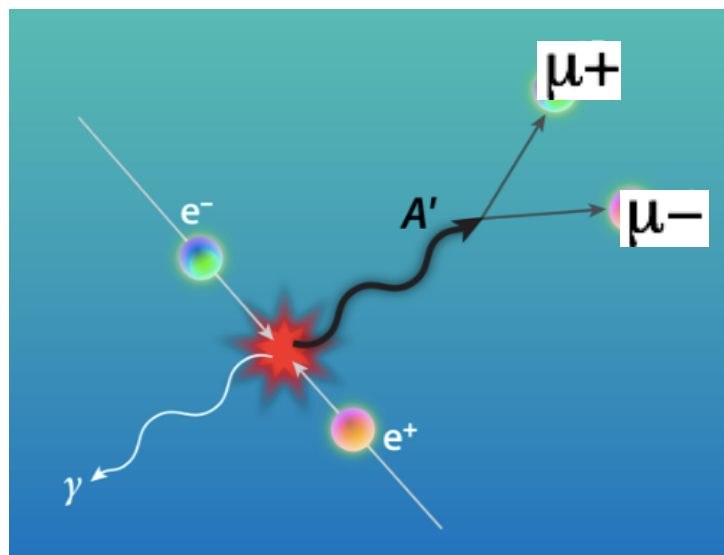


Dark Photon at the C\mathcal{E}PC

Xiao-Gang He, SJTU/NTU
Collaborators: Min He and Cheng-Kai Huang
IAS, Hong Kong

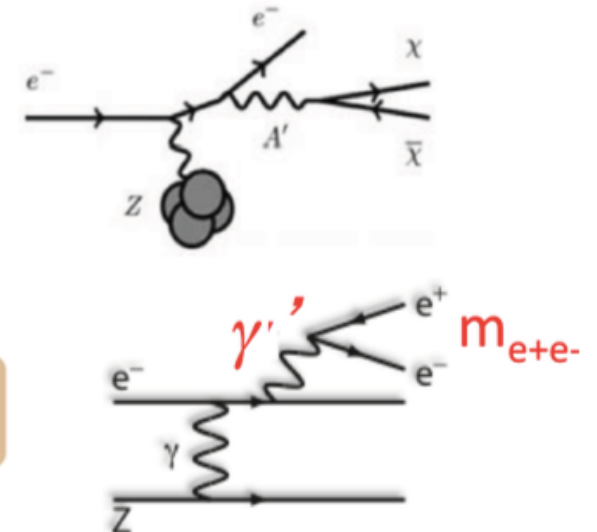
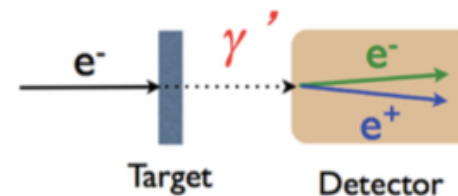
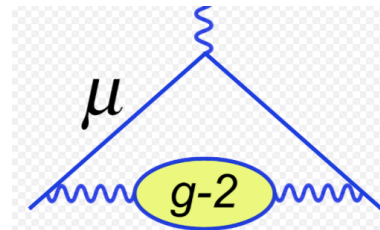
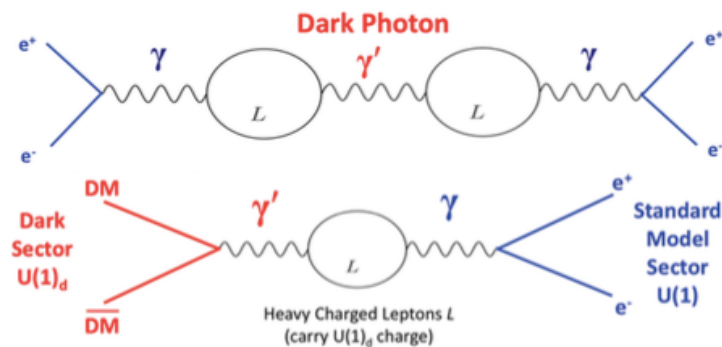


The Dark Photon

A vector boson X_μ couples to SM matter electromagnetic current J^μ_{em} as

$$\varepsilon e Q_{\text{em}} j^\mu_{\text{em}} X_\mu$$

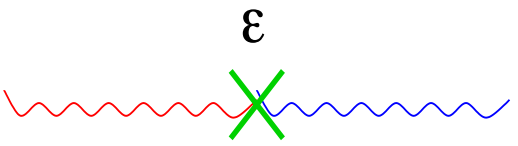
$$\varepsilon \ll 1$$



Generating Dark Photon Interaction through Gauge Boson Kinetic Mixing

$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} - \frac{1}{4} X_{\mu\nu} X^{\mu\nu}$$

will use X or A' for dark photon

$$\epsilon X_{\mu\nu} F^{\mu\nu}$$


$$X_{\mu\nu} = \partial_\mu X_\nu - \partial_\nu X_\mu \quad F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu$$

X and A are gauge fields of $U(1)_X \times U(1)_A$

This term is renormalizable and gauge invariant

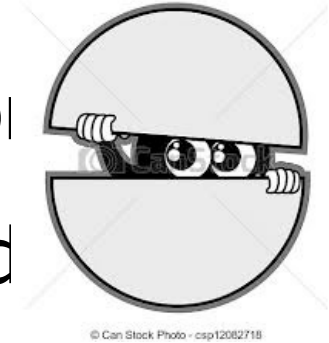
ϵ is a unknown number in a given model.

There are many interesting consequences

Consider $U(1)_A = U(1)_Y$ and

$U(1)_X$ a new gauge group: dark photon or

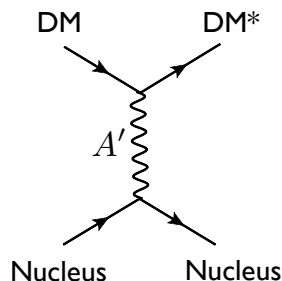
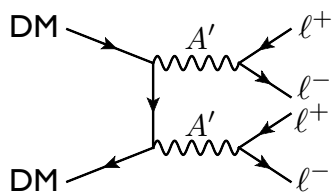
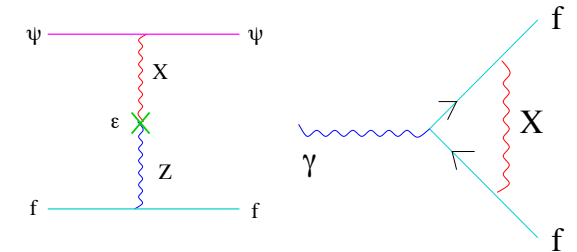
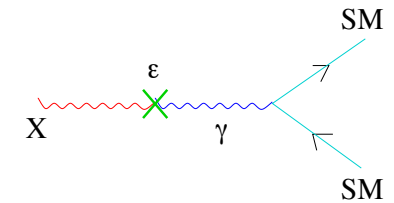
Dark photon connected to a hidden world
(dark sector...)



- $SU(2)_L \times U(1)_Y \times U(1)_X$ gauge invariance:

$$\mathcal{L} \supset -\frac{1}{4}(X_{\mu\nu})^2 - \frac{1}{4}(B_{\mu\nu})^2 - \frac{1}{4}(W_{\mu\nu}^a)^2 - \frac{\epsilon}{2c_W} B_{\mu\nu} X^{\mu\nu}$$

$$\rightarrow (\dots) - \frac{\epsilon}{2} X_{\mu\nu} (F^{\mu\nu} - t_W Z^{\mu\nu}) \quad -\mathcal{L} \supset e j_{em}^\mu A_\mu$$

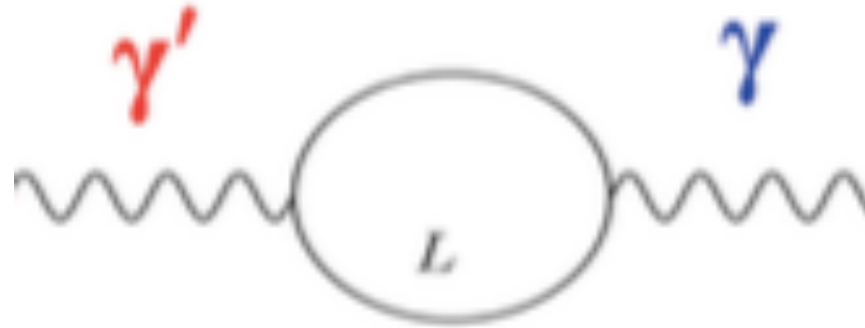


$$+ \left[g_x j_x^\mu - \epsilon e j_{em}^\mu - \epsilon t_W \left(\frac{\eta}{1-\eta} \right) g_Z j_Z^\mu \right] X_\mu$$

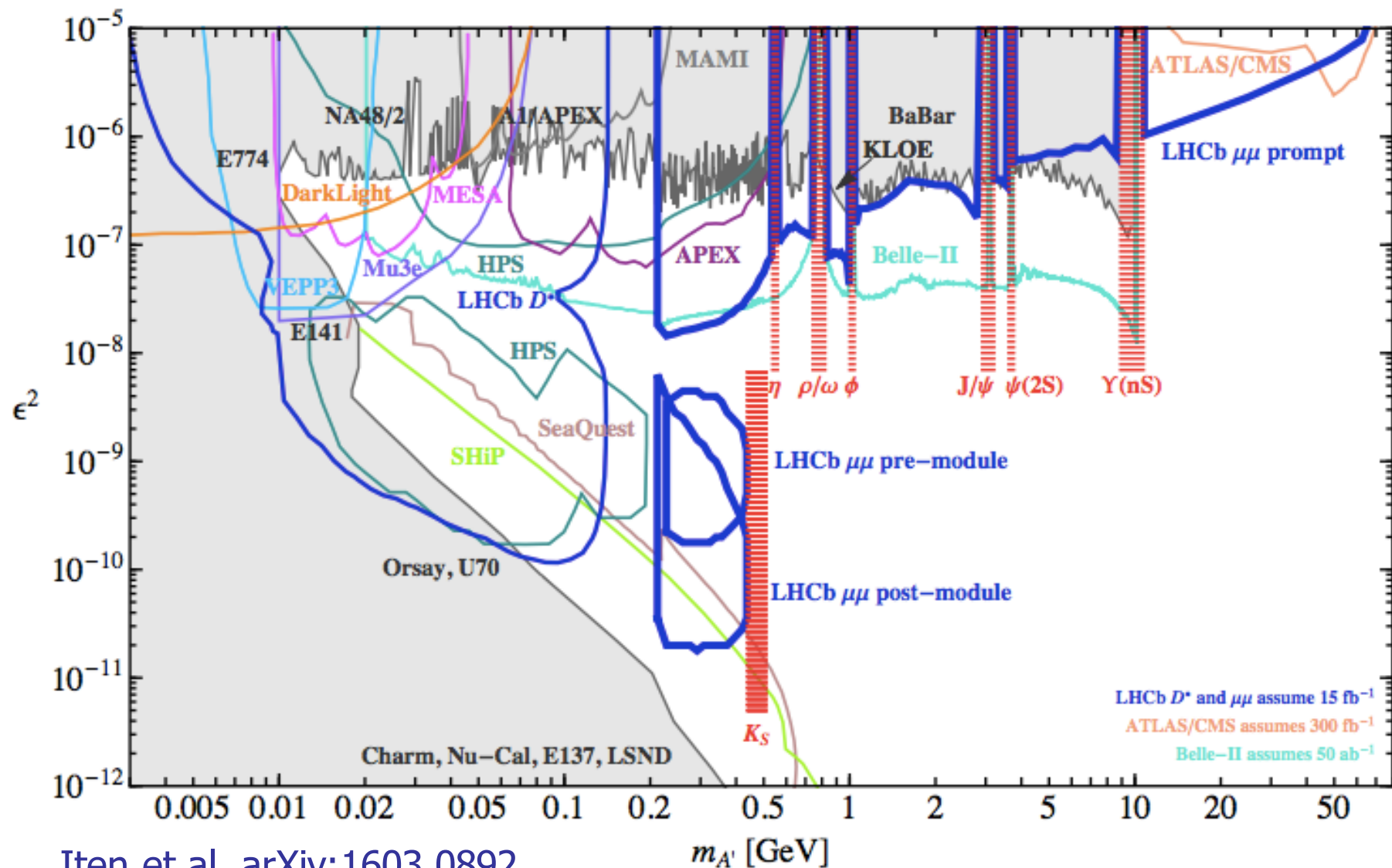
$$+ \left[g_Z j_Z^\mu + \epsilon t_W \left(\frac{1}{1-\eta} \right) g_x j_x^\mu \right] Z_\mu$$

$$\mathcal{M}^2 = m_Z^2 \begin{pmatrix} \eta & \epsilon t_W \eta \\ \epsilon t_W \eta & 1 \end{pmatrix} \quad \text{with } \eta = m_x^2 / m_Z^2$$

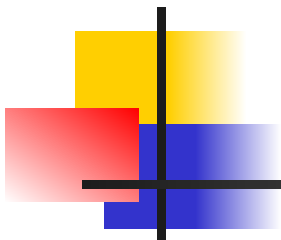
Loop generation of photon and dark photon mixing



Summary of constraints on the dark photon mass and coupling



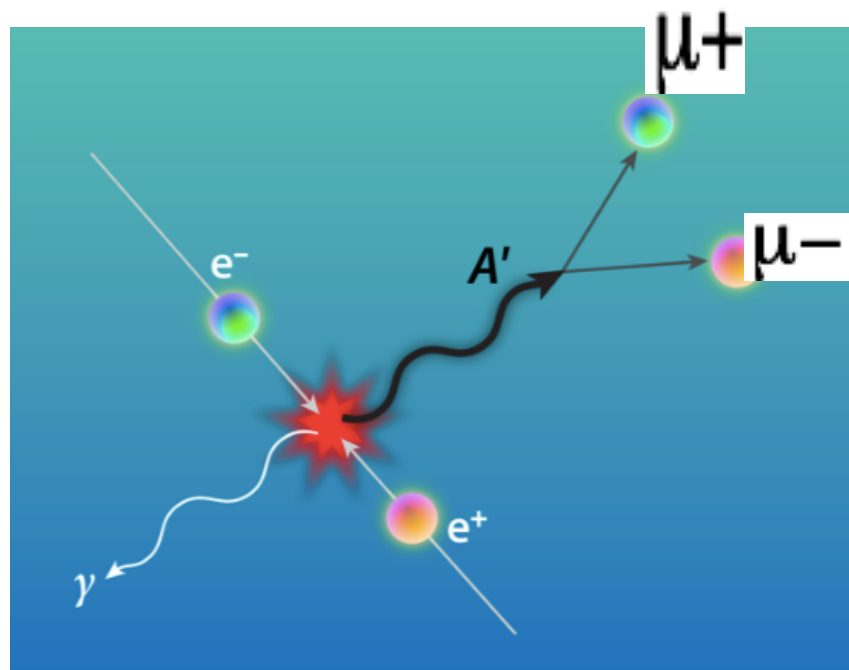
Iten et al, arXiv:1603.0892



What CEPC can do for dark photon?

This talk describe:

study dark photon using $e^+e^- \rightarrow \gamma A' \rightarrow \mu^+\mu^-$



CEPC project (Xinchou Lou)

A reminder about the CEPC-SppC

Phase 1: e^+e^- Higgs (Z) factory two detectors, 1M ZH events in ~10yrs

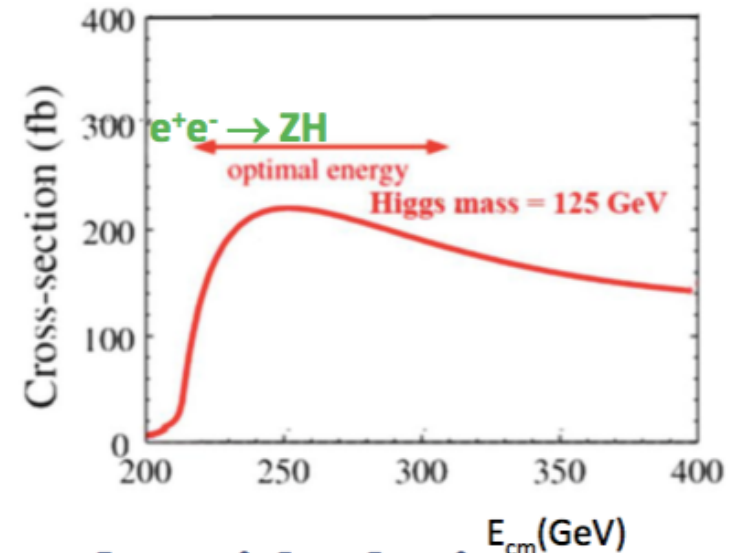
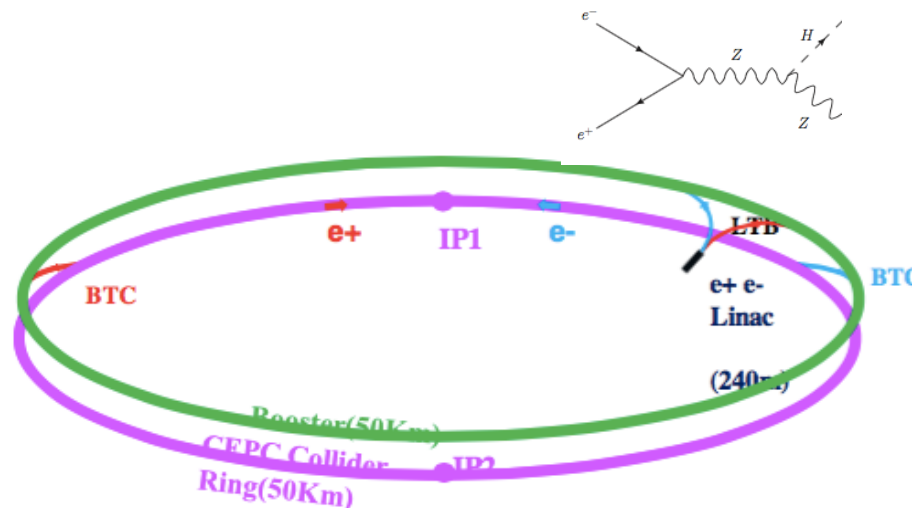
Circular Electron Positron Collider (CEPC)

$E_{\text{cm}} \approx 240 \text{ GeV}$, luminosity $\sim 2 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$, can also run at the Z-pole $\sim 10^{10}$ Z bosons

Precision measurement of the Higgs boson (and the Z boson)

Phase 2: a discovery machine; pp collision with $E_{\text{cm}} \approx 50\text{-}100 \text{ TeV}$; ep, HI options

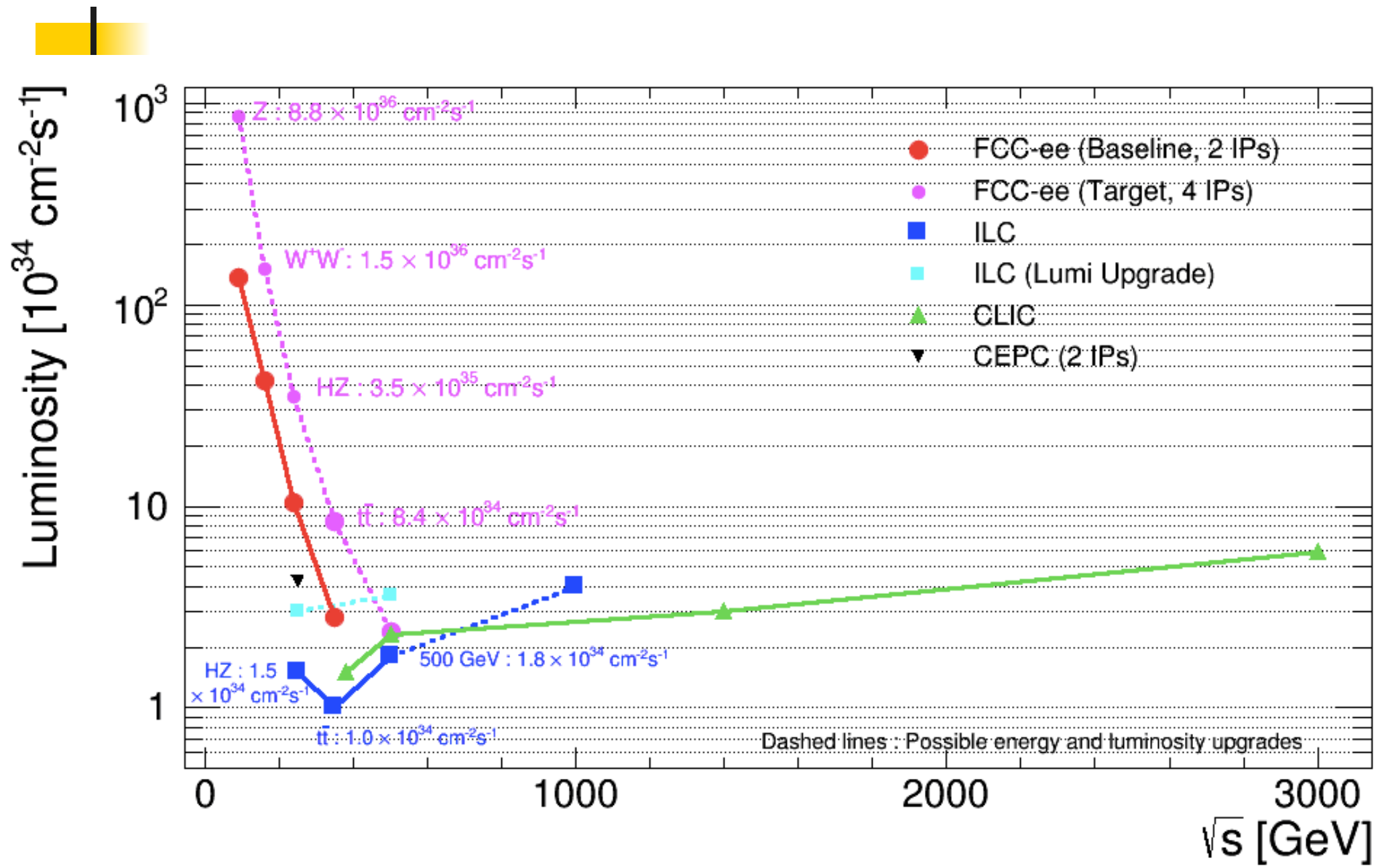
Super proton-proton Collider (SppC)

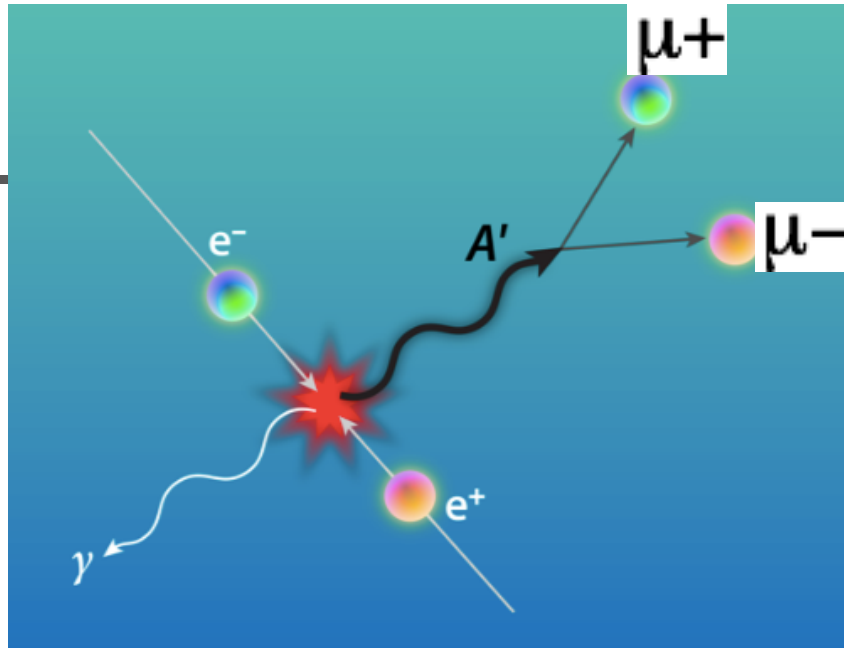


**avored post BEPCII accelerator based particle physics
program in China**

September 2, 2016

3





$$\frac{d\sigma_{e^+e^- \rightarrow \gamma A' \rightarrow \gamma \mu^+ \mu^-}}{d\sigma_{e^+e^- \rightarrow \gamma \gamma^* \rightarrow \gamma \mu^+ \mu^-}} \Big|_{m_{\mu\mu} \sim m_{A'}} \sim \epsilon^4 \frac{m_{\mu\mu}^4}{(m_{\mu\mu}^2 - m_{A'}^2)^2 + \Gamma_{A'}^2 m_{A'}^2}.$$

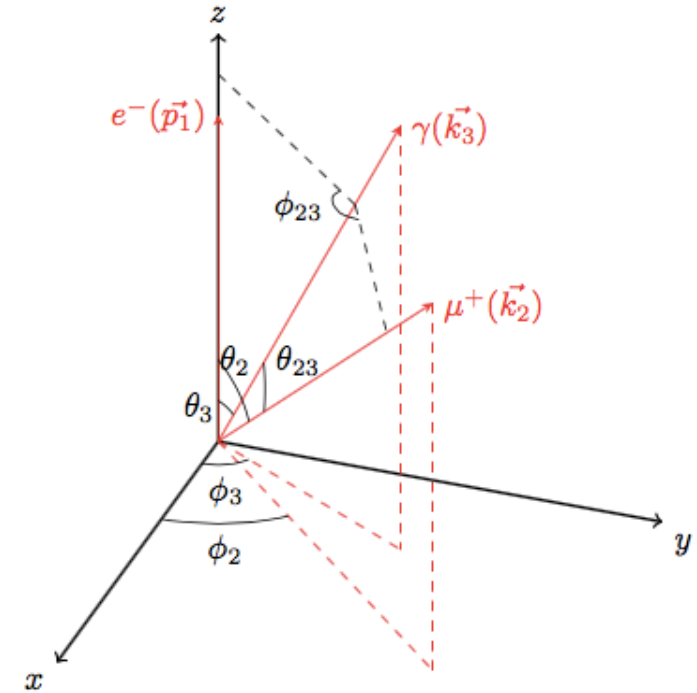
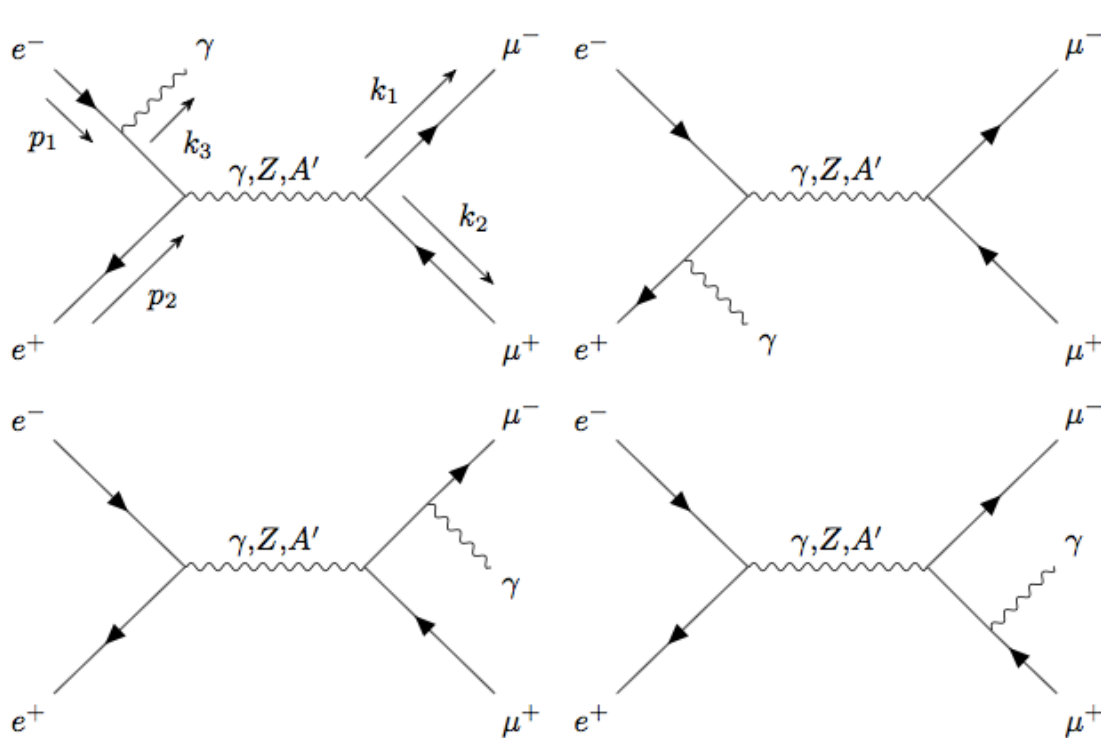
$$\frac{s}{B_{em-background}} \sim \epsilon^4 \frac{\pi}{8} \frac{m_{A'}^2}{\Gamma_{A'} \sigma_{\mu\mu}},$$

Naïve expectation

$$\Gamma_{A' \rightarrow f\bar{f}} = \frac{\epsilon^2}{3} Q_f^2 \alpha_{em} m_{A'} \left(1 + 2 \frac{m_f^2}{m_{A'}^2}\right) \sqrt{1 - \frac{4m_f^2}{m_{A'}^2}}.$$

Integrate dimuon energy range $|m_{\mu\mu} - m_{A'}| < 2\sigma_{\mu\mu}$

Evaluation of the cross section



$$\begin{aligned}
 s &= (p_1 + p_2)^2, \\
 s_1 &= (p_1 + p_2 - k_1)^2 = (k_2 + k_3)^2 = s - 2\sqrt{s}E_1 + m_1^2, \\
 s_2 &= (p_1 + p_2 - k_2)^2 = (k_1 + k_3)^2 = s - 2\sqrt{s}E_2 + m_2^2, \\
 s_3 &= (p_1 + p_2 - k_3)^2 = (k_1 + k_2)^2 = s - 2\sqrt{s}E_3 + m_1^2,
 \end{aligned}$$

$$\begin{aligned}
 \sigma &= \frac{1}{2 \cdot \sqrt{s}/2 \cdot 2 \cdot \sqrt{s}/2 \cdot 2} \int d\Pi_3 |M|^2 \\
 &= \frac{1}{64s^2(2\pi)^4} \int_{s_3^{\min}}^{s_3^{\max}} ds_3 \int_{s_2^{\min}(s_3)}^{s_2^{\max}(s_3)} ds_2 \int_{-1}^1 d\cos\theta_3 \int_0^{2\pi} d\phi_{23} |M|^2
 \end{aligned}$$



$$e^+e^- \rightarrow \gamma \gamma^* \rightarrow \gamma \mu^+ \mu^-$$

Using notation

$$\begin{aligned} s &= (p_1 + p_2)^2, & t &= (p_2 - k_2)^2, & u &= (p_2 - k_1)^2, \\ s' &= (k_1 + k_2)^2, & t' &= (p_1 - k_1)^2, & u' &= (p_1 - k_2)^2. \end{aligned}$$

We set $m_e = m_\mu = 0$, then the squared amplitude for this process is

$$\frac{1}{4} \sum_{spins} |iM_0|^2 = \frac{4e^6(t^2 + t'^2 + u^2 + u'^2)[2ss'(t + t') + 2tt'(s + s') + u(st + s't') + u'(st' + s't)]}{(s' + t + u)(s' + t' + u')(s' + t + u')(s' + t' + u)}.$$

$$e^+e^- \rightarrow \gamma A'^* \rightarrow \gamma \mu^+ \mu^-$$

$$\frac{4\epsilon^4 e^6 [(s' - m_A^2)(s - m_A^2) + \Gamma^2 m_A^2](t^2 + t'^2 + u^2 + u'^2)[ss'(t + t' - u - u') + (tt' - uu')(s + s')]}{[(s' - m_A^2)^2 + \Gamma^2 m_A^2][(s - m_A^2)^2 + \Gamma^2 m_A^2](s' + t + u)(s' + t' + u')(s' + t + u')(s' + t' + u)}$$

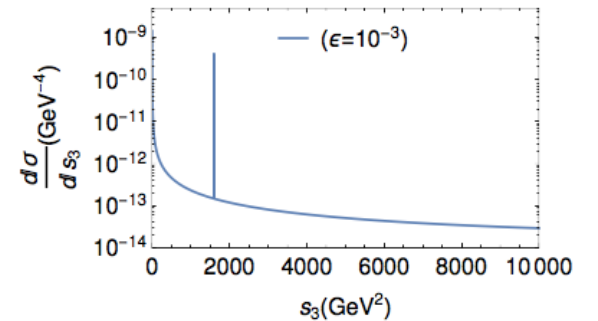
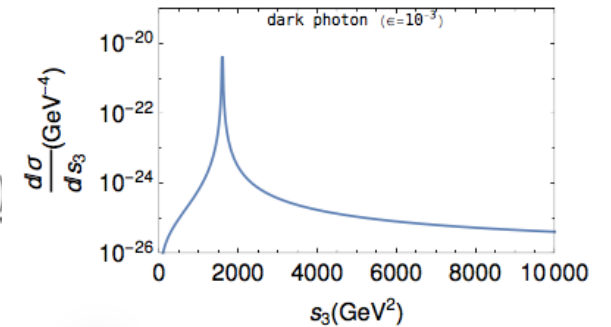
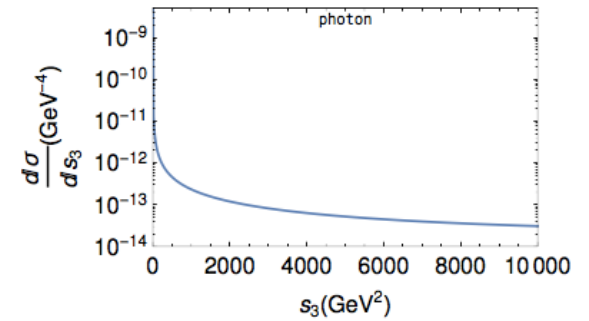
$$\sigma(e^+e^- \rightarrow \gamma \mu^+ \mu^-) = \sigma(e^+e^- \rightarrow \gamma A') \text{Br}(A' \rightarrow \mu^+ \mu^-)$$

$$\frac{d\sigma(e^+e^- \rightarrow \gamma \gamma \rightarrow \gamma \mu^+ \mu^-)}{ds_3},$$

$$\frac{d\sigma(e^+e^- \rightarrow \gamma A \rightarrow \gamma \mu^+ \mu^-)}{ds_3}$$

$$\begin{aligned} \Gamma(A \rightarrow f \bar{f}) &= \frac{g_f^2 m_A}{12\pi} \left(1 + \frac{2m_f^2}{m_A^2}\right) \left(1 - \frac{4m_f^2}{m_A^2}\right)^{\frac{1}{2}}, \\ \Gamma &= \sum_f \Gamma(A \rightarrow f \bar{f}), \end{aligned}$$

$$S_3 = (k_1 + k_2)^2 = m_{\mu\mu}^2 \text{ muon pair invariant mass squared}$$



Observable

$$R = \frac{\sigma_{\gamma A'}^{m_{\mu\mu}}}{\sigma_{\gamma\gamma}^{m_{\mu\mu}}} = \frac{\int_{(m_{A'} - \sigma_{\mu\mu})^2}^{(m_{A'} + \sigma_{\mu\mu})^2} (d\sigma_{\gamma A}/ds_3) ds_3}{\int_{(m_{A'} - \sigma_{\mu\mu})^2}^{(m_{A'} + \sigma_{\mu\mu})^2} (d\sigma_{\gamma\gamma}/ds_3) ds_3}$$

Given σ with sensitivity on R ,
 ε^2 is a function of $m_{A'}$, $\sigma = 0.5\% m_A$

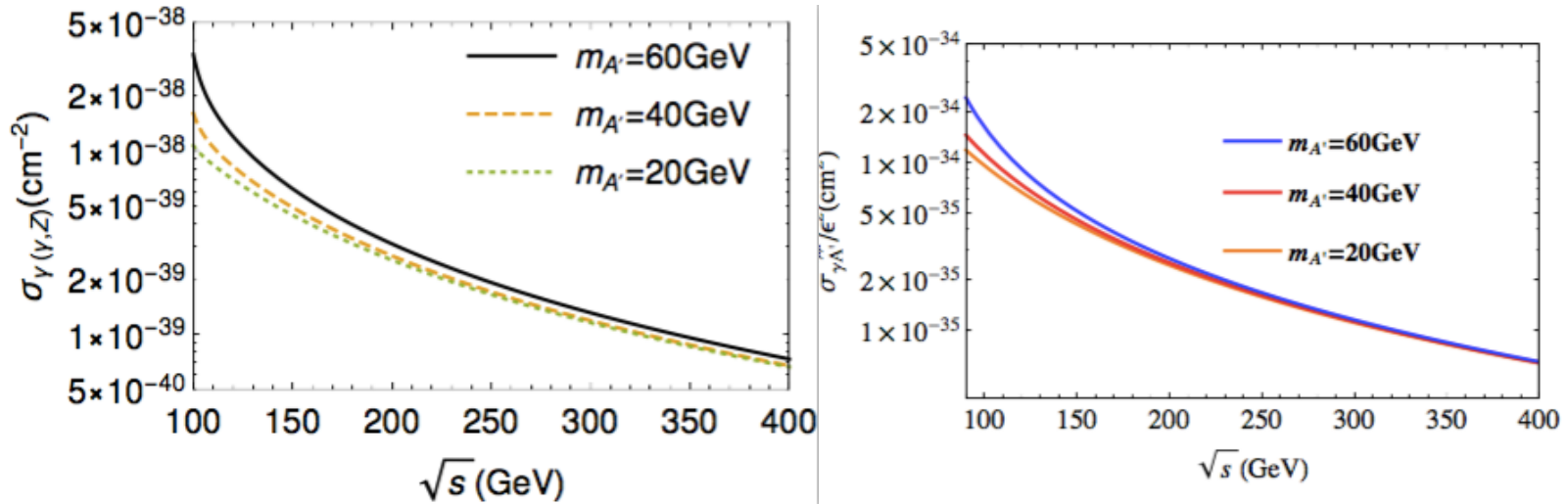


FIG. 2: Cross sections $\sigma_{\gamma\gamma}^{m_{\mu\mu}}$ and $\sigma_{\gamma A'}^{m_{\mu\mu}}$ as functions of \sqrt{s} . $m_{A'} = 20, 40$ and 60 GeV. The $m_{A'}$ dependence of $\sigma_{\gamma\gamma}^{m_{\mu\mu}}$ is due to integration ranges depend on $m_{A'}$.

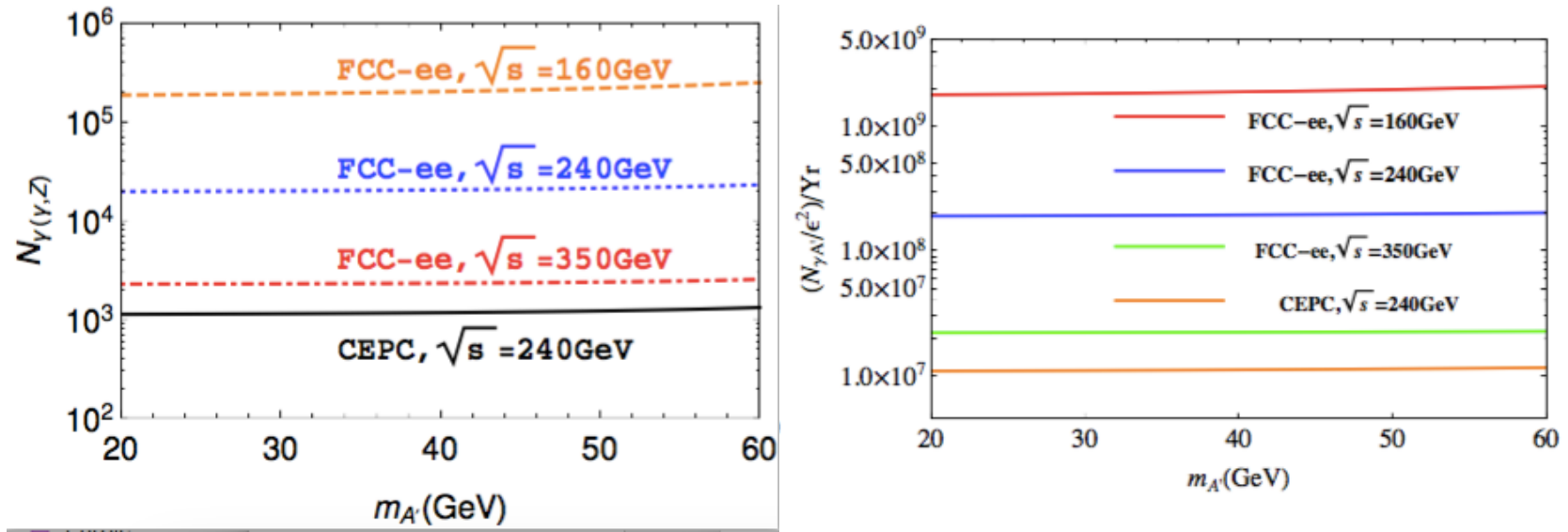
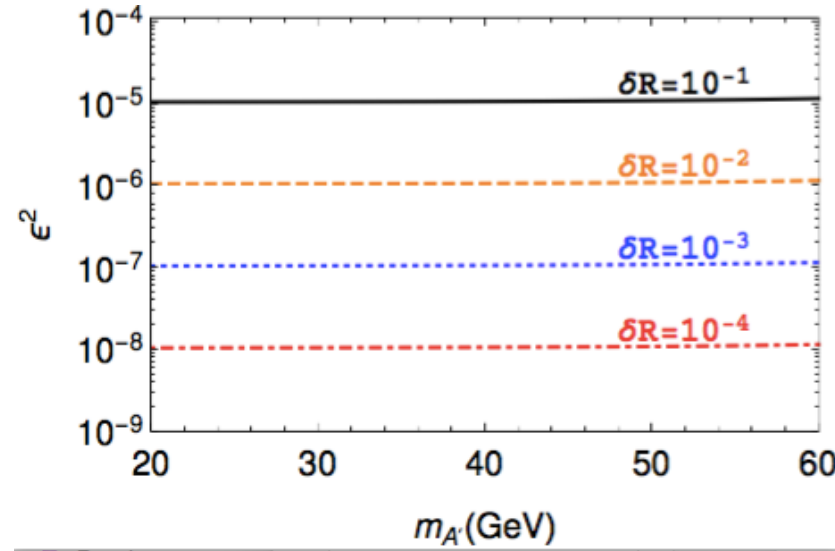
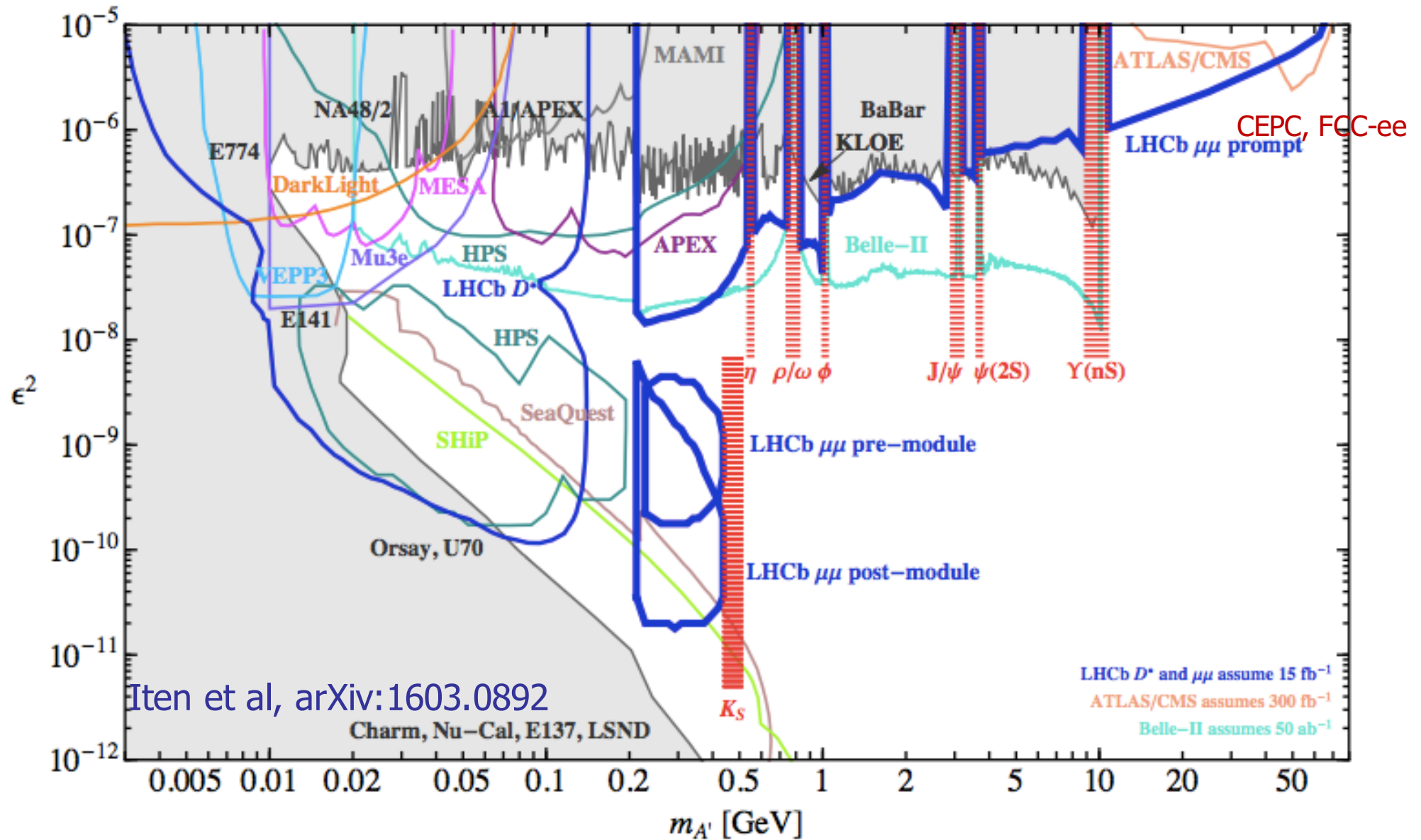


FIG. 3: $N_{\gamma\gamma}$ and $N_{\gamma A'}/\epsilon^2$ as functions of $m_{A'}$ for CEPC ($\sqrt{s} = 240 \text{ GeV}$) and FCC-ee ($\sqrt{s} = 160, 240, 350 \text{ GeV}$) for one year running.



CEPC may have advantage probing dark photon
at 10 to a few 10s ($\ll m_Z$) GeV mass range.





Spontaneous symmetry breaking and Abelian-NonAbelian gauge fields mixing

Arguelles, XG He, G. Ovanesyan, T. Peng and M. Ramsey-Mulsof, arXiv:1604.00044

Assuming that there is a field Δ^a transforming as 3 under $SU(2)_W$, then one can make gauge singlet: $W_{\mu\nu}^a X^{\mu\nu} \Delta^a$

If the VEV of $\langle \Delta^a \rangle = v_3/\text{sqrt}(2)$ along a particular direction in group space is not zero, one can generate kinetic mixing term

$$W_{\mu\nu}^3 X^{\mu\nu} v_3/\text{sqrt}(2)$$

Problem: not renormalizable.

If one gives up renormalizability one can write higher order operators to generate abelian and non-abelian gauge fields mixing!

In fact in the SM, one can generate such a mixing between $SU(2)_L$ and $U(1)_Y$

$$W_{\mu\nu}^a X^{\mu\nu} (H^\dagger \tau^a H)$$

Here H is the usual SM doublet!

Possible to have kinetic mixing between abelian and non-abelian gauge fields. Chen, Cline, and Frey, 2009; He, Ovanesyan, Ramsey-Musolf, 2014.

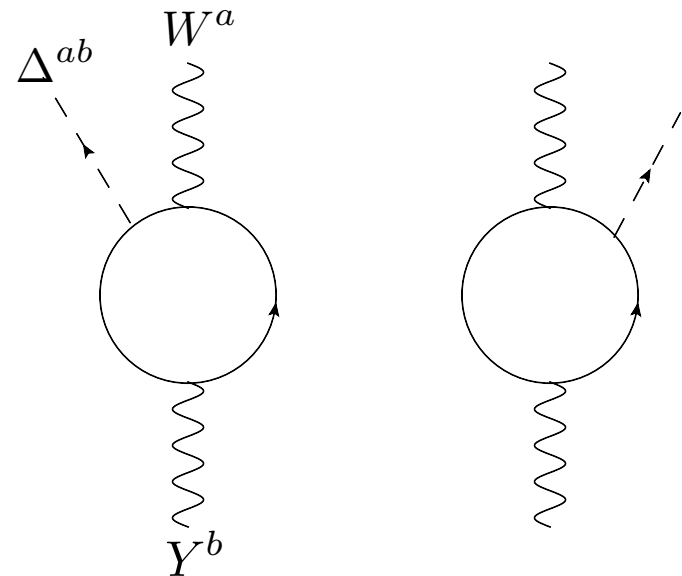
UV completion of kinetic mixing of Abelian-NonAbelian gauge field?

Yes, they can be generated at loop level starting from a renormalizable theory.

The particle in the loop carry both abelian and non-abelian charges.

One can even talking about $SU(N)$ and $SU(m)$ kinetic mixing

$$W_{\mu\nu}^a Y^{b\mu\nu} \Delta_{ab}$$



Kinetic mixing between an Abelian and a non-Abelian fields should be very common when going beyond SM.

A triplet $\Delta^a_{(0,3,0)}$ and W-B mixing

$$SU(2)_W = SU(2)_L, U(1)_X = U(1)_Y$$

$$\begin{aligned} L_{k-mixing} &= -\frac{1}{2}\alpha \frac{v_\Delta/\sqrt{2}}{\Lambda} B^{0,\mu\nu} W_{\mu\nu}^{3,0} & m_W^2 &= (m_W^0)^2 \left(1 + 4\frac{v_\Delta^2}{v^2}\right) \\ &= -\frac{1}{2}\epsilon \left(s_W c_W A_{\mu\nu}^0 A^{0,\mu\nu} - s_W c_W Z_{\mu\nu}^0 Z^{0,\mu\nu} + (c_W^2 - s_W^2) A_{\mu\nu}^0 Z^{0,\mu\nu}\right) \end{aligned}$$

Analysis the effects through S,T, U parameters

$$\begin{aligned} \Delta L_{eff} &= -\frac{A}{4} A_{\mu\nu}^0 A^{0,\mu\nu} - \frac{B}{2} W_{\mu\nu}^{+,0} W^{-,0,\mu\nu} - \frac{C}{4} Z_{\mu\nu}^0 Z^{0,\mu\nu} + \frac{G}{2} A_{\mu\nu}^0 Z^{0,\mu\nu} \\ &+ w(m_W^0)^2 W_\mu^{+,0} W^{-,0,\mu} + \frac{z}{2}(m_Z^0)^2 Z_\mu^0 Z^{0\mu}, \end{aligned}$$

$$A = 2s_W c_W \epsilon, \quad B = 0, \quad C = -2s_W c_W \epsilon, \quad G = -(c_W^2 - s_W^2)\epsilon, \quad w = 4\frac{v_\Delta^2}{v^2}, \quad z = 0.$$

$$\alpha S = 4s_W^2 c_W^2 \left(A - C - \frac{c_W^2 - s_W^2}{s_W c_W} G \right) = 4s_W^2 c_W^2 \left(4s_W c_W + \frac{(c_W^2 - s_W^2)^2}{s_W c_W} \right) \epsilon,$$

$$\alpha T = w - z = 4\frac{v_\Delta^2}{v^2},$$

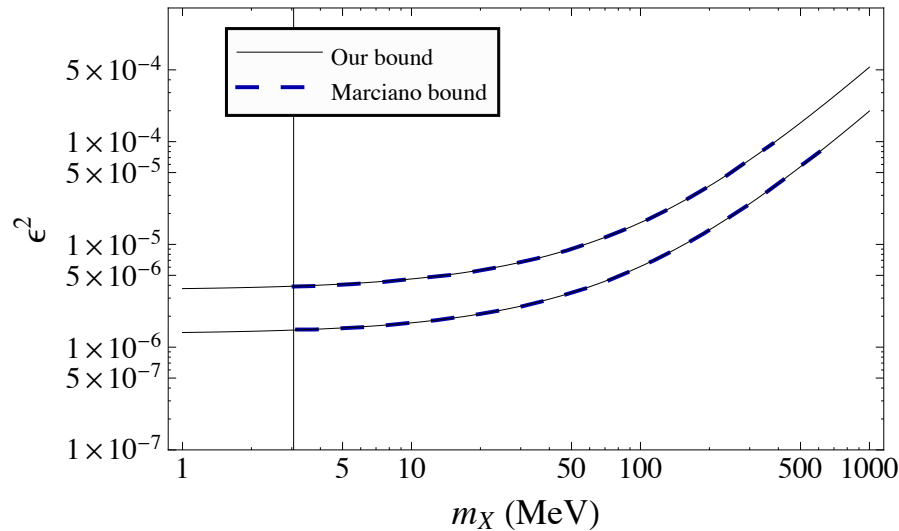
$$\alpha U = 4s_W^4 \left(A - \frac{1}{s_W^2} B + \frac{c_W^2}{s_W^2} C - 2\frac{c_W}{s_W} G \right) = 0.$$

Some phenomenological implications

$$\mathcal{O}_{WX}^{(5)} = -\frac{\beta}{\Lambda} \text{Tr} (W_{\mu\nu} \Sigma) X^{\mu\nu}$$

$$\epsilon = \beta \sin \theta_W \left(\frac{v_\Sigma}{\Lambda} \right)$$

Bound on ϵ from muon $g-2$ on kinetic mixing



Bound on ϵ_{WX} from muon $g-2$ on kinetic mixing

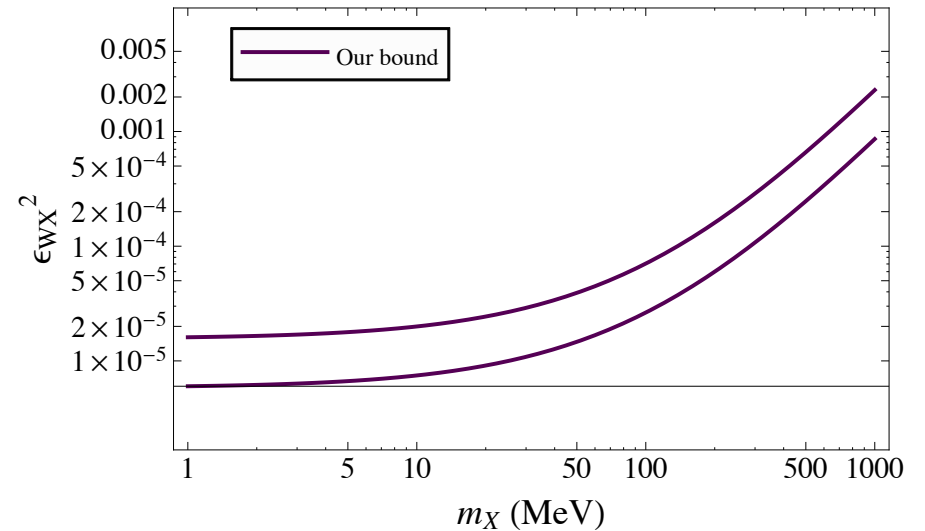


FIG. 1: Bound on abelian mixing parameter ϵ (left) and non-abelian mixing parameter ϵ_{WX} (right).

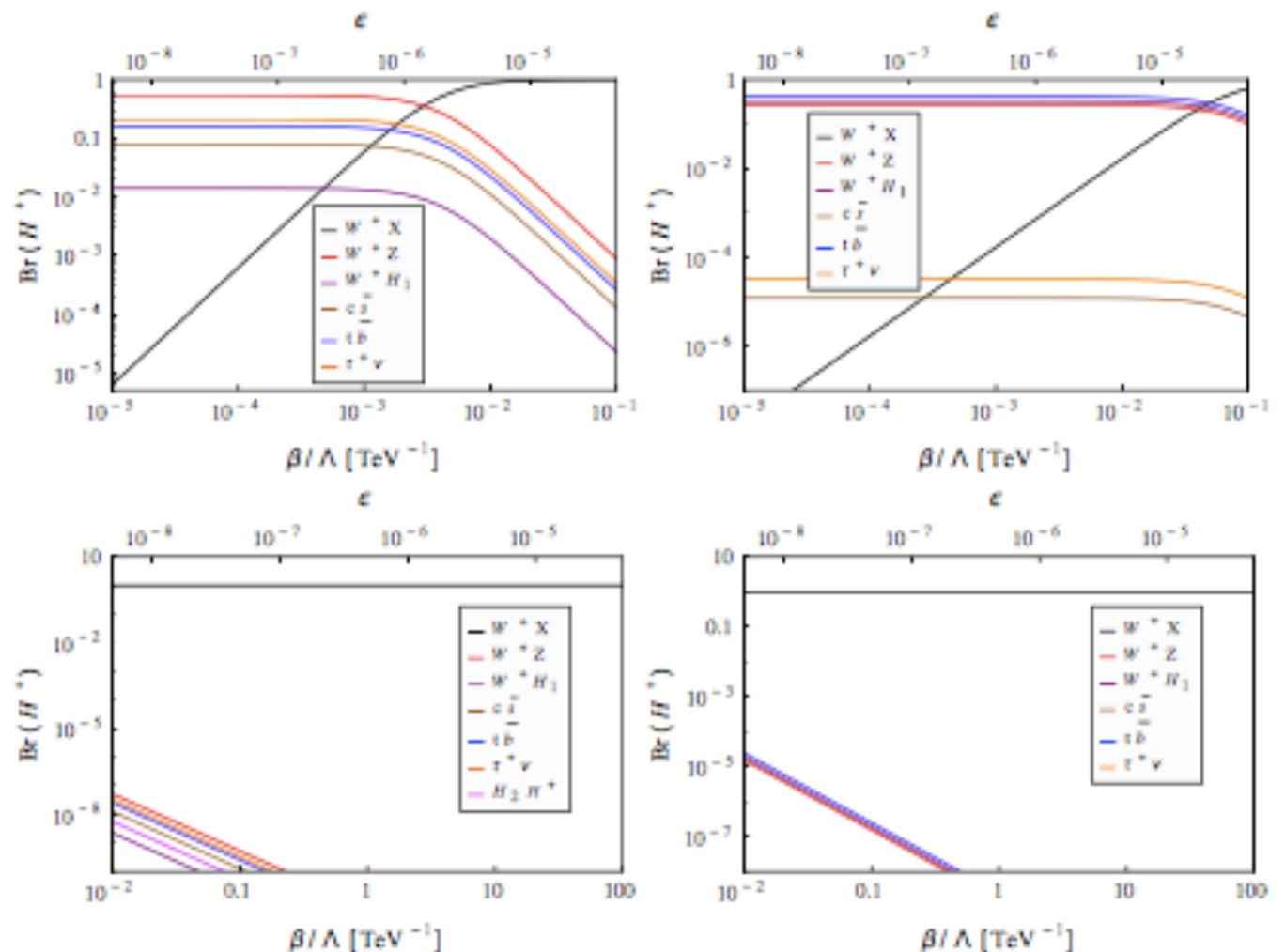
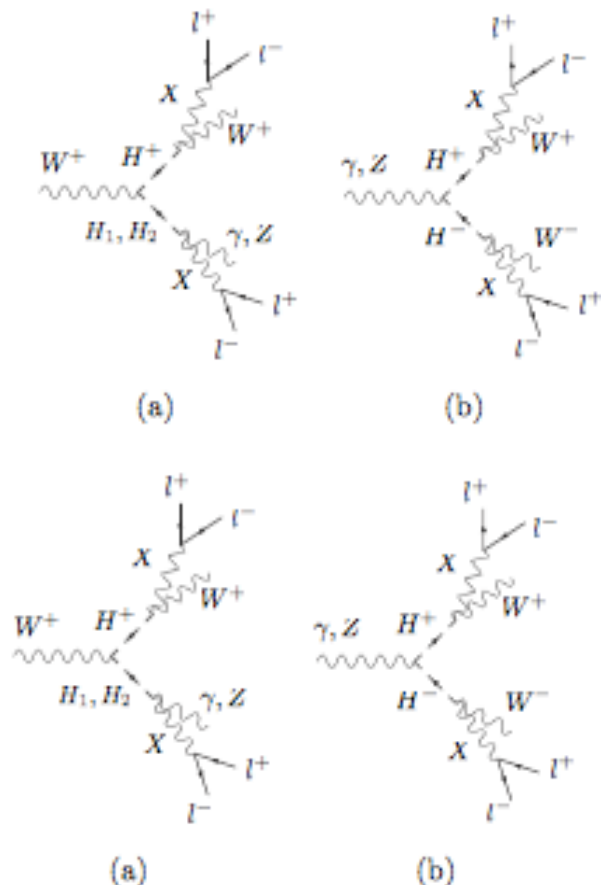
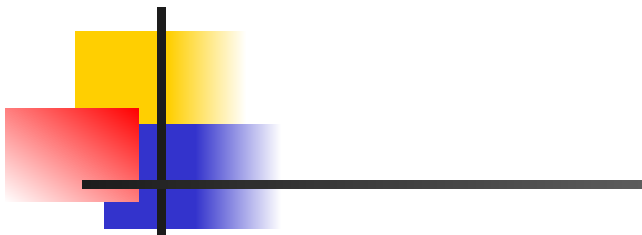


Figure 4. Branching ratios for H^+ decays as a function of β/Λ (bottom horizontal axis) and ϵ (upper horizontal axis) for $m_X = 0.4$ GeV. The top (bottom) row corresponds to $v_\Sigma = 1$ GeV ($v_\Sigma = 10^{-3}$ GeV), while the left (right) column corresponds to $m_{H^+} = 130$ GeV ($m_{H^+} = 130$ GeV). The solid black line indicates the branching ratio for $H^+ \rightarrow W^+ X$. Branching ratios for other final states are as indicated by the legend insert.

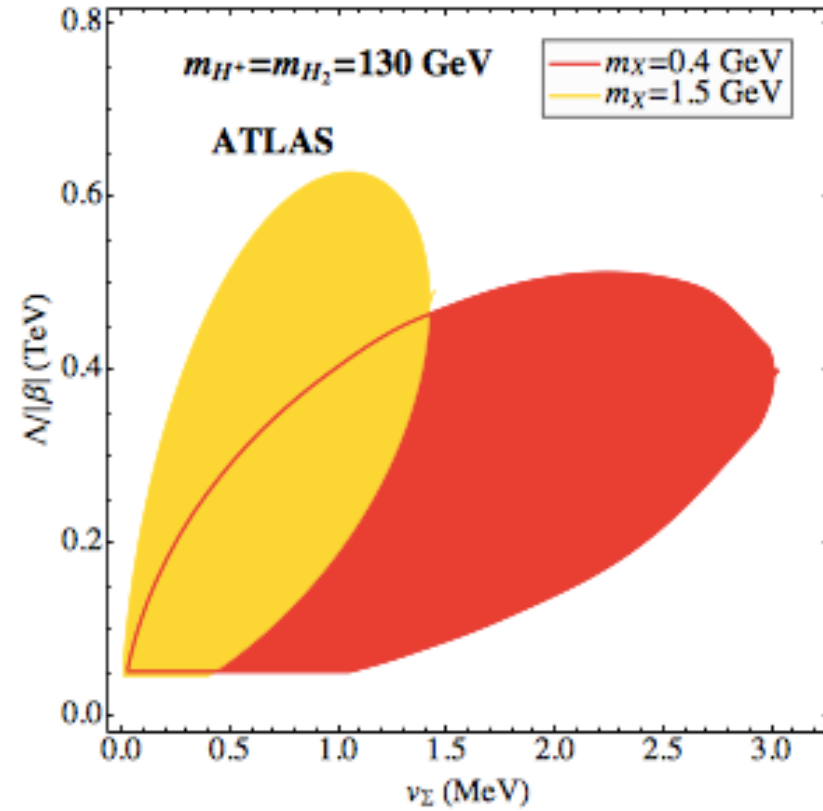
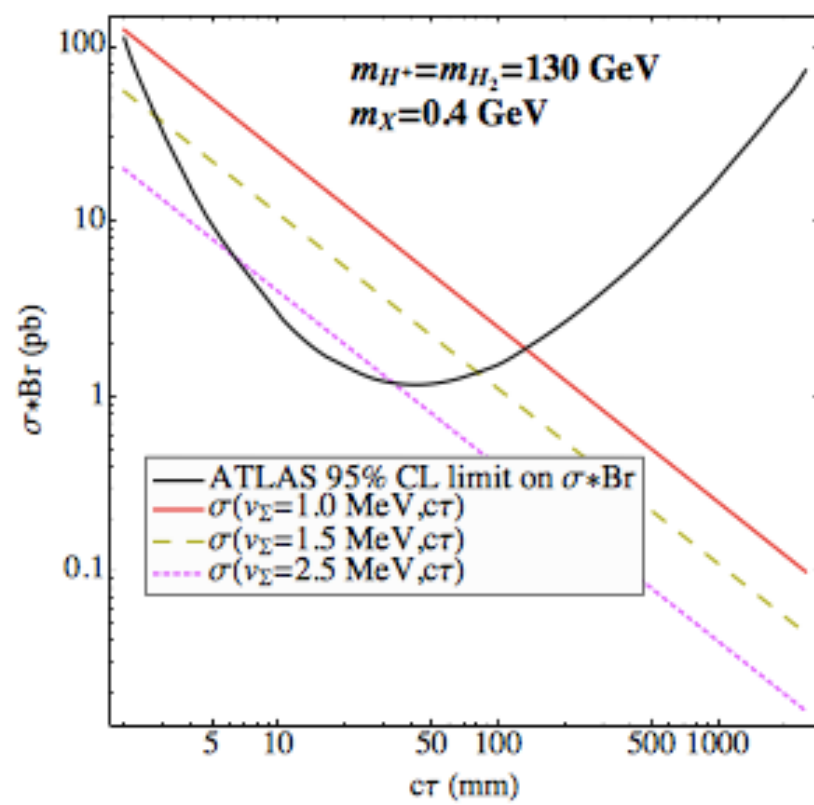


Figure 5. Constrains on triplet-assisted non-abelian kinetic mixing, recast from the ATLAS search reported Ref. [12]. The left panel gives the exclusion in the $(c\tau, \sigma \times \text{BR})$ plane, where the region above the parabola is excluded. The diagonal lines indicate the dependence of $\sigma \times \text{BR}$ on $c\tau$ for different representative choices of v_Σ . The right panel gives the exclusion region in the $(v_\Sigma, \Lambda/\beta)$ plane for $m_X = 0.4$ GeV (red region) and $m_X = 1.5$ GeV (yellow region).