupoles are added to ccs sextupoles for the optimization
  (4)
  K. Oide
- Non-interleave sextupole pair in RF region(2)
- Octupole to correct higher order chromaticity in vertical direction (2)
- More sextupole in dispersive region(8)

# 20 more knobs: by=2mm (1-2 sigma enlargement at small momentum deviation)



# 20 more knobs: by=1.5mm (1-2 $\sigma$ enlargement at small momentum deviation)



## Combined D+S scheme

The power consumption of the arc sextupoles are too high.

Sextupole: 16.7 MW (copper coils)

Dipole: 6.5 MW (Al coils)

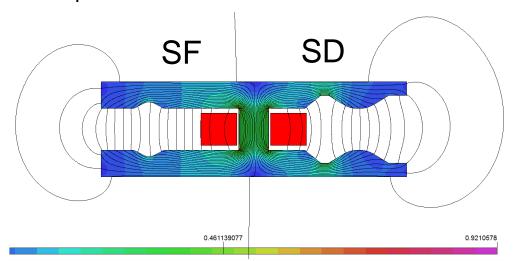
Reducing the strength of the stand-alone sextupoles can help.

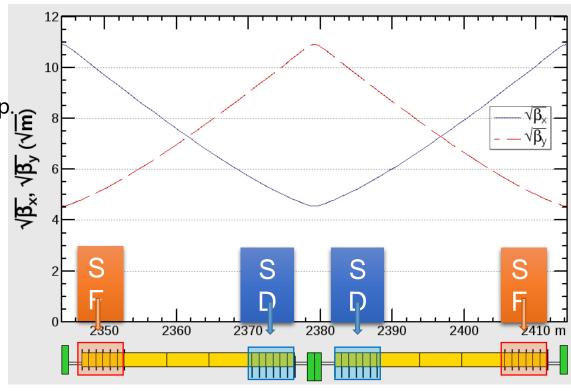
Combined function magnet: dipole + sextupole

Combined sextupoles: half of linear chromaticity

Stand-alone sextupoles: Chromaticity and DA

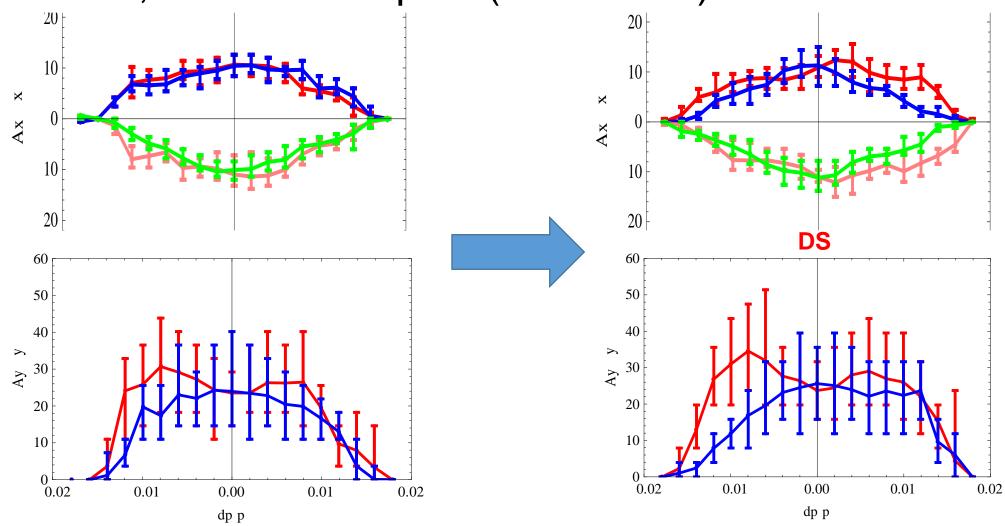
No additional power sources for combined SF and SD





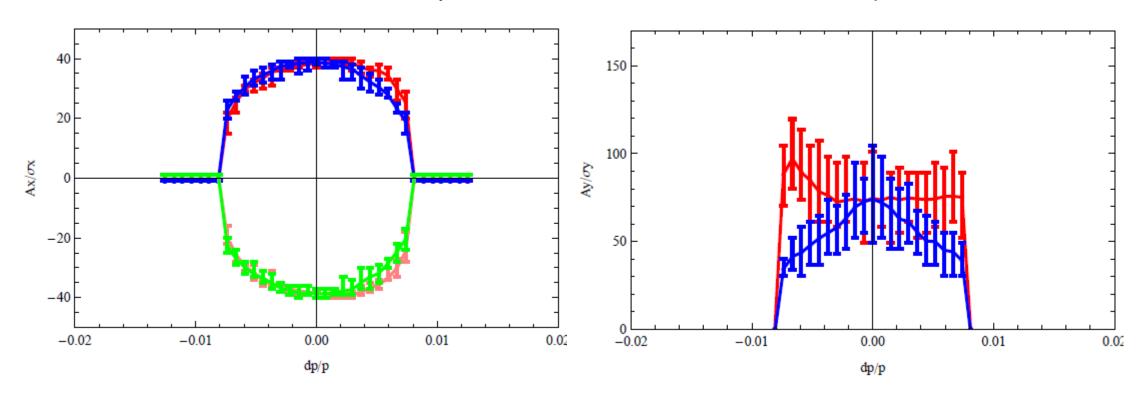
## DA of DS Scheme

By=1.5mm, DownhillSimplex (234 knobs)

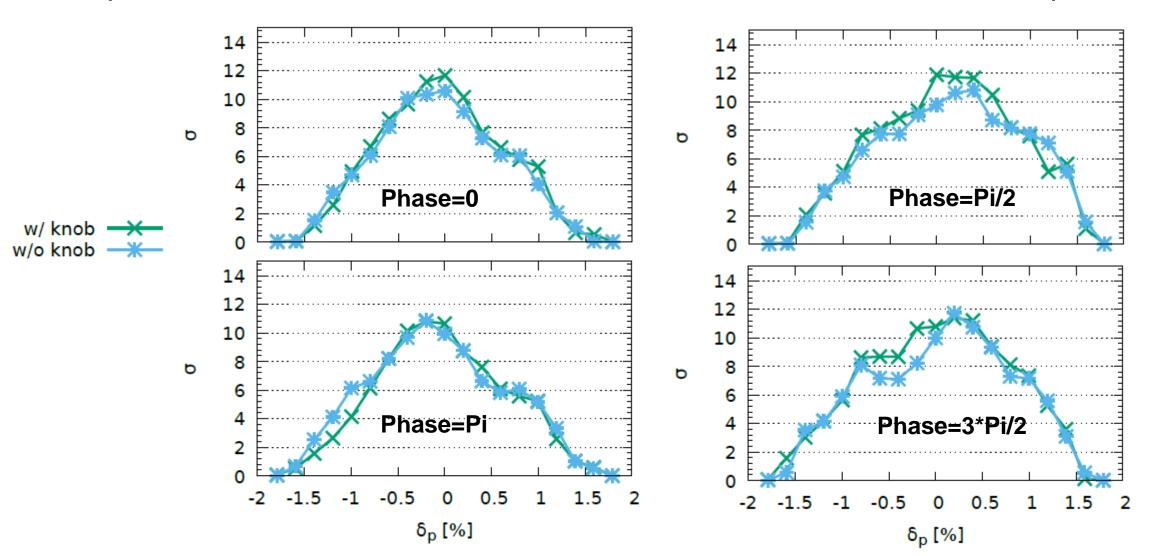


### DA at Z with combined DS

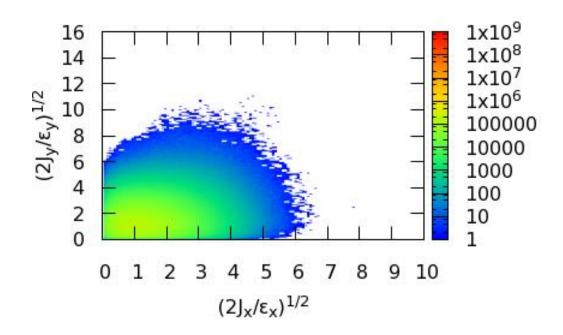
We do not need to worry about the break of non-interleave sextupole scheme

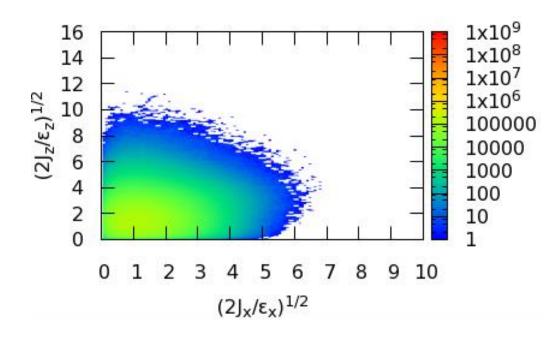


# 20 more knobs: by=1.5mm DS Scheme (no so clear contribution from 20 more knobs)

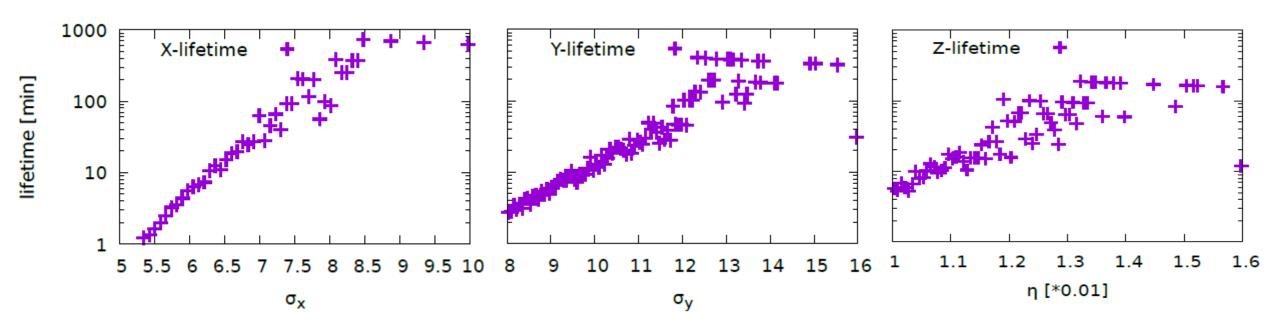


## Beam Distribution: by=1.5mm Lattice + Beamstrahlung + SR Fluctuation





## Beam Lifetime: by=1.5mm Lattice + Beamstrahlung + SR Fluctuation



Achieved DA:  $\sim 15\sigma_x$ ,  $\sim 15\sigma_y$ ,  $\sim 0.015$ 

100min, DA requirement:  $7.5\sigma_x$ , 12.5 $\sigma_y$ , 0.0135

## Summary & Discussion

- By\*=1.5mm, The DA requirement (lifetime/injection) is met without error, nearly no margin so far.
- We only focus on the delta-x aperture in optimization, but the vertical phase is also tuned, which may breaks the symmetry in delta-y space.
- We only focus on the DA at one point in the ring. Free all the sextupoles(56\*4) in arc may bring worse symmetry.
- 20 more knobs could help enlarge the transverse DA
- Combined function Dipole(+S) may enlarge the momentum acceptance. But the conclusion is not finalized, since cutting long dipole into 5 pieces may help.