

SUSY SEARCHES AT LHC AND BEYOND

Xuai Zhuang (庄胥爱)

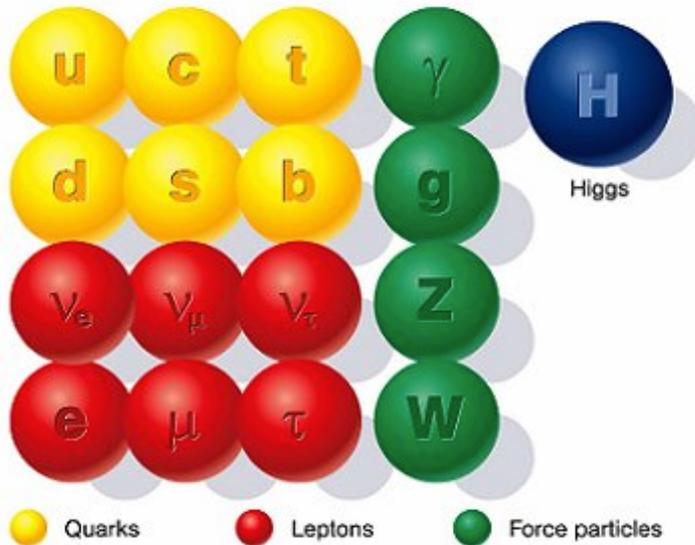
xuai.zhuang@cern.ch

IHEP, Beijing, China

18-21 Jan. 2016, HK

Standard Model and Supersymmetry

Standard particles

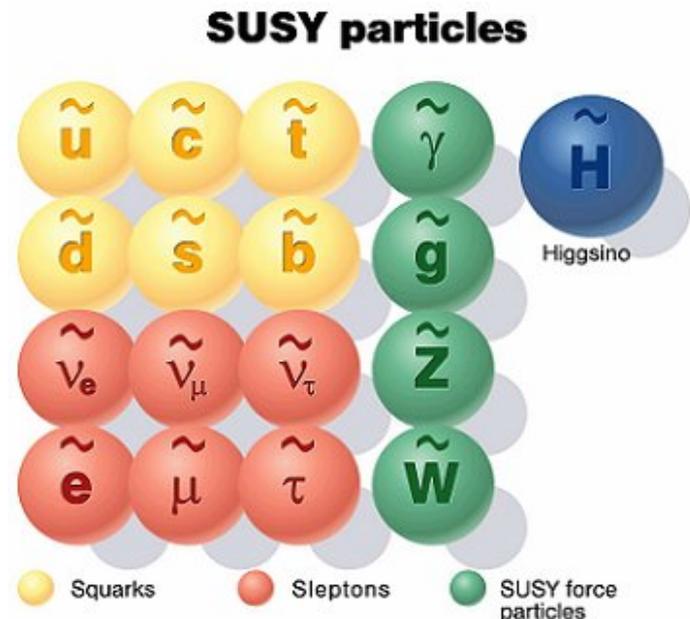
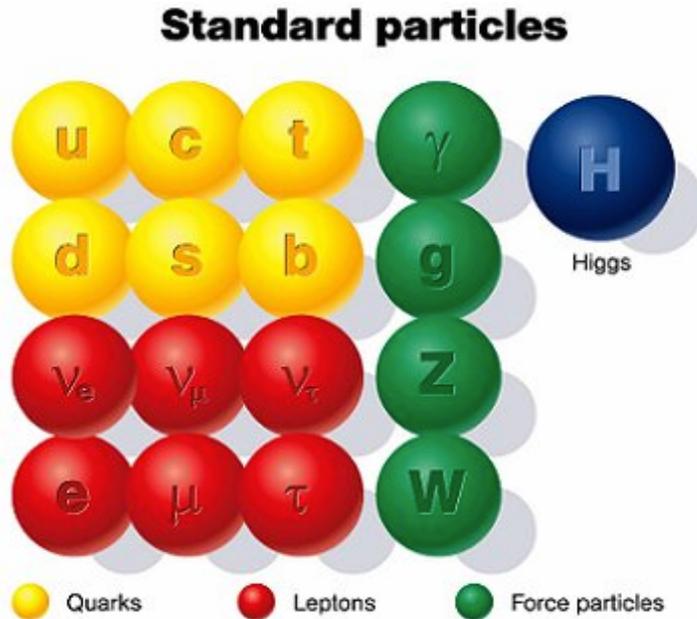


■ Standard Model (SM)

Very successful description of phenomena at TeV scale, but some shortcomings:

- Hierarchy problem
- Can not unify gauge couplings
- No dark matter (DM)
- ...

Standard Model and Supersymmetry



■ Standard Model (SM)

Very successful description of phenomena at TeV scale, but some shortcomings:

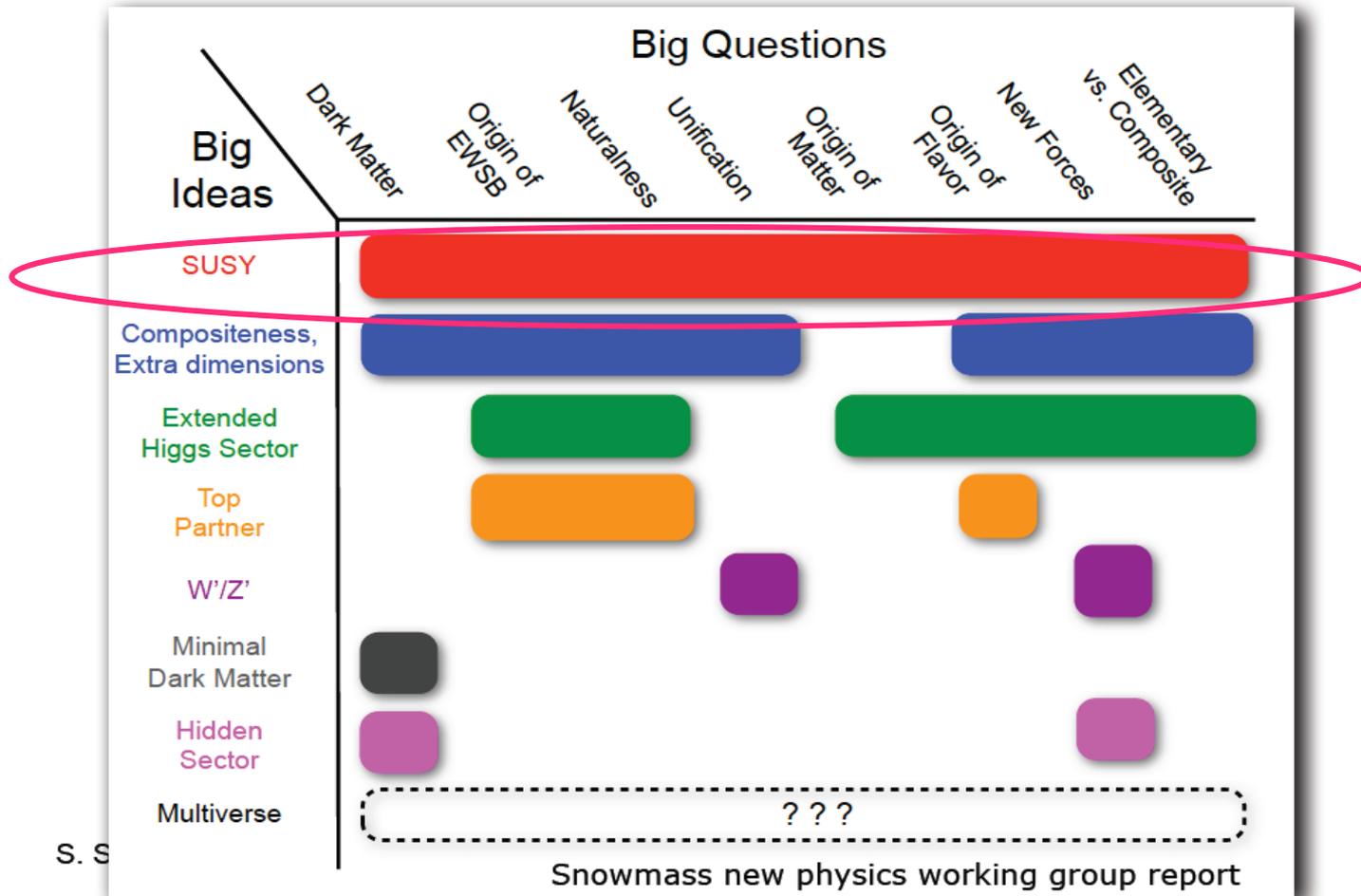
- Hierarchy problem
- Can not unify gauge couplings
- No dark matter (DM)
- ...

■ Supersymmetry (SUSY)

Unique extension of Poincare spacetime symmetry

- Moderate the hierarchy problem
- Grand unification of gauge couplings
- Provide excellent DM candidate
- ...

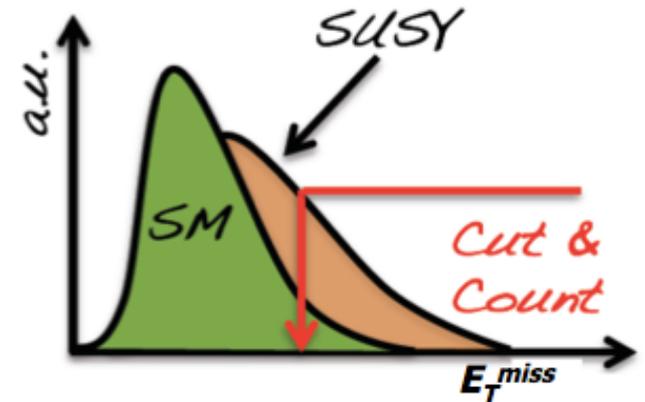
New Physics beyond the SM



- If SUSY is at TeV scale, it will be produced copiously at LHC
- SUSY search is one of the most hot topic at LHC and beyond

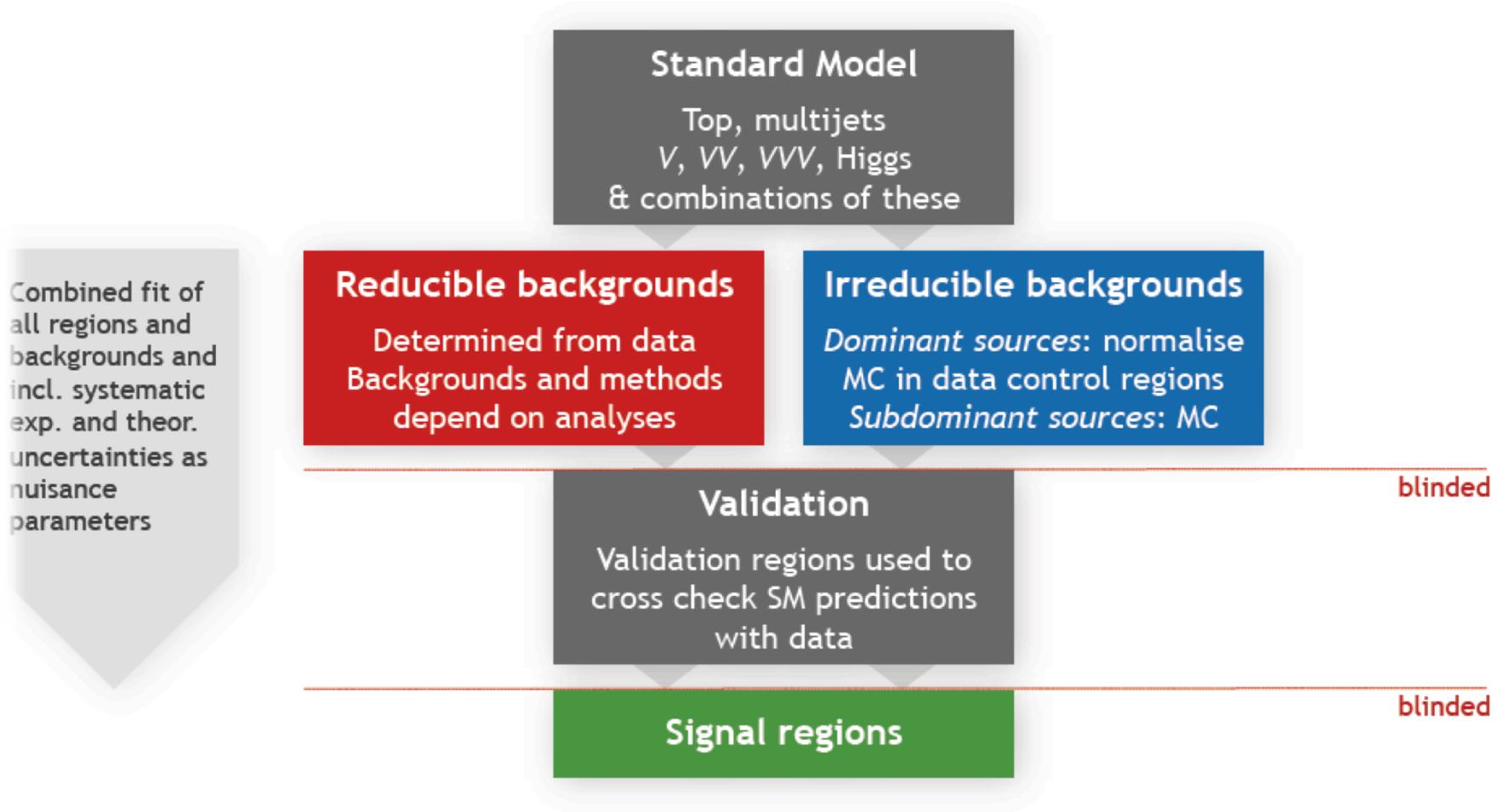
SUSY Search Strategy

- **SUSY search strategy:** search for deviation from SM
- **SUSY sensitive variables:** Try to establish excess of events in some **sensitive kinematic distribution** (E_T^{miss} , M_{eff} , m_T ...)
- **SM background:** SUSY searches rely on accurate modeling of the Standard Model backgrounds

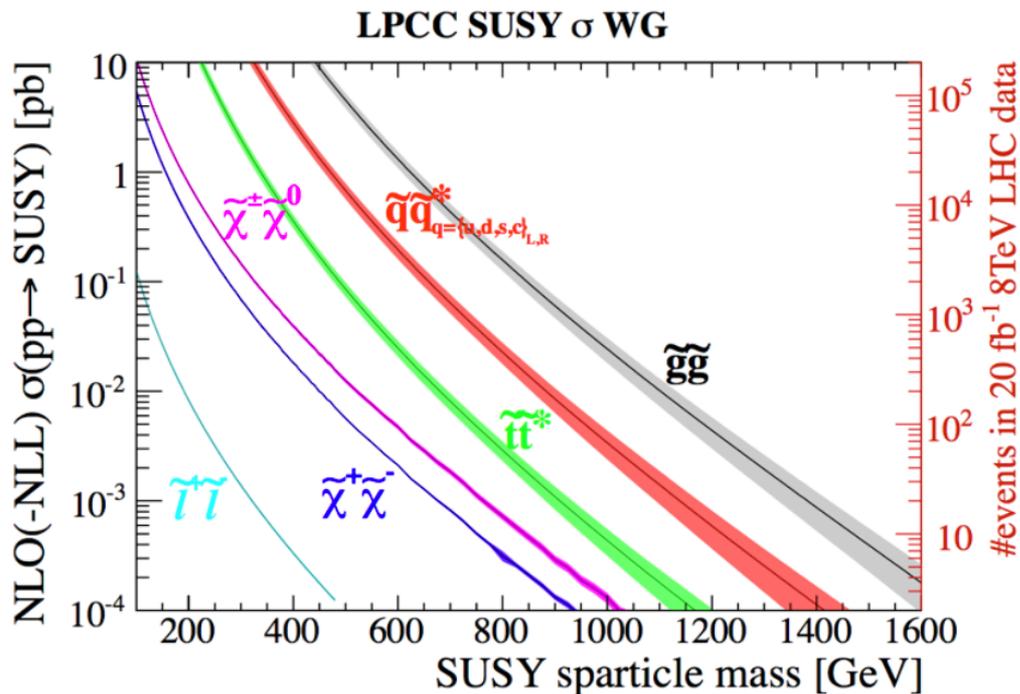


SM Background Modeling

- SUSY searches rely on accurate modeling of the Standard Model backgrounds



SUSY Search @ LHC



Strong production:

- ☐ targeting gluinos and 1st and 2nd generation squarks
- ☐ by far largest cross-sections

3rd generation:

- ☐ targeting stop and sbottoms
- ☐ Should be lowest mass squarks for naturalness reasons

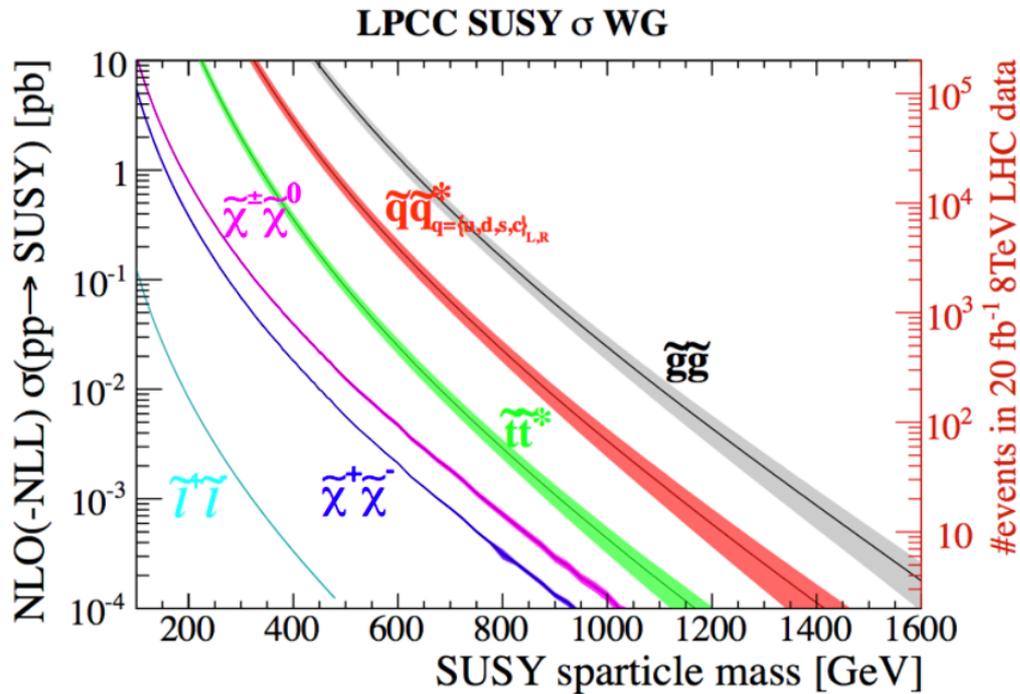
Electroweak production:

- ☐ targeting Electroweakinos, sleptons
- ☐ Lowest mass sparticles, clean signature

RPV/LL:

- ☐ targeting R-parity violating models and long lived sparticles
- ☐ More exotic models

SUSY Search @ LHC



Outline:

→ SUSY Search from
 real data @ LHC
 (8-13 TeV)



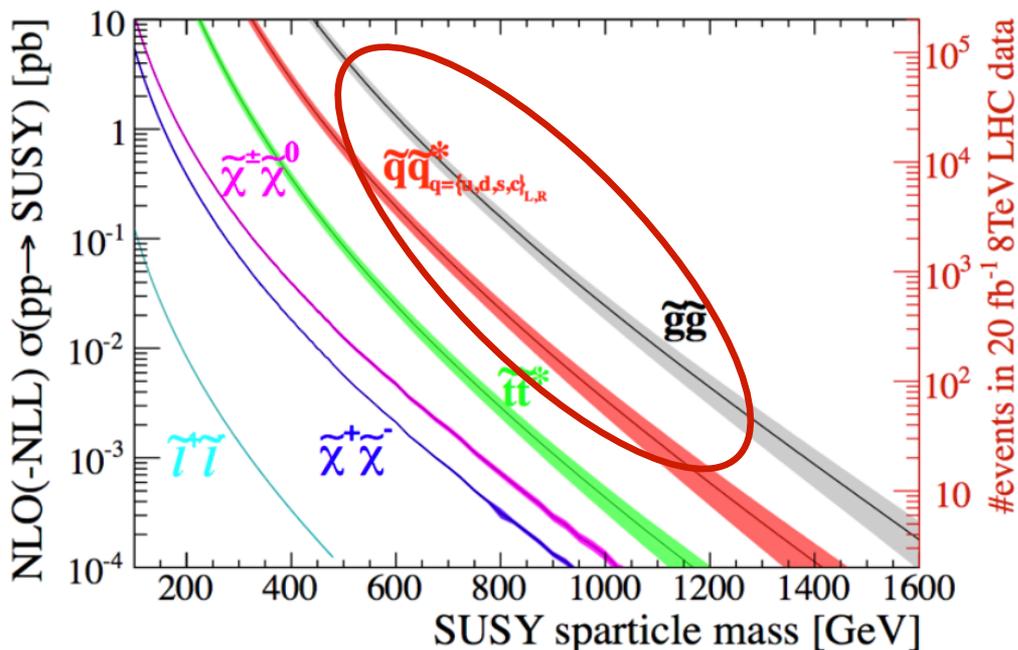
→ Longer term
 prospects @ LHC and
 Future Collider (14,
 33, 100 TeV)





SUSY Search @ LHC (Run1+2)

LPCC SUSY σ WG



The results are based on 3.3 fb⁻¹ @ 13 TeV (Run2)

Strong production:

- targeting gluinos and 1st and 2nd generation squarks
- by far largest cross-sections

3rd generation:

- targeting stop and sbottoms
- Should be lowest mass squarks for naturalness reasons

Electroweak production:

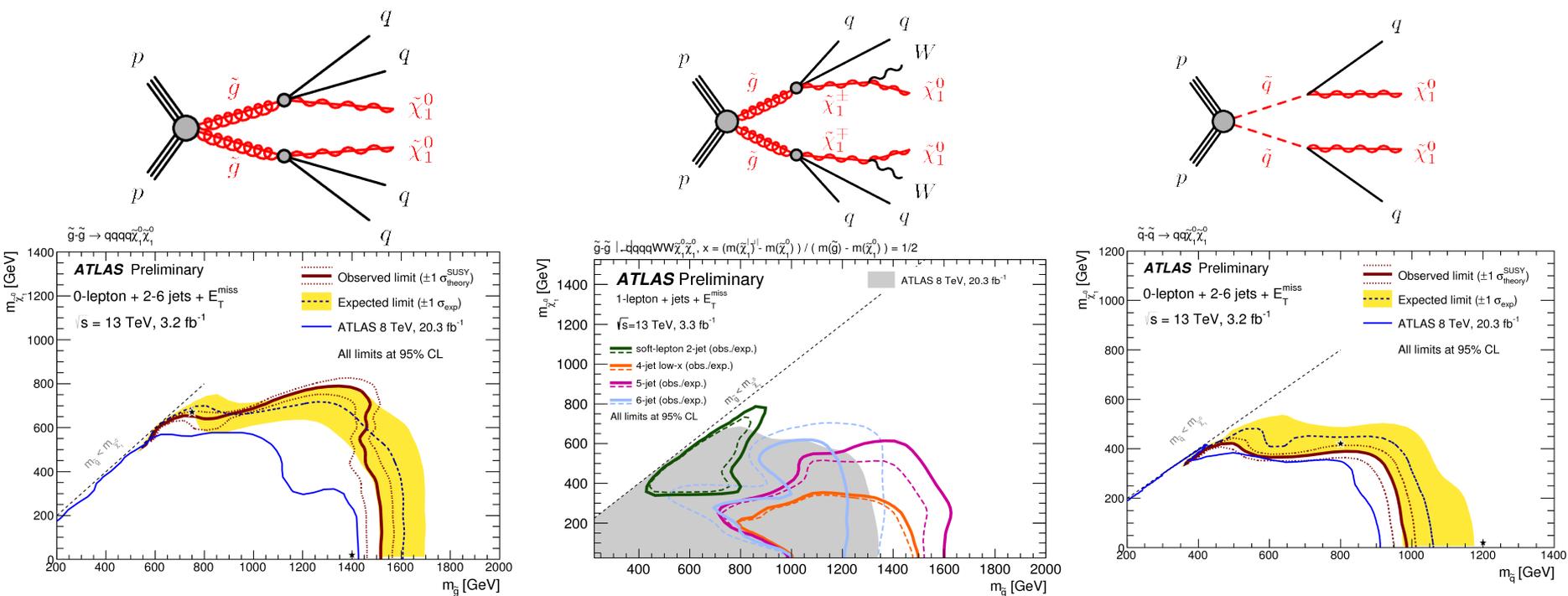
- targeting Electroweakinos, sleptons
- Lowest mass sparticles, clean signature

RPV/LL:

- targeting R-parity violating models and long lived sparticles
- More exotic models

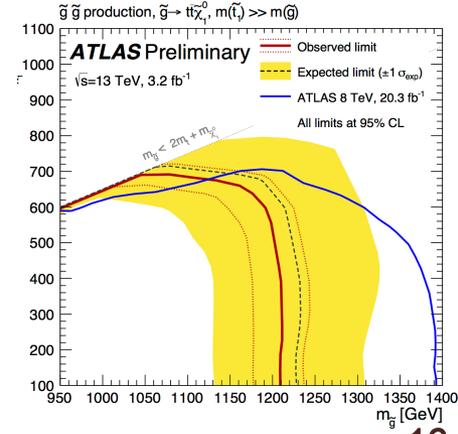
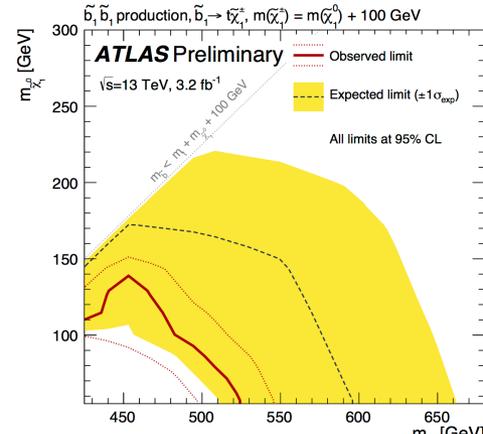
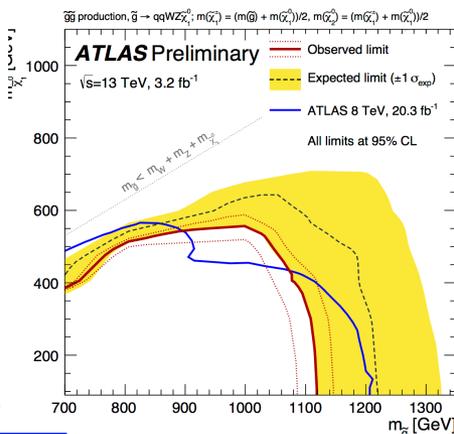
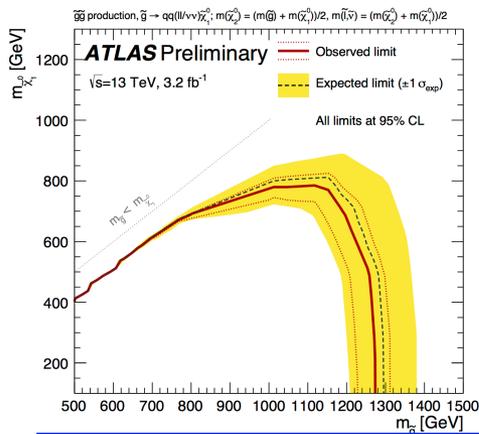
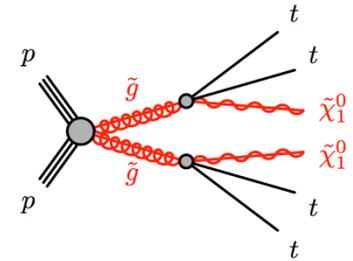
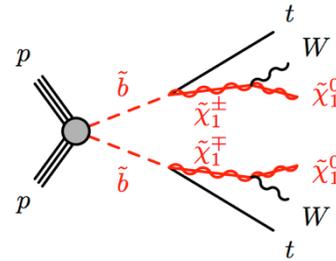
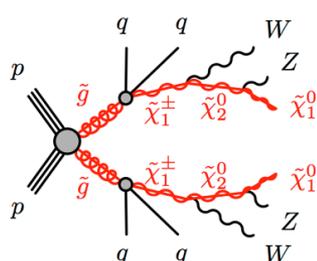
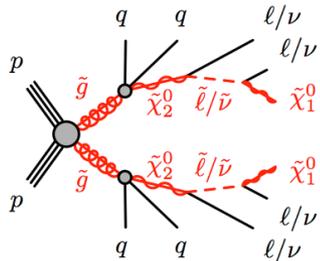
Strong Production: 0-1L+jets+MET

- Search for **gluinos** and **1st and 2nd generation squarks**
- Final states with jets, missing transverse momentum and **no or one isolated lepton (e/μ)** (**IHEP: 1L channel**)
- Signal to BG discrimination based on: **Meff, MET, mT**
- 28 signal regions defined targeting different search scenarios
- **Excludes gluino masses up to 1.6 TeV, squark mass up to 980 GeV**

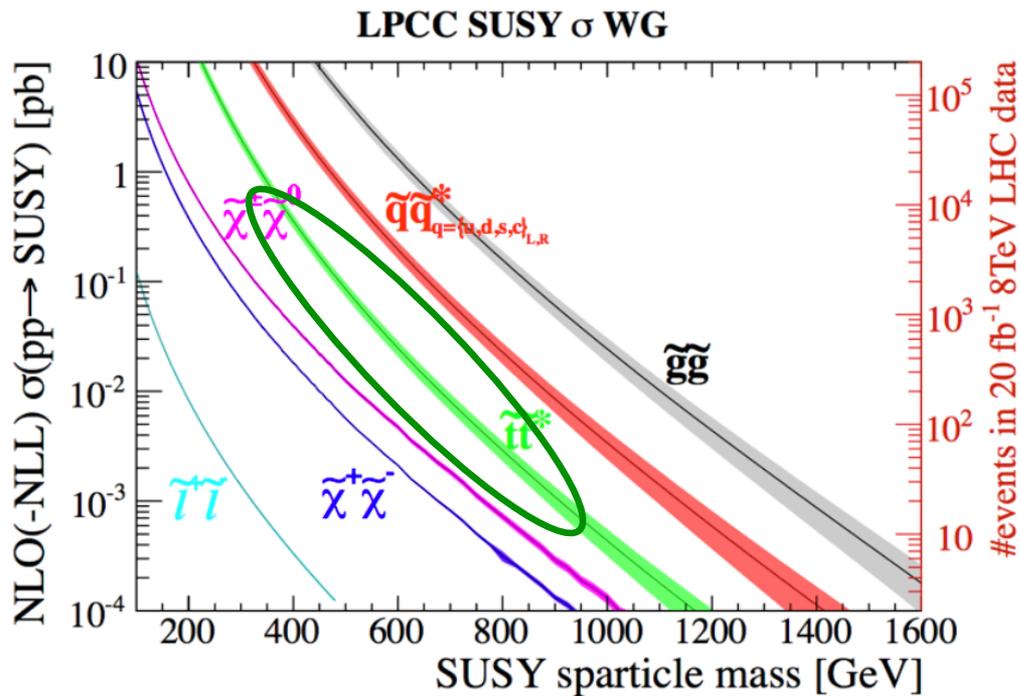


Strong Production: SS/3L+jets+MET

- Search for squarks/gluinos via long decay chain in SS/3L (IHEP)**
 - Sensitive for a wide range of models (Fig. 1)
 - Very clean channels with only tiny SM bg (mainly top+V, diboson, triboson) → **A good probe for new physics**
- 4 SRS defined, targeting specific scenarios
- Glino mass <1.1-1.3 TeV and LSP mass < 550-800 GeV are excluded for gluino pair production**



SUSY Search @ LHC



The results are based on 3.3 fb⁻¹ @ 13 TeV (Run2) for sbottom, 20 fb⁻¹ @ 8 TeV (Run1) for stop

Strong production:

- targeting gluinos and 1st and 2nd generation squarks
- by far largest cross-sections

3rd generation:

- targeting stop and sbottoms
- Should be lowest mass squarks for naturalness reasons

Electroweak production:

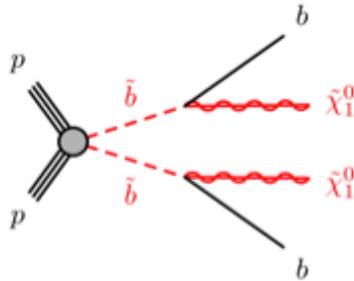
- targeting Electroweakinos, sleptons
- Lowest mass sparticles, clean signature

RPV/LL:

- targeting R-parity violating models and long lived sparticles
- More exotic models

Strong Production: $\tilde{b}\tilde{b}$

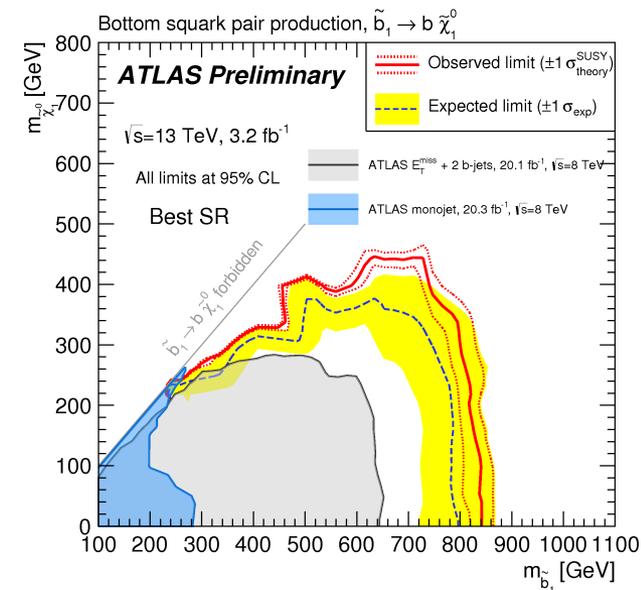
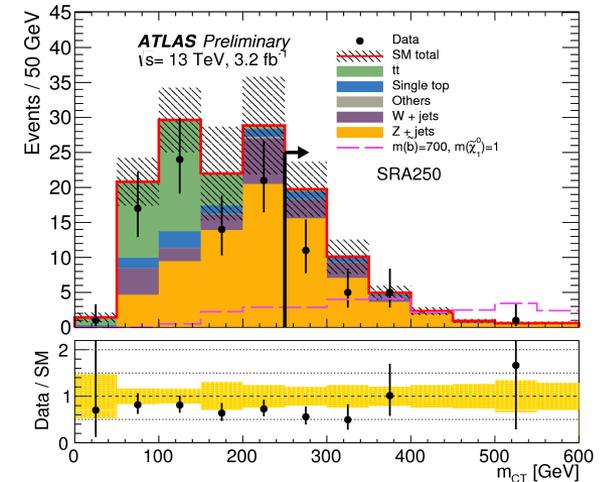
- Search for sbottom directly from $\tilde{b}\tilde{b}$ production with a 2b + MET FS



- Discriminate variables: m_{CT} , MET
- 2 signal regions defined with 2 b-jets and medium or tight MET cut
- No significant excess observed
- Excludes sbottom masses up to 850 GeV

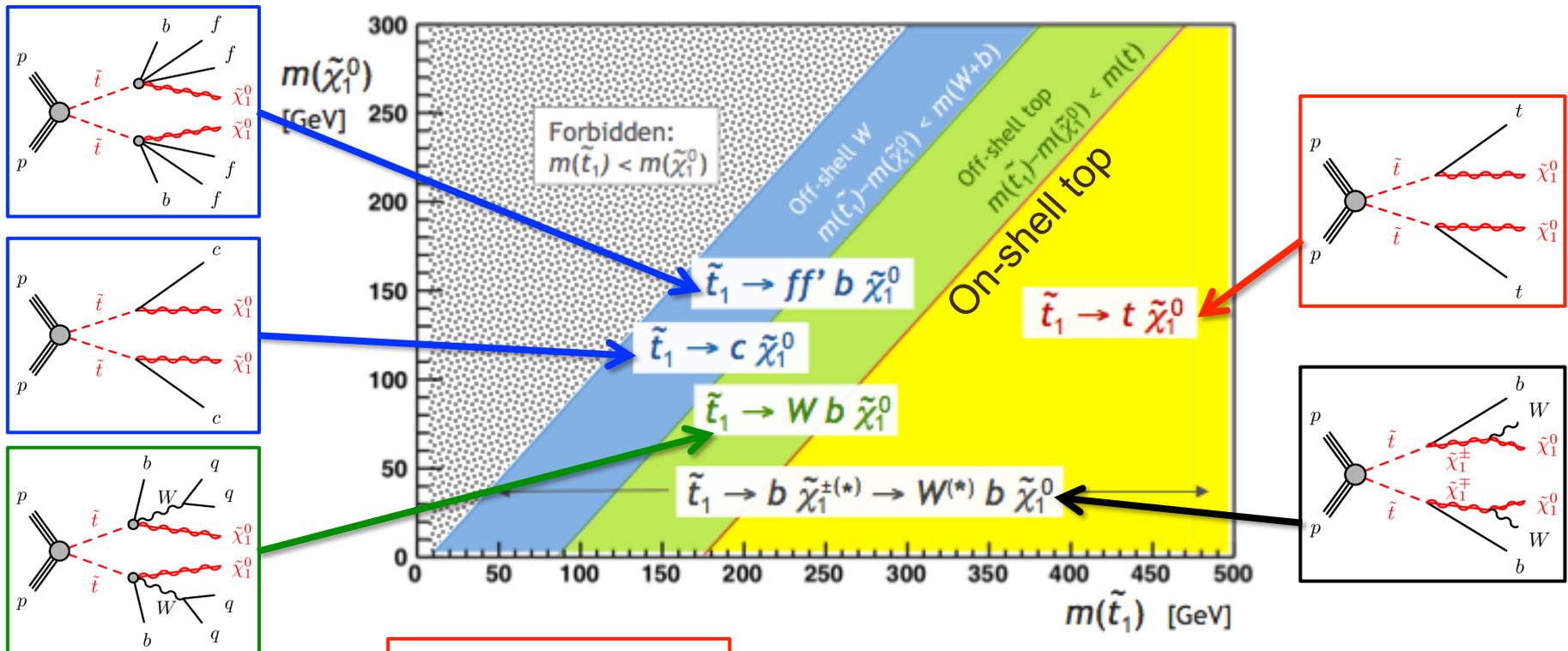
$$m_{CT}^2(v_1, v_2) = [E_T(v_1) + E_T(v_2)]^2 - [\mathbf{p}_T(v_1) - \mathbf{p}_T(v_2)]^2$$

ATLAS-CONF-2015-066

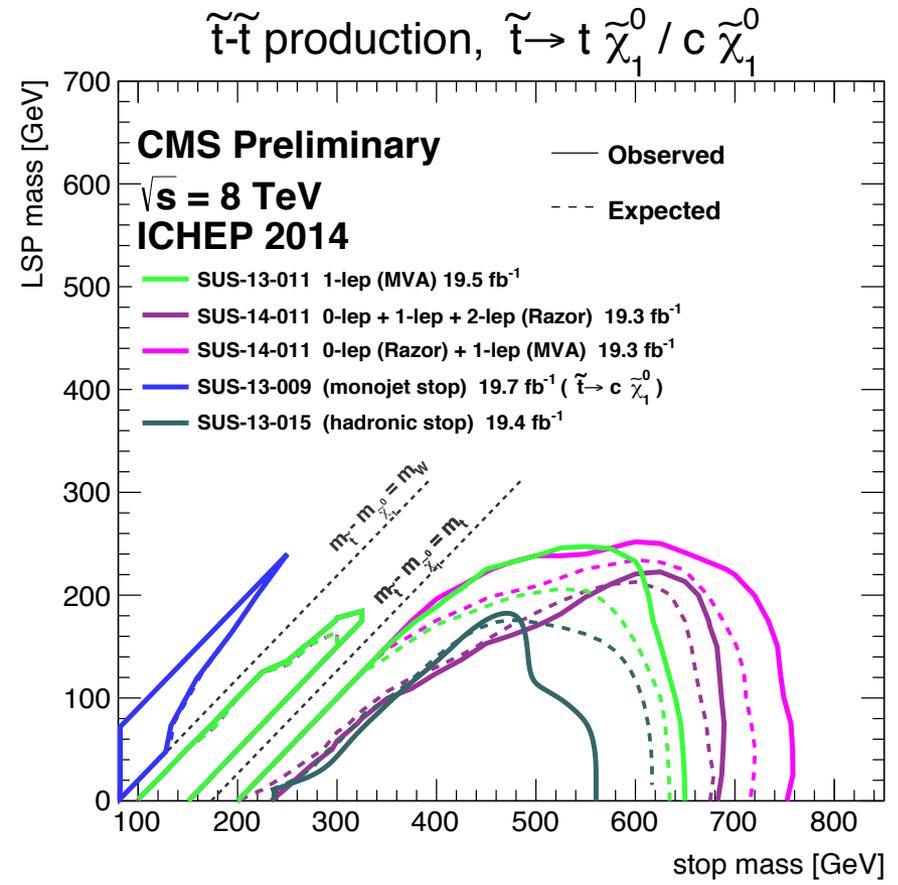
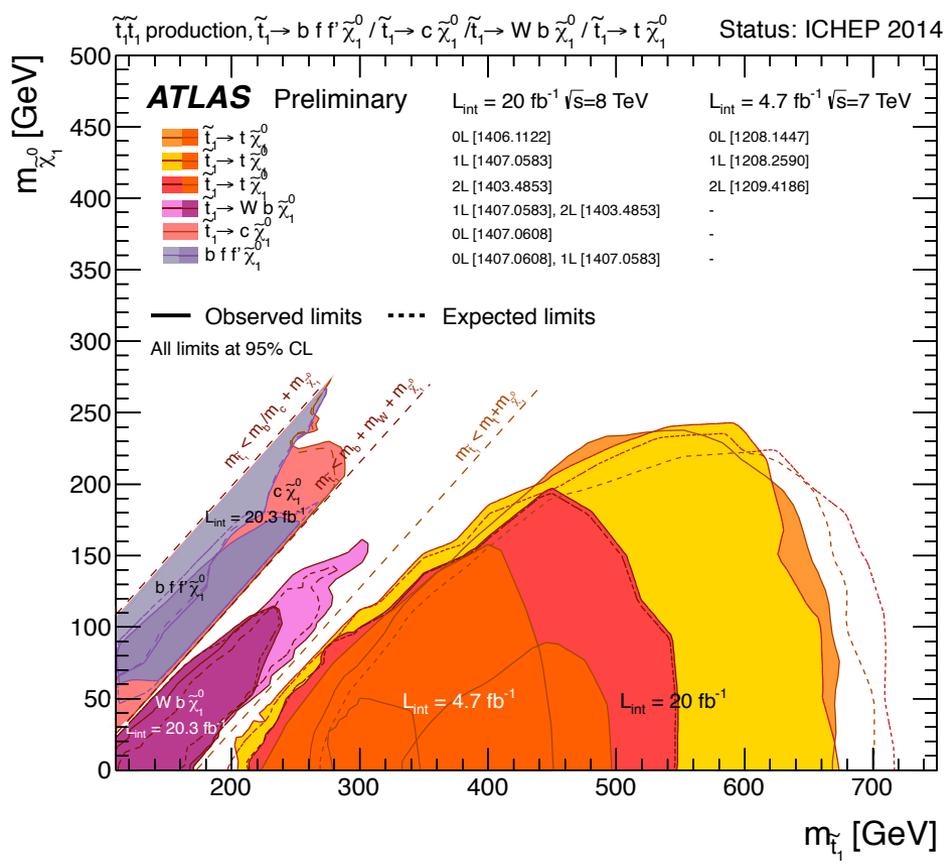


Strong Production: $\sim t \sim t$

- Search for **stop** directly from $\sim t \sim t$ production
- **Large spectrum of possible stop decays**, covering range from low to heavy stop mass, various decay modes.

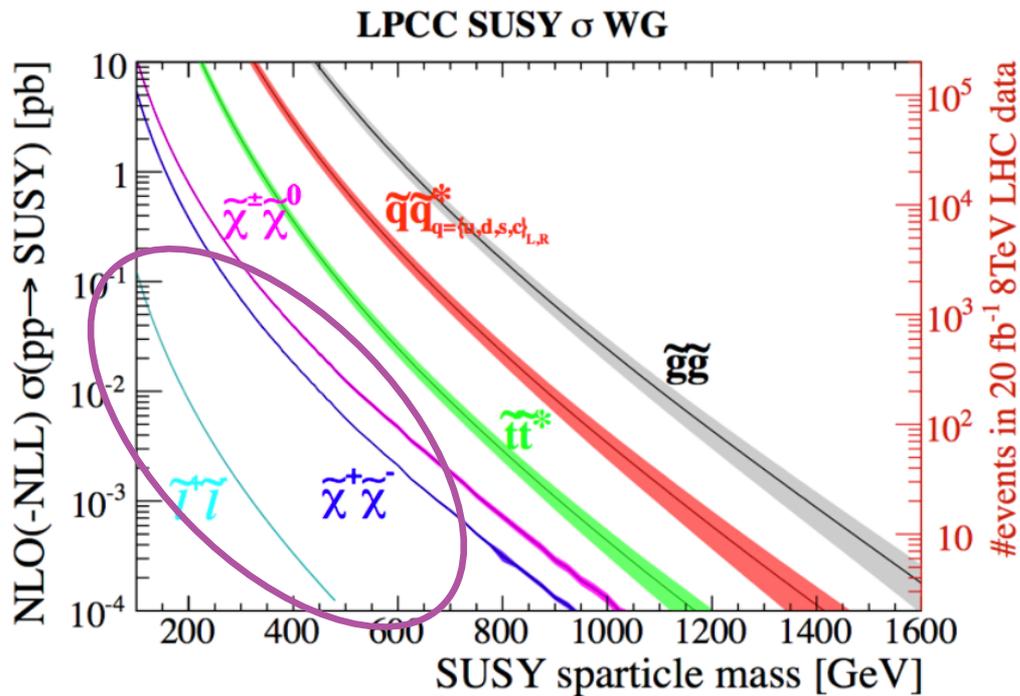


Direct stop pair production Summary



■ Exclusion for $m(\tilde{t}_1) < \sim 660 \text{ GeV}$ for massless LSP, exclusion up to $m(\text{LSP}) \sim 250 \text{ GeV}$

SUSY Search @ LHC



**The results are based on 20 fb⁻¹
@ 8 TeV (Run1)**

Strong production:

- targeting gluinos and 1st and 2nd generation squarks
- by far largest cross-sections

3rd generation:

- targeting stop and sbottoms
- Should be lowest mass squarks for naturalness reasons

Electroweak production:

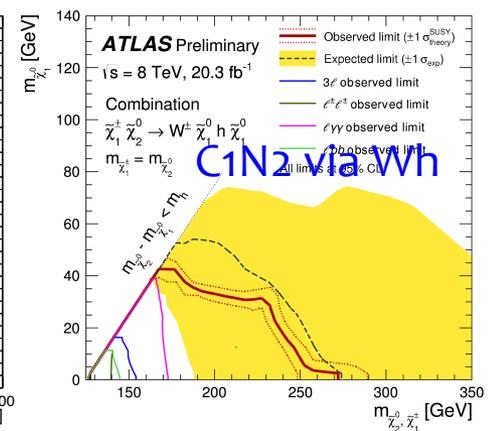
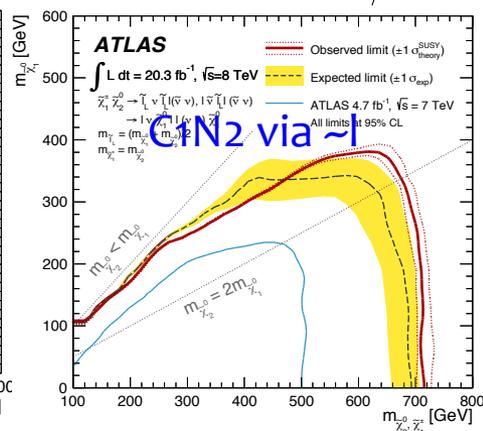
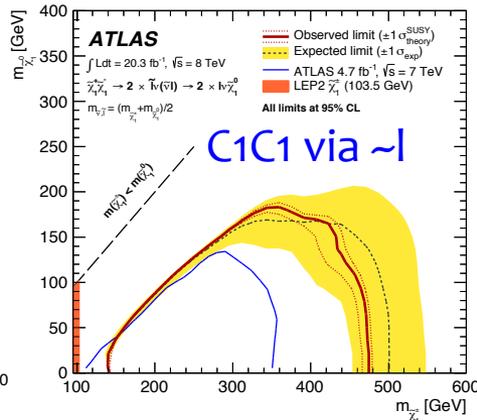
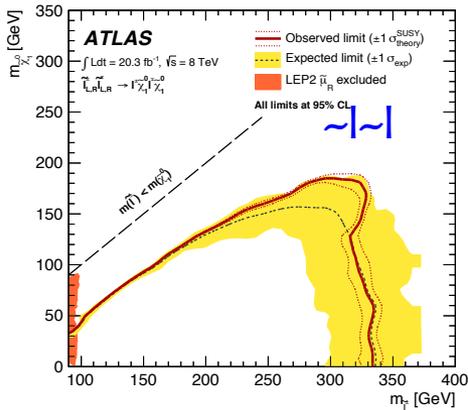
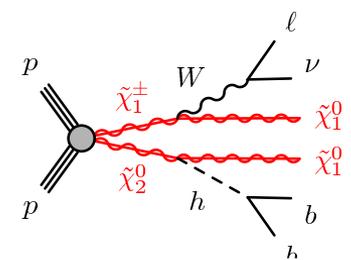
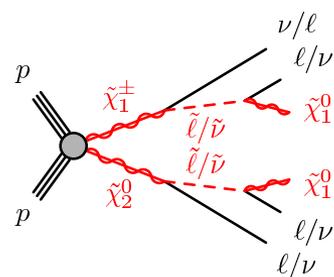
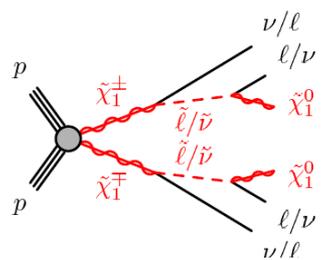
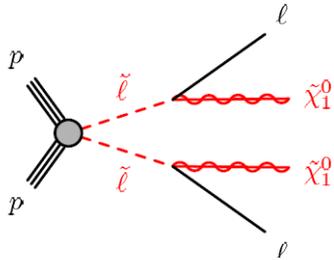
- targeting Electroweakinos, sleptons
- Lowest mass sparticles, clean signature

RPV/LL:

- targeting R-parity violating models and long lived sparticles
- More exotic models

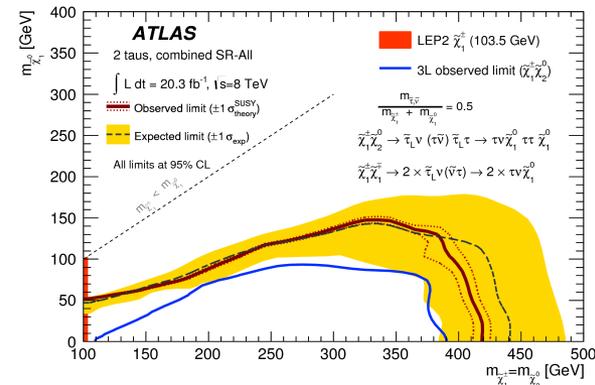
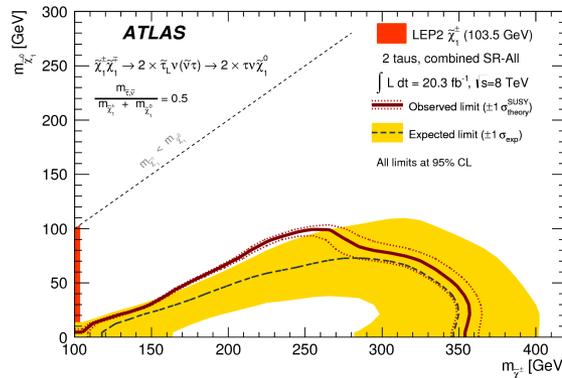
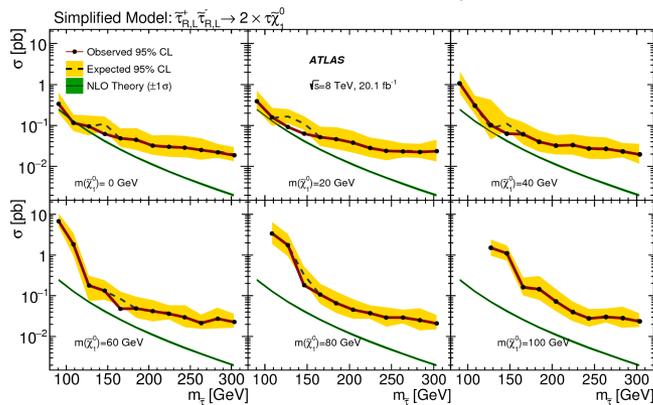
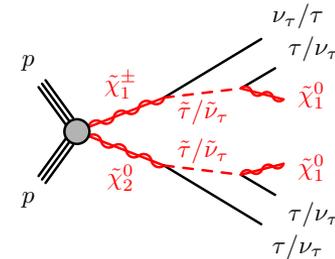
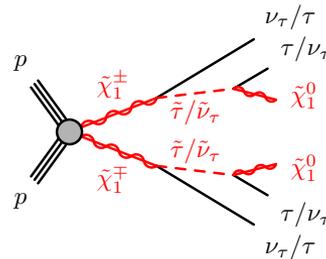
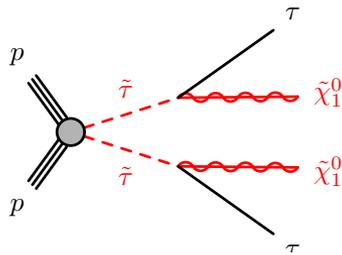
EWK Production: 1-3L+MET

- Search for **sleptons** with **2L (e/μ) + MET FS** → **~l > 330 GeV**
- Search for **charginos and neutralinos** with **2-3L (e/μ) + MET FS**
→ **Excludes electroweakino masses up to 400-700 GeV**
- Search for **charginos and neutralinos via higgs decay (Wh → 1l + bb, γγ, ll, ττ)** → **Excludes electroweakino masses up to 250 GeV**

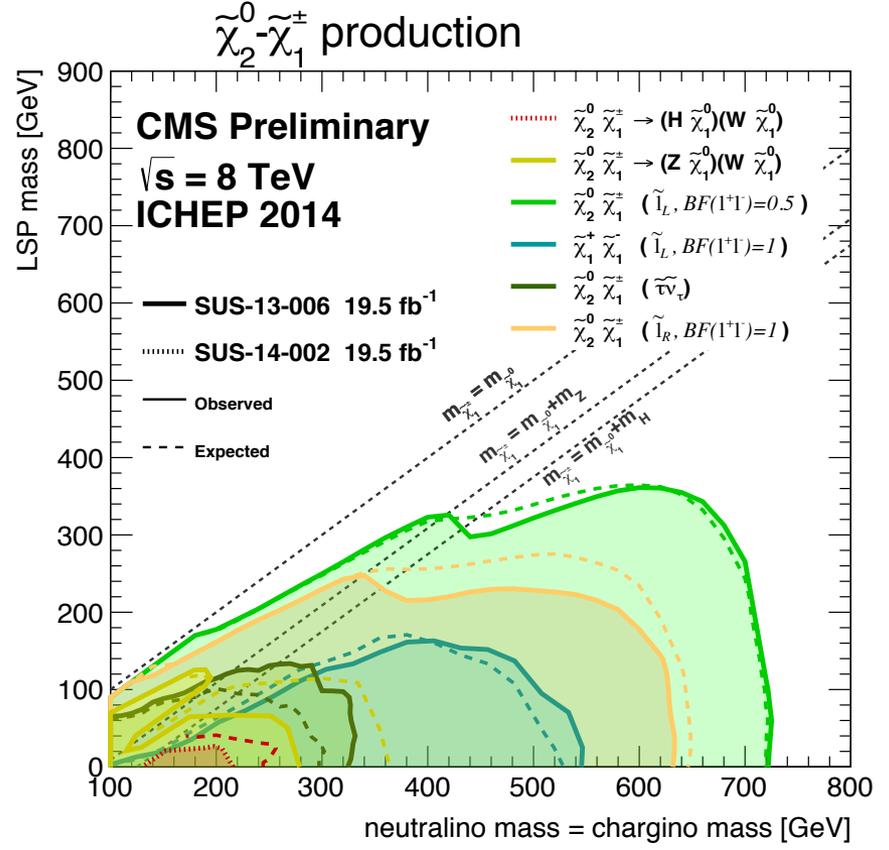
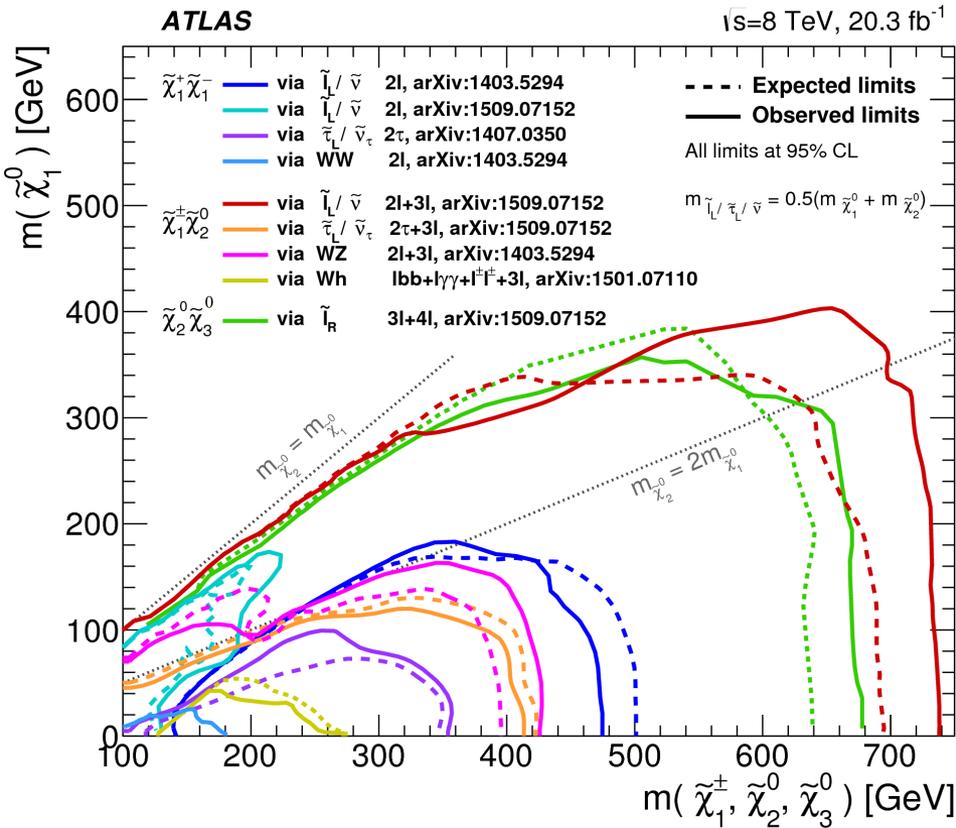


EWK Production: 2tau+MET

- IHEP member firstly proposed the search for stau and gaugino with final state: $\geq 2\tau + \text{MET}$, which is also the first search in LHC experiment.
- 4SRs targeting different scenarios
 - Excludes electroweakino masses up to 350-400 GeV



EWK Production Summary



- Comparable for C1N2 via slepton
- CMS: no results on C1C1 via stau and WW



Prospects at Future Proton Colliders

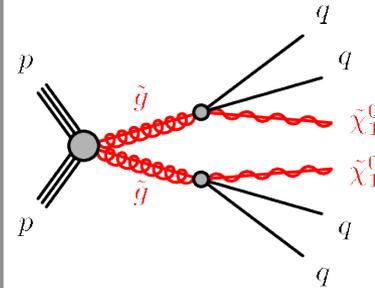
arXiv:1311.6480

Machine	\sqrt{s}	Final Integrated Luminosity
LHC Phase I	14 TeV	300 fb ⁻¹
HL-LHC or LHC Phase II	14 TeV	3000 fb ⁻¹
HE-LHC	33 TeV	3000 fb ⁻¹
VLHC	100 TeV	3000 fb ⁻¹

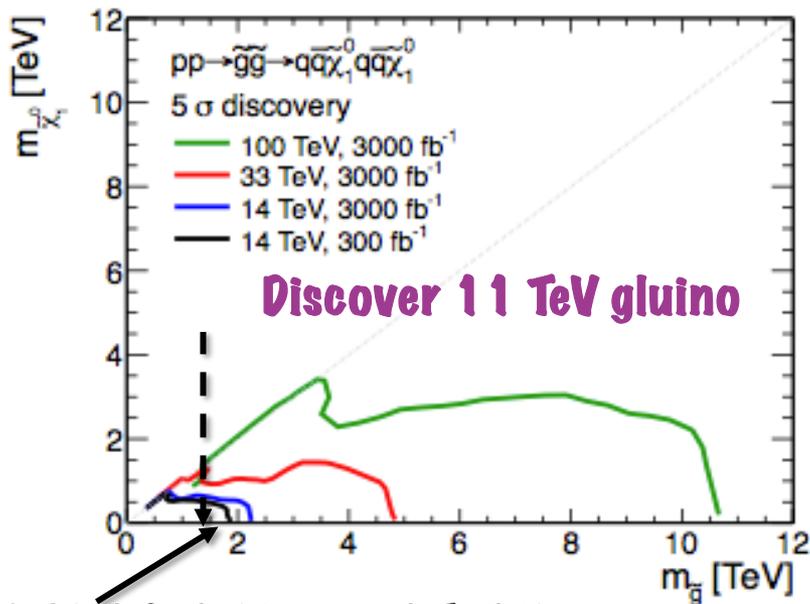
- Long term prospects for 4 collider scenarios have been studied (14, 33, 100 TeV @3000 fb⁻¹)
- Use same search strategy as Run1@LHC
- Use simple analysis strategies, avoid assumption, on detector design, pileup sensitivity, etc

Glino-Neutralino Signature

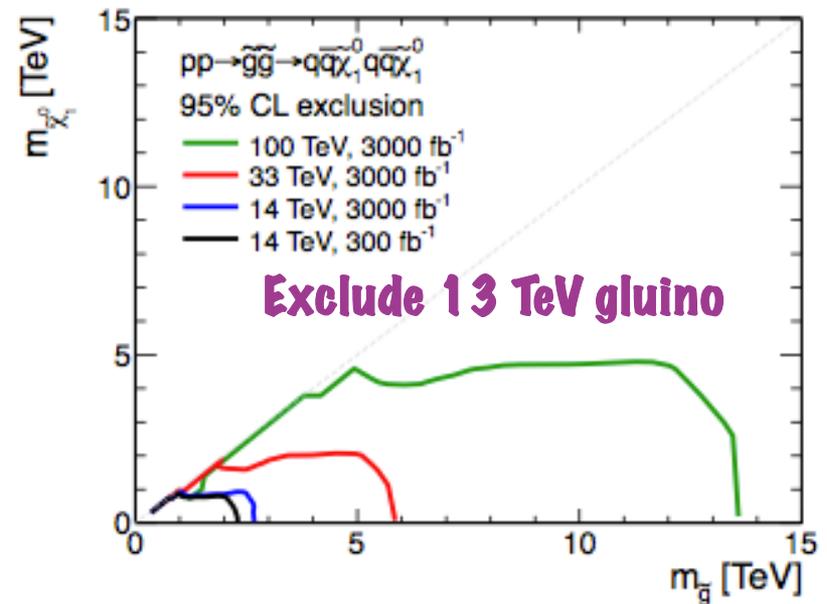
- Search for gluinos with no lepton, multi-jets, large missing transverse momentum
- Signal to BG discrimination based on: MET, HT (Σ jet pt)
- Discover (Exclude) 11 (13) TeV gluino
- Increasing the center-of-mass energy has a tremendous impact on the experimentally available parameter space (~ 5 x beyond 14 TeV @100 TeV)



arXiv:
1311.6480



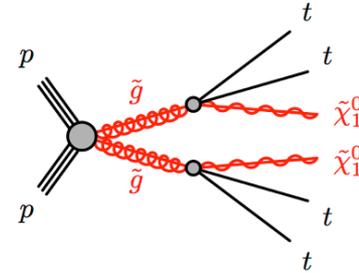
LHC 13 TeV limit ~ 1.5 TeV



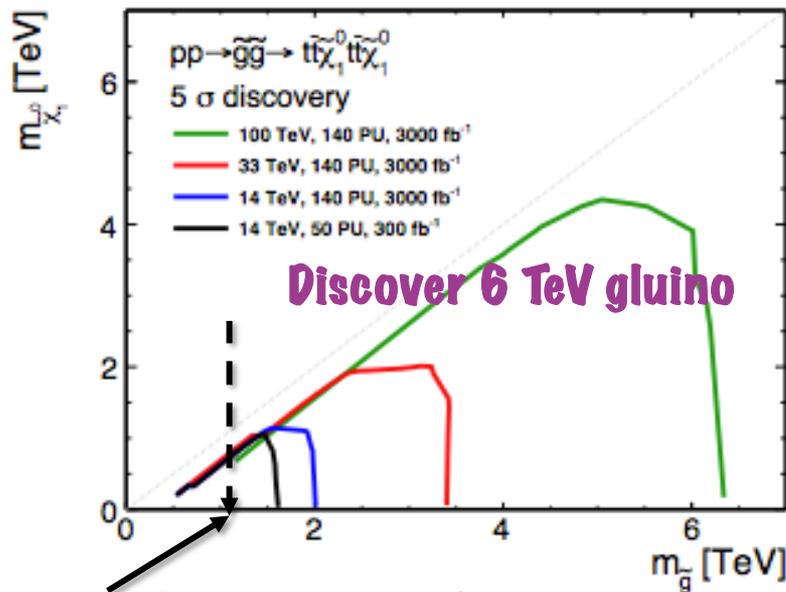
20% systematic uncertainty, no pileup

Glino-Neutralino Signature – heavy flavor

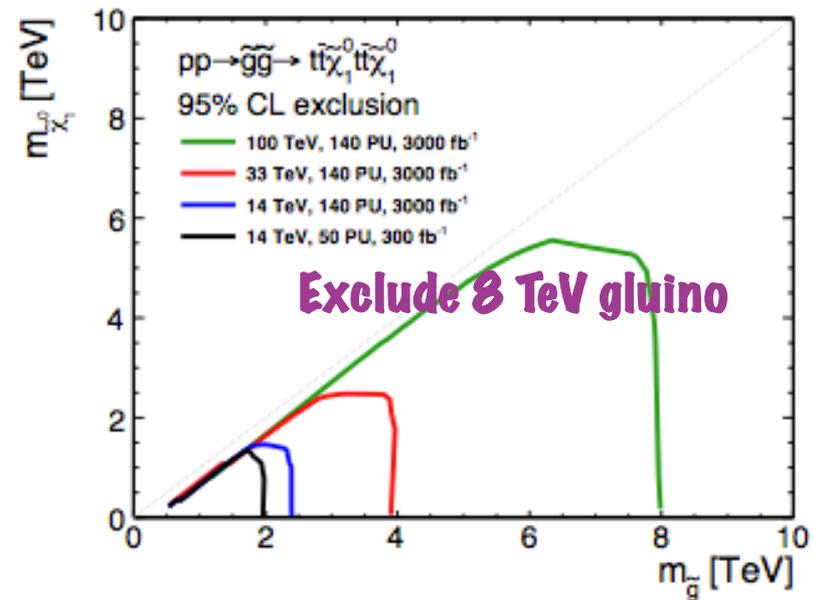
- Search for **gluinos** with **Same Sign 2 lepton**, **2b-jets**, **large missing transverse momentum**
- Signal to BG discrimination based: **MET, HT, meff, mT2**
- **Discover (Exclude) 6 (8) TeV gluino**
- Increasing the center-of-mass energy has a tremendous impact on the experimentally available parameter space (~ 3 x beyond 14 TeV @100 TeV)



arXiv:
1311.6480



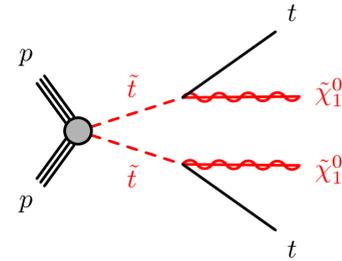
LHC 13 TeV limit ~ 1.2 TeV



20% systematic uncertainty, no pileup

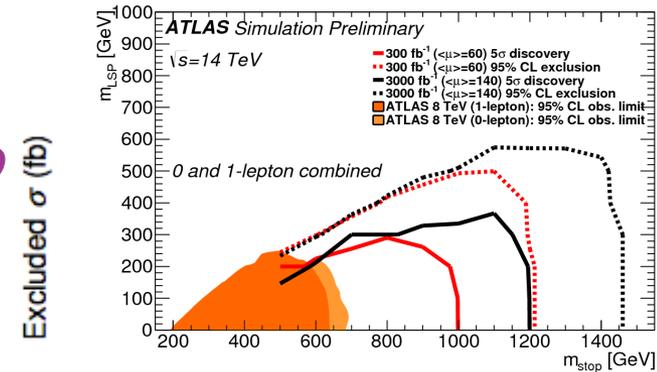
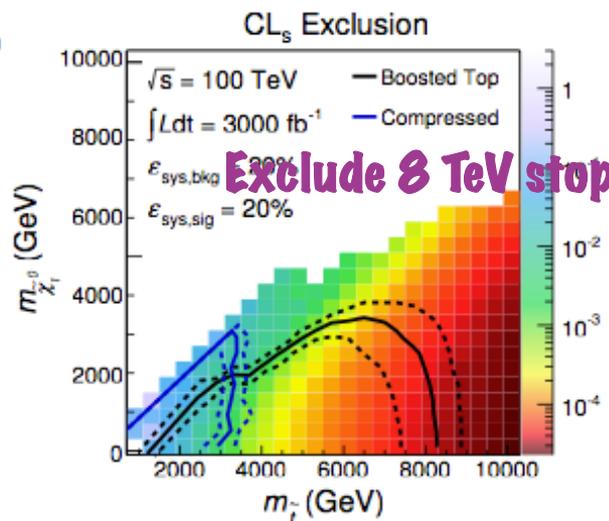
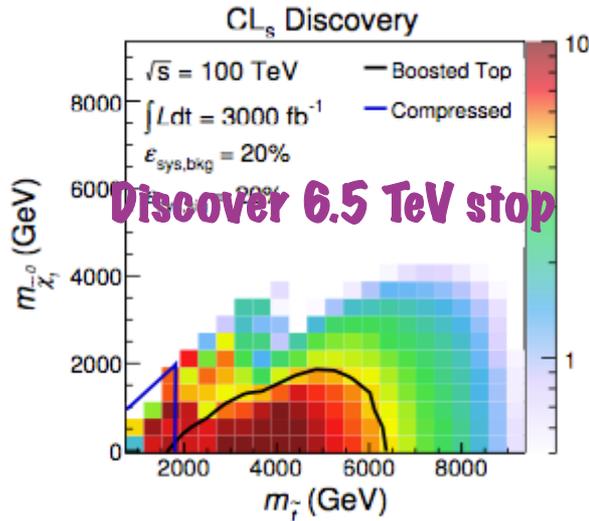
Stop-Neutralino Signature

- Search for **stop** with on-shell top decay @ 100 TeV
- Tops are very boosted at 100 TeV, the search strategy with isolated leptons, b-tags or top-tagging are sensitive to detector granularity/performance, pileup conditions etc. → So use simple handles **with hard jets, MET and muon-in-jet**
- Two scenarios with high mass stop and compressed region designed
- Discover (Exclude) 6.5 (8) TeV stop @100TeV



arXiv:
1406.4512

**LHC 14:
Exclude 1.4 TeV stop**

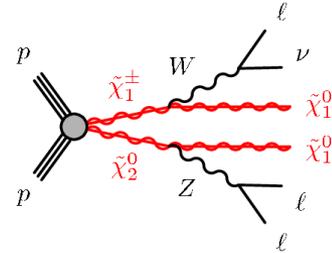


ATL-PHYS-PUB-2014-010

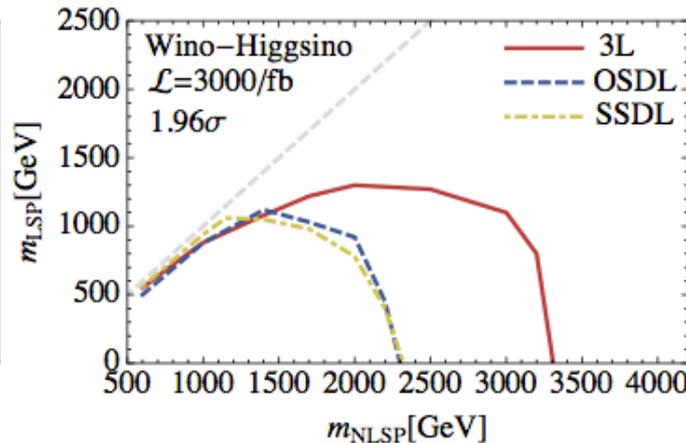
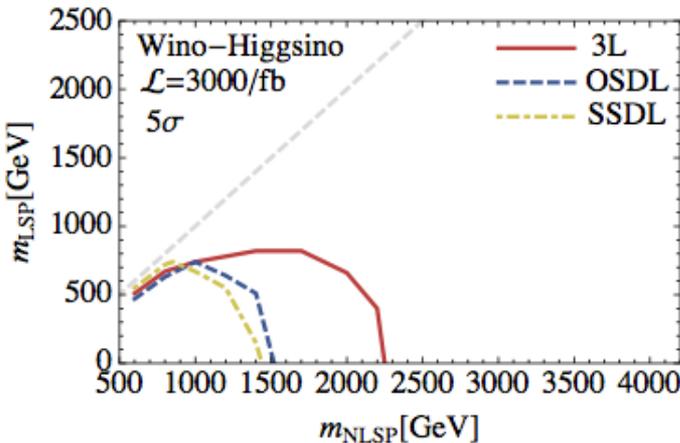
LHC 8: ~ 700 GeV 24

EWK Signature

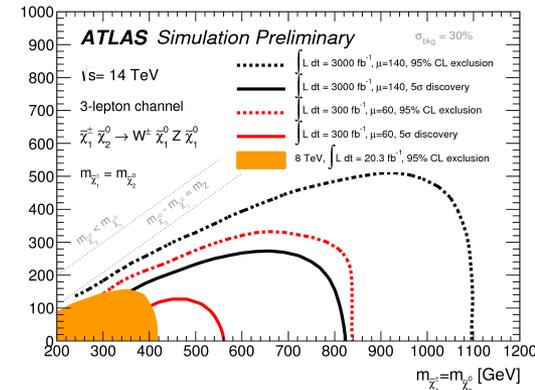
- Increasing bounds on colored SUSY particles, maybe only **electroweakinos** in the low energy spectrum. LHC has limited reach for direct produced EWK particles
- Potential search for **electroweakinos** with **multi-lepton signatures: 3L || OS2L || SS2L @100 TeV**
- Discover (Exclude) 2.1 (3.2) TeV electroweakinos for wino NLSP



arXiv:
1410.6287



LHC 14:
Exclude 1.1 TeV stop



ATL-PHYS-PUB-2013-011

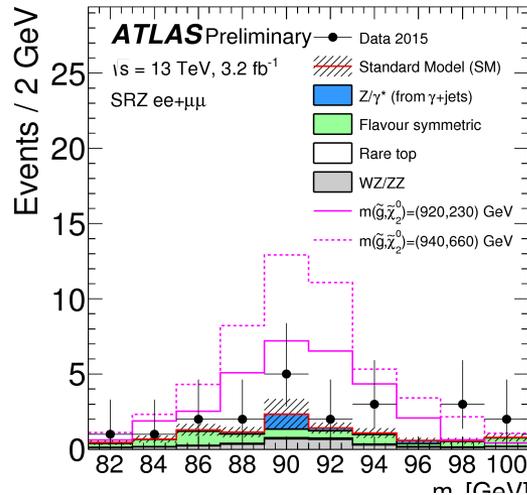
LHC 8: ~ 400 GeV 25

Summary

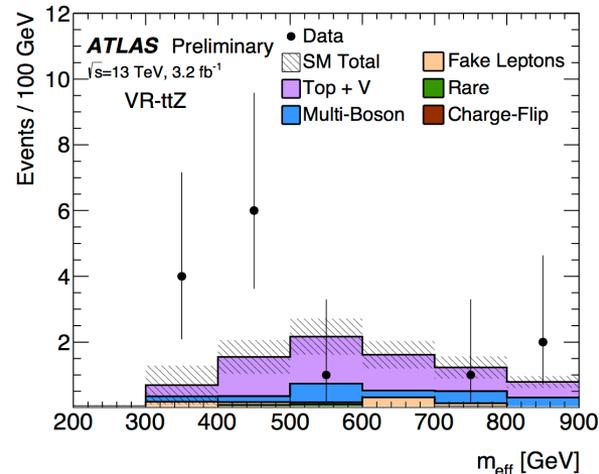
- [LHC 8 TeV $\sim 20 \text{ fb}^{-1}$] In canonical scenarios, sensitivity is achieved to **$\sim 1.2 \text{ TeV}$ gluinos**, **$\sim 700 \text{ GeV}$ stops** and **$\sim 400 \text{ GeV}$ EWK-inos**
 - [LHC 14 TeV $\sim 3000 \text{ fb}^{-1}$] Discovery potential up to **2.2 TeV gluinos**, **1.2 TeV stop** and **800 GeV EWK-inos**
 - [100 TeV $\sim 3000 \text{ fb}^{-1}$] Discover (Exclude) **11 (13) TeV gluino**, **6.5 (8) TeV stop**, **2.1 (3.2) TeV EWK-inos**
- [LHC 13 TeV $\sim 3.3 \text{ fb}^{-1}$] some extensions for squark and gluino sensitivity with 2015 RUN2 data, some small excess hints observed but still weak, need more data! Looking forward for 2016 and beyond!

Thanks for your attention!

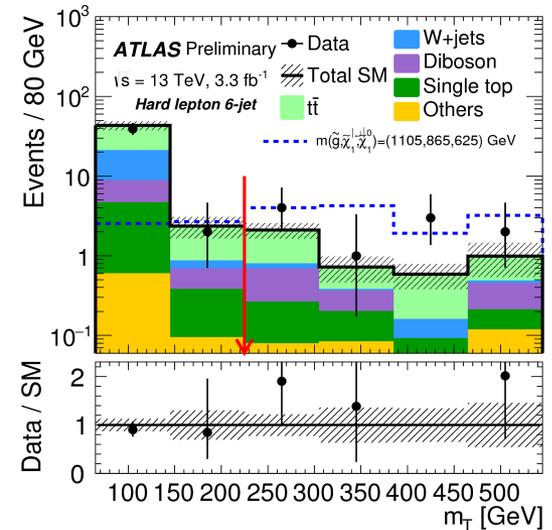
Excess Hints in Run2



Z+MET: a mild excess 2.2σ in 2L (Z+MET) analysis (same SR as run1, where a 3σ excess was found)



SS/3L: an excess in ttZ VR (see 3.5σ excess in $3l+3b$ VR in run1, will revisit in run2)



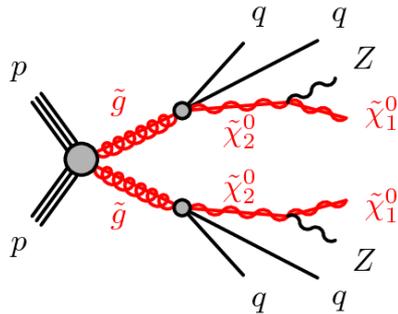
1L: m_T distribution disagrees in 6J SR ($\sim 2\sigma$)

- There are some excess hints in 3 SUSY analyses (**1L**, **SS/3L**, **Z+MET**)
 → Exciting prospects for 2016!

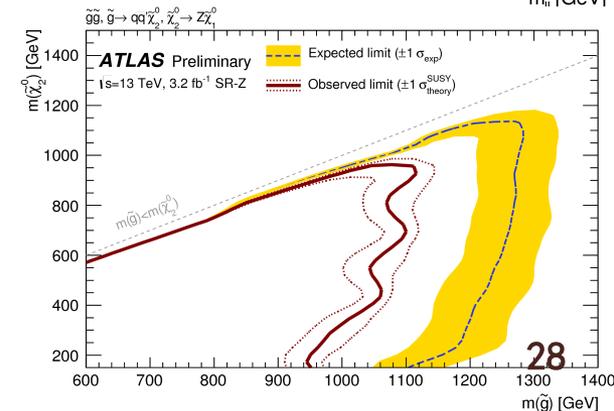
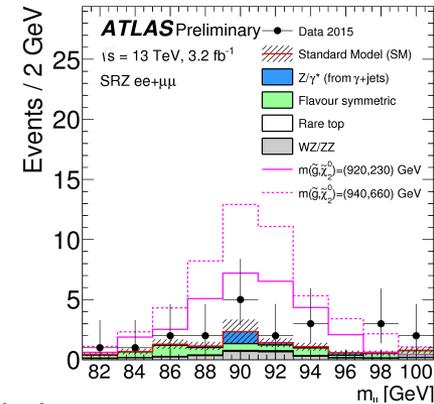
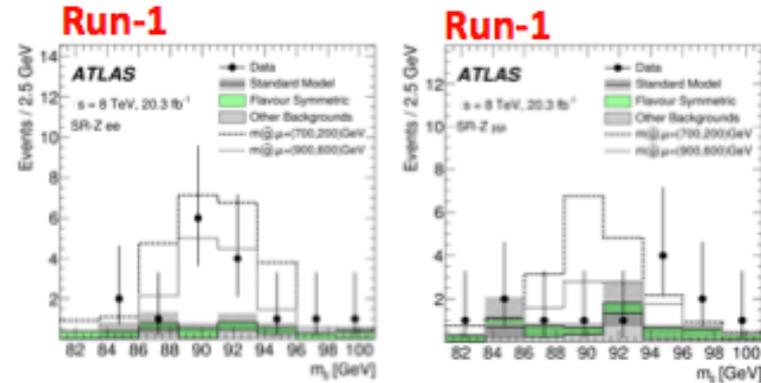
Strong Production: Z(II)+MET

ATLAS-CONF-2015-082

- Search for gluinos with a Z + jets + MET signature



- There is an excess (3σ) at ATLAS Run1 (not as CMS): obs. 29, exp. 10.8 ± 2.2 ()
- Check it with Run2 using run1-like SR: Z (II), 2jets, MET > 225 GeV, HT > 600 GeV
- a mild excess seen in Run2: obs. 21, exp. 10.4 ± 2.4 (2.2σ in intermediate MET)
- Excludes gluino masses up to 1.1 TeV



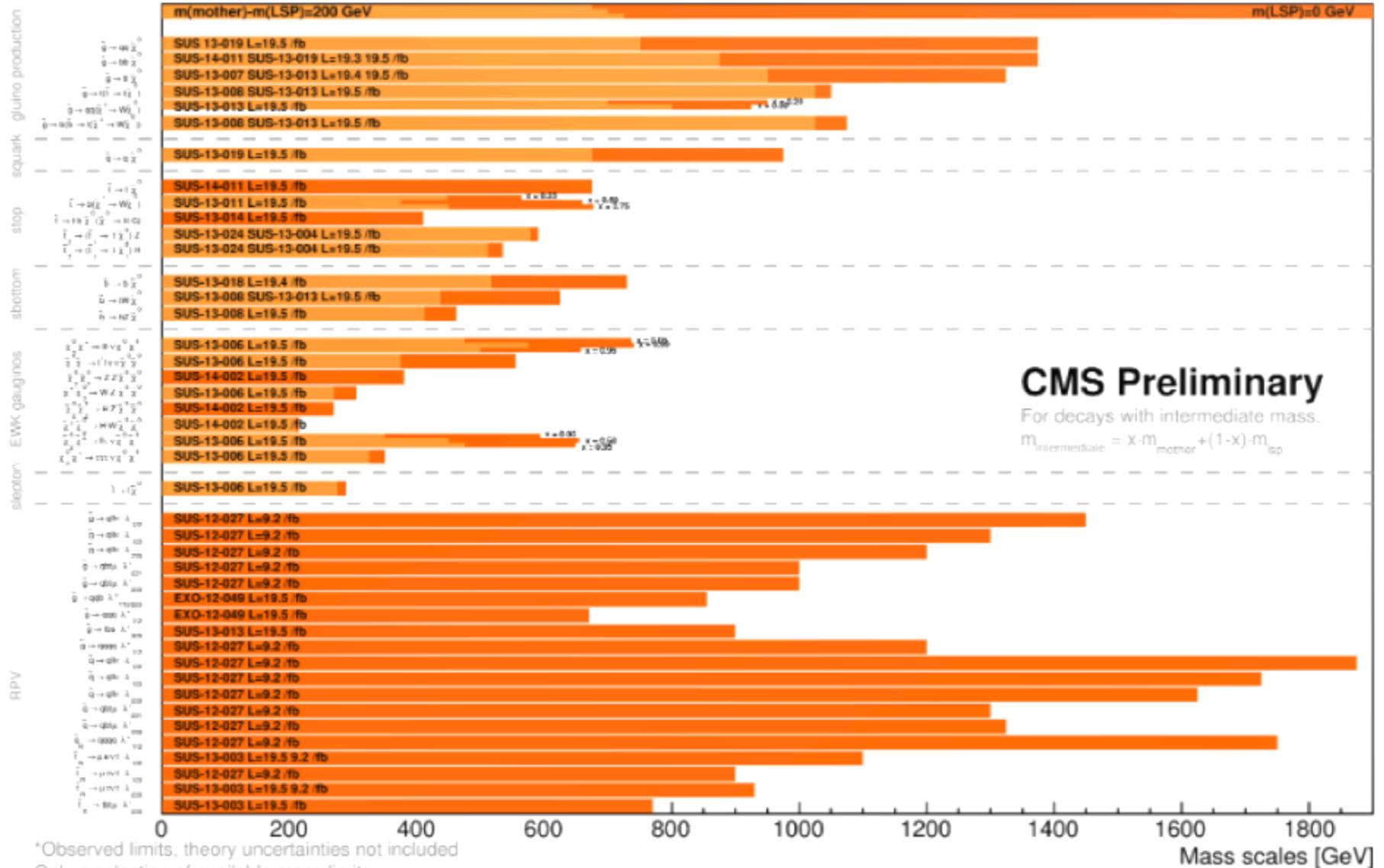
Model	e, μ, τ, γ	Jets	E_T^{miss}	$\int \mathcal{L} dt [\text{fb}^{-1}]$	Mass limit	$\sqrt{s} = 7 \text{ TeV}$	$\sqrt{s} = 8 \text{ TeV}$	Reference		
Inclusive Searches	MSUGRA/CMSSM	0-3 e, μ /1-2 τ	2-10 jets/3 b	Yes	20.3	\tilde{q}, \tilde{g}	1.8 TeV	$m(\tilde{q})=m(\tilde{g})$	1507.05525	
	$\tilde{q}\tilde{q}, \tilde{q} \rightarrow q\tilde{\chi}_1^0$	0	2-6 jets	Yes	20.3	\tilde{q}	850 GeV	$m(\tilde{\chi}_1^0)=0 \text{ GeV}, m(1^{\text{st}} \text{ gen. } \tilde{q})=m(2^{\text{nd}} \text{ gen. } \tilde{q})$	1405.7875	
	$\tilde{q}\tilde{q}, \tilde{q} \rightarrow q\tilde{\chi}_1^0$ (compressed)	mono-jet	1-3 jets	Yes	20.3	\tilde{q}	100-440 GeV	$m(\tilde{q})-m(\tilde{\chi}_1^0) < 10 \text{ GeV}$	1507.05525	
	$\tilde{q}\tilde{q}, \tilde{q} \rightarrow q(\ell\ell/\ell\nu/\nu\nu)\tilde{\chi}_1^0$	2 e, μ (off-Z)	2 jets	Yes	20.3	\tilde{q}	780 GeV	$m(\tilde{\chi}_1^0)=0 \text{ GeV}$	1503.03290	
	$\tilde{g}\tilde{g}, \tilde{g} \rightarrow q\tilde{q}\tilde{\chi}_1^0$	0	2-6 jets	Yes	20.3	\tilde{g}	1.33 TeV	$m(\tilde{\chi}_1^0)=0 \text{ GeV}$	1405.7875	
	$\tilde{g}\tilde{g}, \tilde{g} \rightarrow qq\tilde{\chi}_1^0$	0-1 e, μ	2-6 jets	Yes	20	\tilde{g}	1.26 TeV	$m(\tilde{\chi}_1^0) < 300 \text{ GeV}, m(\tilde{\chi}^\pm)=0.5(m(\tilde{\chi}_1^0)+m(\tilde{g}))$	1507.05525	
	$\tilde{g}\tilde{g}, \tilde{g} \rightarrow qq(\ell\ell/\ell\nu/\nu\nu)\tilde{\chi}_1^0$	2 e, μ	0-3 jets	-	20	\tilde{g}	1.32 TeV	$m(\tilde{\chi}_1^0)=0 \text{ GeV}$	1501.03555	
	GMSB ($\tilde{\ell}$ NLSP)	1-2 τ + 0-1 ℓ	0-2 jets	Yes	20.3	\tilde{g}	1.6 TeV	$\tan\beta > 20$	1407.0603	
	GGM (bino NLSP)	2 γ	-	Yes	20.3	\tilde{g}	1.29 TeV	$c\tau(\text{NLSP}) < 0.1 \text{ mm}$	1507.05493	
	GGM (higgsino-bino NLSP)	γ	1 b	Yes	20.3	\tilde{g}	1.3 TeV	$m(\tilde{\chi}_1^0) < 900 \text{ GeV}, c\tau(\text{NLSP}) < 0.1 \text{ mm}, \mu < 0$	1507.05493	
GGM (higgsino-bino NLSP)	γ	2 jets	Yes	20.3	\tilde{g}	1.25 TeV	$m(\tilde{\chi}_1^0) < 850 \text{ GeV}, c\tau(\text{NLSP}) < 0.1 \text{ mm}, \mu > 0$	1507.05493		
GGM (higgsino NLSP)	2 e, μ (Z)	2 jets	Yes	20.3	\tilde{g}	850 GeV	$m(\text{NLSP}) > 430 \text{ GeV}$	1503.03290		
Gravitino LSP	0	mono-jet	Yes	20.3	$F^{1/2}$ scale	865 GeV	$m(\tilde{G}) > 1.8 \times 10^{-4} \text{ eV}, m(\tilde{g})=m(\tilde{q})=1.5 \text{ TeV}$	1502.01518		
3 rd gen. \tilde{g} med.	$\tilde{g}\tilde{g}, \tilde{g} \rightarrow b\tilde{b}\tilde{\chi}_1^0$	0	3 b	Yes	20.1	\tilde{g}	1.25 TeV	$m(\tilde{\chi}_1^0) < 400 \text{ GeV}$	1407.0600	
	$\tilde{g}\tilde{g}, \tilde{g} \rightarrow t\tilde{t}\tilde{\chi}_1^0$	0	7-10 jets	Yes	20.3	\tilde{g}	1.1 TeV	$m(\tilde{\chi}_1^0) < 350 \text{ GeV}$	1308.1841	
3 rd gen. squarks direct production	$\tilde{g}\tilde{g}, \tilde{g} \rightarrow t\tilde{t}\tilde{\chi}_1^0$	0-1 e, μ	0	Yes	20.1	\tilde{g}	1.4 TeV	$m(\tilde{\chi}_1^0) < 300 \text{ GeV}$	1407.0600	
	$\tilde{g}\tilde{g}, \tilde{g} \rightarrow b\tilde{b}\tilde{\chi}_1^0$	0-1 e, μ	3 b	Yes	20.1	\tilde{g}	1.3 TeV	$m(\tilde{\chi}_1^0) < 300 \text{ GeV}$	1407.0600	
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow t\tilde{\chi}_1^0$	0	1 b	Yes	20.3	\tilde{t}_1	275-440 GeV	$m(\tilde{\chi}_1^0) = 2 m(\tilde{\chi}_1^0)$	1404.2500	
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow b\tilde{\chi}_1^+$	1-2 e, μ	1-2 b	Yes	4.7/20.3	\tilde{t}_1	110-167 GeV	$m(\tilde{\chi}_1^+) = 2m(\tilde{\chi}_1^0), m(\tilde{\chi}_1^0)=55 \text{ GeV}$	1209.2102, 1407.0583	
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow Wb\tilde{\chi}_1^0$ or $\tilde{\chi}_1^0$	0-2 e, μ	0-2 jets/1-2 b	Yes	20.3	\tilde{t}_1	90-191 GeV	$m(\tilde{\chi}_1^0)=1 \text{ GeV}$	1506.08616	
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow c\tilde{\chi}_1^0$	0	mono-jet/c-tag	Yes	20.3	\tilde{t}_1	90-240 GeV	$m(\tilde{t}_1)-m(\tilde{\chi}_1^0) < 85 \text{ GeV}$	1407.0608	
	$\tilde{t}_1\tilde{t}_1$ (natural GMSB)	2 e, μ (Z)	1 b	Yes	20.3	\tilde{t}_1	150-580 GeV	$m(\tilde{\chi}_1^0) > 150 \text{ GeV}$	1403.5222	
	$\tilde{t}_2\tilde{t}_2, \tilde{t}_2 \rightarrow \tilde{t}_1 + Z$	3 e, μ (Z)	1 b	Yes	20.3	\tilde{t}_2	290-600 GeV	$m(\tilde{\chi}_1^0) < 200 \text{ GeV}$	1403.5222	
	EW direct	$\tilde{\ell}_{L,R}\tilde{\ell}_{L,R}, \tilde{\ell} \rightarrow \ell\tilde{\chi}_1^0$	2 e, μ	0	Yes	20.3	$\tilde{\ell}$	90-325 GeV	$m(\tilde{\chi}_1^0)=0 \text{ GeV}$	1403.5294
		$\tilde{\chi}_1^+\tilde{\chi}_1^-, \tilde{\chi}_1^+ \rightarrow \ell\nu(\ell\bar{\nu})$	2 e, μ	0	Yes	20.3	$\tilde{\chi}_1^\pm$	140-465 GeV	$m(\tilde{\chi}_1^0)=0 \text{ GeV}, m(\tilde{\ell}, \tilde{\nu})=0.5(m(\tilde{\chi}_1^+)+m(\tilde{\chi}_1^-))$	1403.5294
$\tilde{\chi}_1^+\tilde{\chi}_1^-, \tilde{\chi}_1^+ \rightarrow \tilde{\nu}\nu(\tilde{\nu}\bar{\nu})$		2 τ	0	Yes	20.3	$\tilde{\chi}_1^\pm$	100-350 GeV	$m(\tilde{\chi}_1^0)=0 \text{ GeV}, m(\tilde{\tau}, \tilde{\nu})=0.5(m(\tilde{\chi}_1^+)+m(\tilde{\chi}_1^-))$	1407.0350	
$\tilde{\chi}_1^+\tilde{\chi}_2^0 \rightarrow \tilde{L}_L\tilde{\nu}_L^0\ell(\tilde{\nu}\nu), \ell\tilde{\nu}_L^0\ell(\tilde{\nu}\nu)$		3 e, μ	0	Yes	20.3	$\tilde{\chi}_1^+, \tilde{\chi}_2^0$	700 GeV	$m(\tilde{\chi}_1^+)=m(\tilde{\chi}_2^0), m(\tilde{\chi}_1^0)=0, m(\tilde{\ell}, \tilde{\nu})=0.5(m(\tilde{\chi}_1^+)+m(\tilde{\chi}_1^-))$	1402.7029	
$\tilde{\chi}_1^+\tilde{\chi}_2^0 \rightarrow W\tilde{\chi}_1^0 Z\tilde{\chi}_1^0$		2-3 e, μ	0-2 jets	Yes	20.3	$\tilde{\chi}_1^+, \tilde{\chi}_2^0$	420 GeV	$m(\tilde{\chi}_1^+)=m(\tilde{\chi}_2^0), m(\tilde{\chi}_1^0)=0, \text{ sleptons decoupled}$	1403.5294, 1402.7029	
$\tilde{\chi}_1^+\tilde{\chi}_2^0 \rightarrow W\tilde{\chi}_1^0 h\tilde{\chi}_1^0, h \rightarrow b\tilde{b}/WW/\tau\tau/\gamma\gamma$		e, μ, γ	0-2 b	Yes	20.3	$\tilde{\chi}_1^+, \tilde{\chi}_2^0$	250 GeV	$m(\tilde{\chi}_1^+)=m(\tilde{\chi}_2^0), m(\tilde{\chi}_1^0)=0, \text{ sleptons decoupled}$	1501.07110	
$\tilde{\chi}_2^0\tilde{\chi}_3^0, \tilde{\chi}_2^0\tilde{\chi}_3^0 \rightarrow \tilde{\ell}_R\ell$		4 e, μ	0	Yes	20.3	$\tilde{\chi}_2^0, \tilde{\chi}_3^0$	620 GeV	$m(\tilde{\chi}_2^0)=m(\tilde{\chi}_3^0), m(\tilde{\chi}_1^0)=0, m(\tilde{\ell}, \tilde{\nu})=0.5(m(\tilde{\chi}_2^0)+m(\tilde{\chi}_1^0))$	1405.5086	
GGM (wino NLSP) weak prod.		1 $e, \mu + \gamma$	-	Yes	20.3	\tilde{W}	124-361 GeV	$c\tau < 1 \text{ mm}$	1507.05493	
Long-lived particles		Direct $\tilde{\chi}_1^+\tilde{\chi}_1^-$ prod., long-lived $\tilde{\chi}_1^\pm$	Disapp. trk	1 jet	Yes	20.3	$\tilde{\chi}_1^\pm$	270 GeV	$m(\tilde{\chi}_1^+)-m(\tilde{\chi}_1^0) \sim 160 \text{ MeV}, \tau(\tilde{\chi}_1^\pm)=0.2 \text{ ns}$	1310.3675
		Direct $\tilde{\chi}_1^+\tilde{\chi}_1^-$ prod., long-lived $\tilde{\chi}_1^\pm$	dE/dx trk	-	Yes	18.4	$\tilde{\chi}_1^\pm$	482 GeV	$m(\tilde{\chi}_1^+)-m(\tilde{\chi}_1^0) \sim 160 \text{ MeV}, \tau(\tilde{\chi}_1^\pm) < 15 \text{ ns}$	1506.05332
	Stable, stopped \tilde{g} R-hadron	0	1-5 jets	Yes	27.9	\tilde{g}	832 GeV	$m(\tilde{\chi}_1^0)=100 \text{ GeV}, 10 \mu\text{s} < \tau(\tilde{g}) < 1000 \text{ s}$	1310.6584	
	Stable \tilde{g} R-hadron	trk	-	-	19.1	\tilde{g}	1.27 TeV	-	1411.6795	
	GMSB, stable $\tilde{\tau}, \tilde{\chi}_1^0 \rightarrow \tilde{\tau}(\tilde{e}, \tilde{\mu}) + \tau(e, \mu)$	1-2 μ	-	-	19.1	$\tilde{\chi}_1^0$	537 GeV	$10 < \tan\beta < 50$	1411.6795	
	GMSB, $\tilde{\chi}_1^0 \rightarrow \gamma\tilde{G}$, long-lived $\tilde{\chi}_1^0$	2 γ	-	Yes	20.3	$\tilde{\chi}_1^0$	435 GeV	$2 < \tau(\tilde{\chi}_1^0) < 3 \text{ ns}$, SPS8 model	1409.5542	
	$\tilde{g}\tilde{g}, \tilde{\chi}_1^0 \rightarrow ee\nu/\mu\nu/\mu\nu\nu$	displ. $ee/\mu\mu$	-	-	20.3	$\tilde{\chi}_1^0$	1.0 TeV	$7 < c\tau(\tilde{\chi}_1^0) < 740 \text{ mm}, m(\tilde{g})=1.3 \text{ TeV}$	1504.05162	
GGM $\tilde{g}\tilde{g}, \tilde{\chi}_1^0 \rightarrow Z\tilde{G}$	displ. vtx + jets	-	-	20.3	$\tilde{\chi}_1^0$	1.0 TeV	$6 < c\tau(\tilde{\chi}_1^0) < 480 \text{ mm}, m(\tilde{g})=1.1 \text{ TeV}$	1504.05162		
RPV	LFV $pp \rightarrow \tilde{\nu}_\tau + X, \tilde{\nu}_\tau \rightarrow e\mu/\tau/\mu\tau$	$e\mu, e\tau, \mu\tau$	-	-	20.3	$\tilde{\nu}_\tau$	1.7 TeV	$\lambda'_{311}=0.11, \lambda_{132/133/233}=0.07$	1503.04430	
	Bilinear RPV CMSSM	2 e, μ (SS)	0-3 b	Yes	20.3	\tilde{q}, \tilde{g}	1.35 TeV	$m(\tilde{q})=m(\tilde{g}), c\tau_{LSP} < 1 \text{ mm}$	1404.2500	
	$\tilde{\chi}_1^+\tilde{\chi}_1^-, \tilde{\chi}_1^+ \rightarrow W\tilde{\chi}_1^0, \tilde{\chi}_1^0 \rightarrow ee\tilde{\nu}_\mu, e\mu\tilde{\nu}_e$	4 e, μ	-	Yes	20.3	$\tilde{\chi}_1^\pm$	750 GeV	$m(\tilde{\chi}_1^0) > 0.2 \times m(\tilde{\chi}_1^\pm), \lambda_{121} \neq 0$	1405.5086	
	$\tilde{\chi}_1^+\tilde{\chi}_1^-, \tilde{\chi}_1^+ \rightarrow W\tilde{\chi}_1^0, \tilde{\chi}_1^0 \rightarrow \tau\tilde{\nu}_e, e\tau\tilde{\nu}_\tau$	3 $e, \mu + \tau$	-	Yes	20.3	$\tilde{\chi}_1^\pm$	450 GeV	$m(\tilde{\chi}_1^0) > 0.2 \times m(\tilde{\chi}_1^\pm), \lambda_{133} \neq 0$	1405.5086	
	$\tilde{g}\tilde{g}, \tilde{g} \rightarrow qqq$	0	6-7 jets	-	20.3	\tilde{g}	917 GeV	$BR(\tilde{t})=BR(\tilde{b})=BR(\tilde{c})=0\%$	1502.05686	
	$\tilde{g}\tilde{g}, \tilde{g} \rightarrow q\tilde{\chi}_1^0, \tilde{\chi}_1^0 \rightarrow qqq$	0	6-7 jets	-	20.3	\tilde{g}	870 GeV	$m(\tilde{\chi}_1^0)=600 \text{ GeV}$	1502.05686	
	$\tilde{g}\tilde{g}, \tilde{g} \rightarrow \tilde{t}_1 t, \tilde{t}_1 \rightarrow bs$	2 e, μ (SS)	0-3 b	Yes	20.3	\tilde{g}	850 GeV	-	1404.250	
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow bs$	0	2 jets + 2 b	-	20.3	\tilde{t}_1	100-308 GeV	$BR(\tilde{t}_1 \rightarrow b\tilde{e}/\mu) > 20\%$	ATLAS-CONF-2015-026	
$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow b\tilde{\ell}$	2 e, μ	2 b	-	20.3	\tilde{t}_1	0.4-1.0 TeV	-	ATLAS-CONF-2015-015		
Other	Scalar charm, $\tilde{c} \rightarrow c\tilde{\chi}_1^0$	0	2 c	Yes	20.3	\tilde{c}	490 GeV	$m(\tilde{\chi}_1^0) < 200 \text{ GeV}$	1501.01325	

[RUN1] In canonical scenarios, sensitivity is achieved to ~1.2 TeV for EWK-inos in RUN1 gluinos, ~700 GeV stops and ~400 GeV for EWK-inos in RUN1

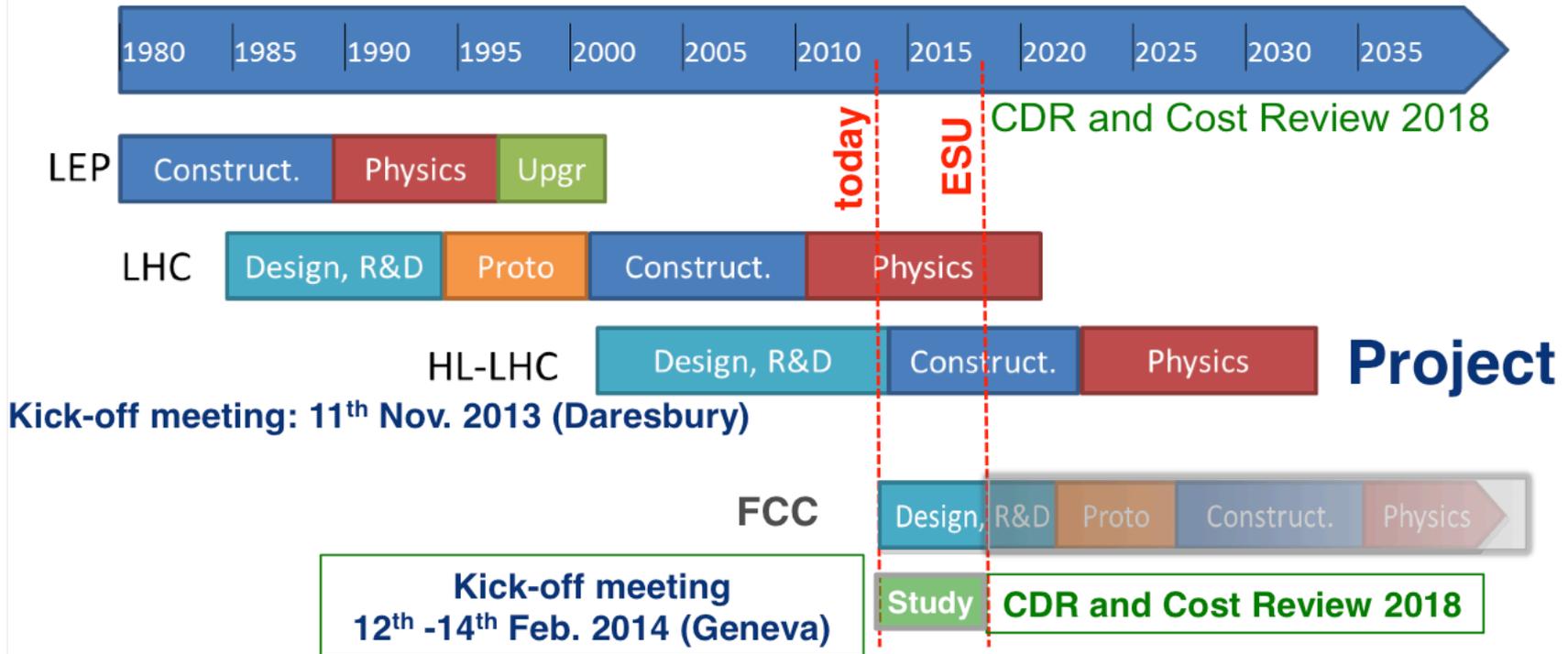
*Only a selection of the available mass limits on new states or phenomena is shown. All limits quoted are observed minus 1 σ theoretical signal cross section uncertainty.

Summary of CMS SUSY Results* in SMS framework

ICHEP 2014



CERN and FCC timelines



Kick-off meeting: 11th Nov. 2013 (Daresbury)

Kick-off meeting
12th -14th Feb. 2014 (Geneva)

Study CDR and Cost Review 2018

- LHC and HL-LHC operation until ~2035
- Must start now developing FCC concepts to be ready in time



SUSY models: good sale in market

□ Simplified Models:

- Not really a model ($Br \sim 100\%$, most masses fixed at high scales)
- Important tool for interpretation

□ Phenomenological models:

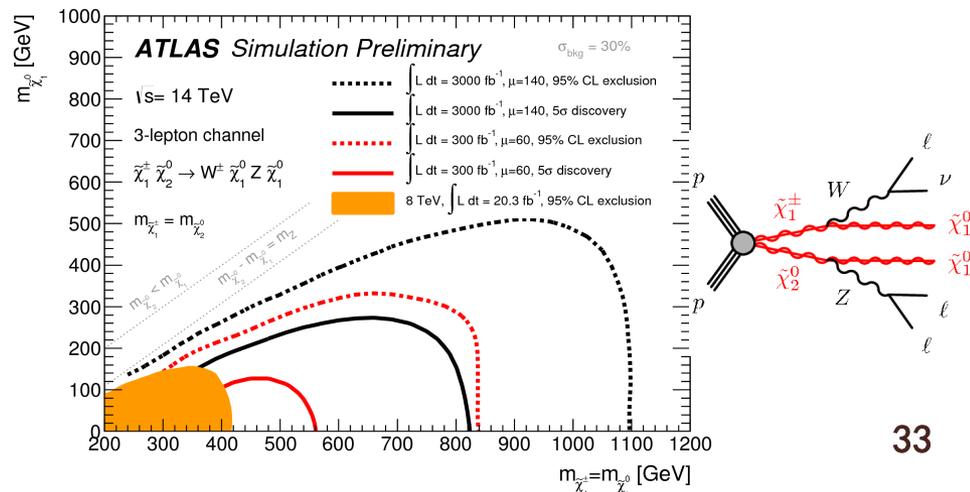
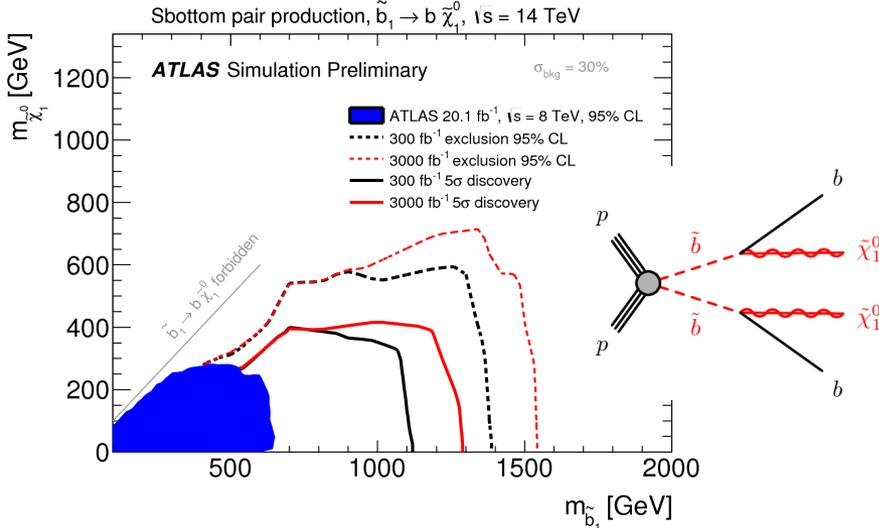
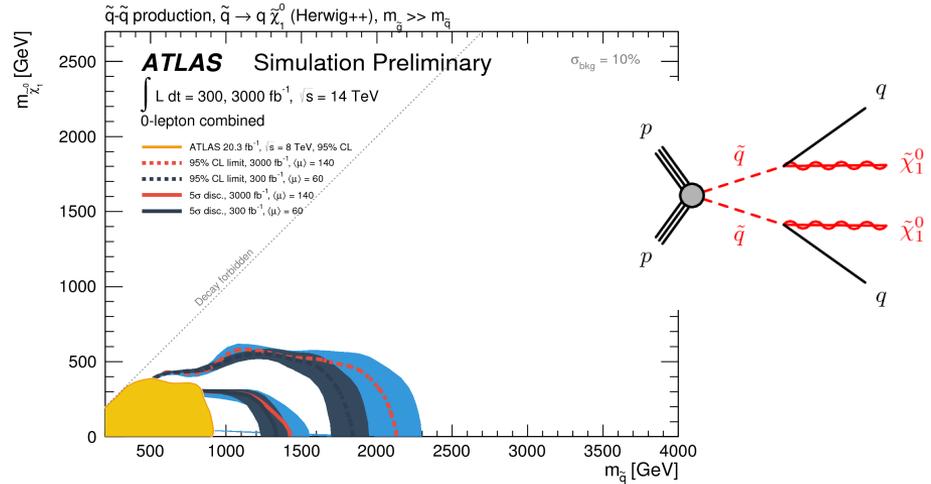
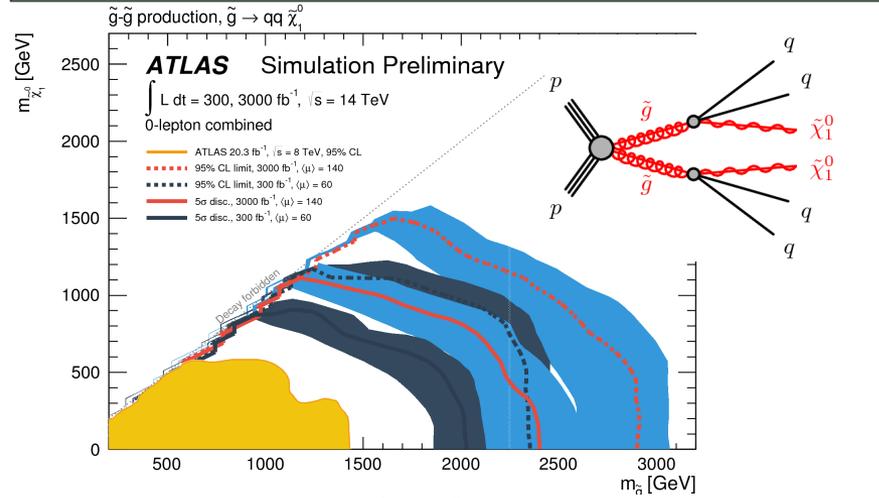
- pMSSM: captures “most” of phenomenologic features of R-parity conserving MSSM
 - 19 free parameters: M_1, M_2, M_3 ; $\tan \beta$, μ and m_A ; 10 sfermion mass parameters; A_t , A_b and A_τ
 - Comprehensive and computationally realistic approximation of the MSSM with neutralino LSP
- GGM (gravitino)

□ Complete SUSY models: mSUGRA, GMSB ...

Long term prospects

ATL-PHYS-PUB-2014-010

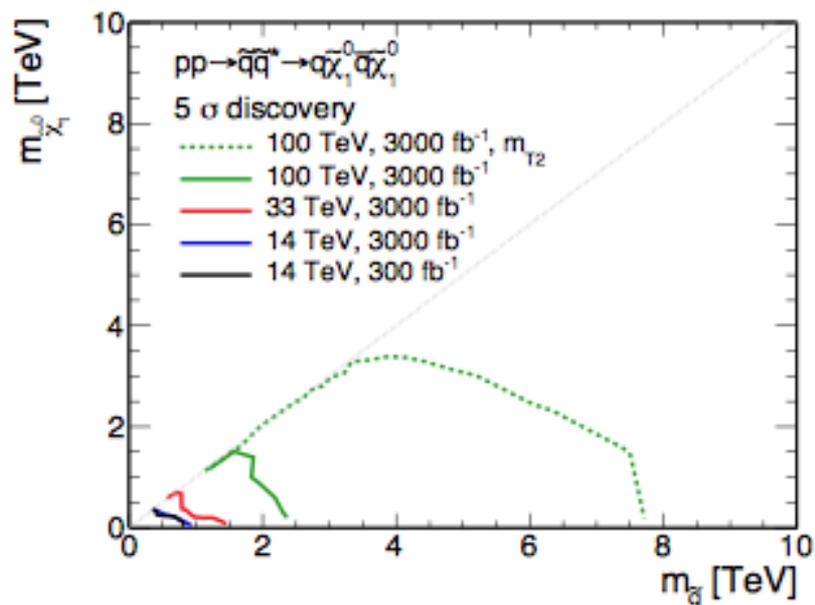
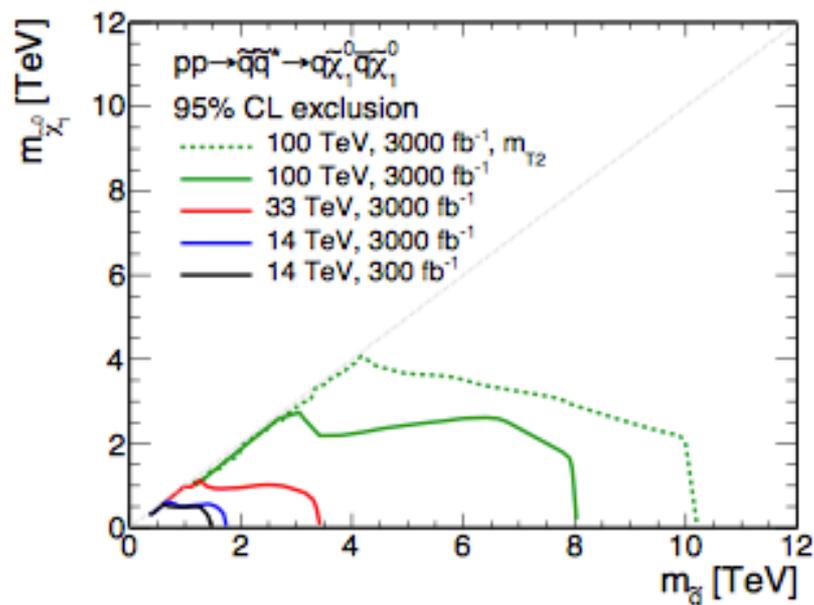
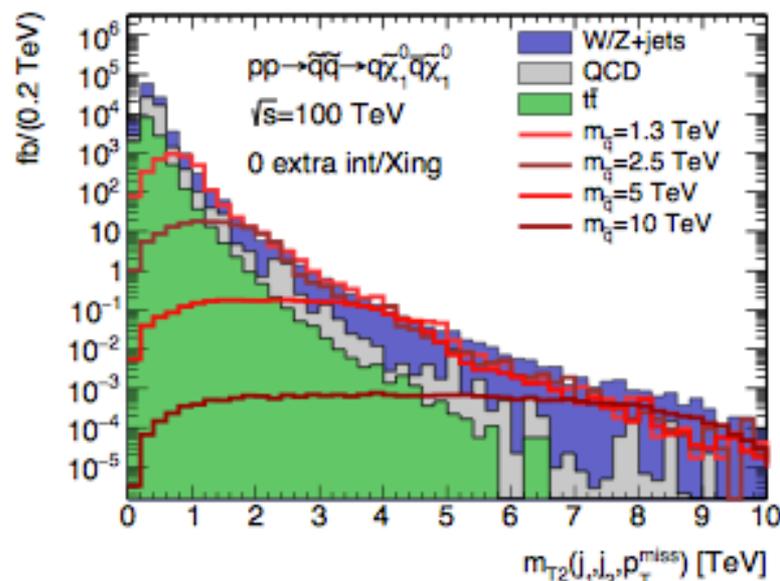
- ATLAS studied long term prospects for the (HL-)LHC with 300, 3000 fb⁻¹@14 TeV
- Discovery potential up to 2.5 TeV gluinos, 1.3 TeV squarks/sbottom and 800 GeV Electroweakinos



$pp \rightarrow \tilde{q}\tilde{q}^* \rightarrow q\tilde{\chi}_1^0\bar{q}\tilde{\chi}_1^0$ – Updates

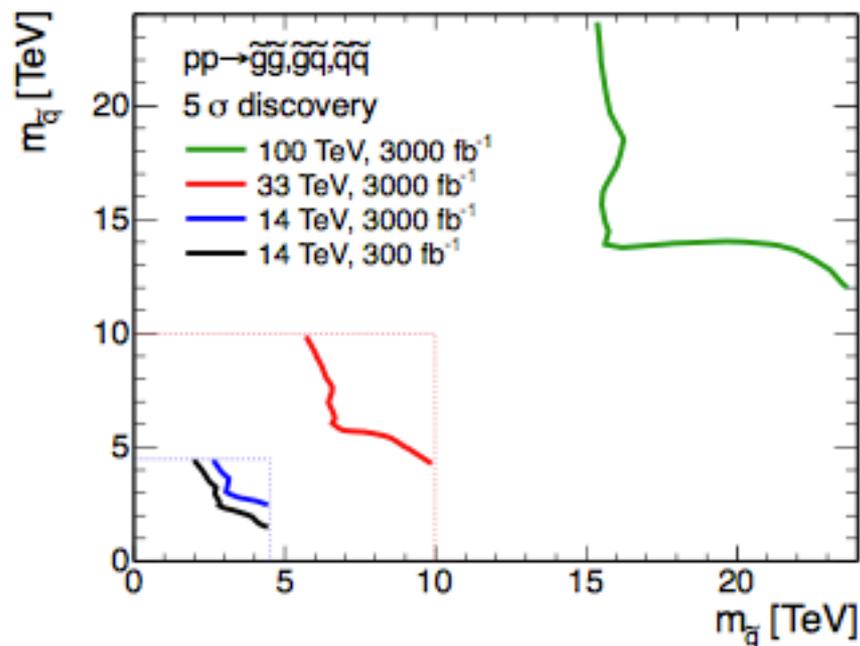
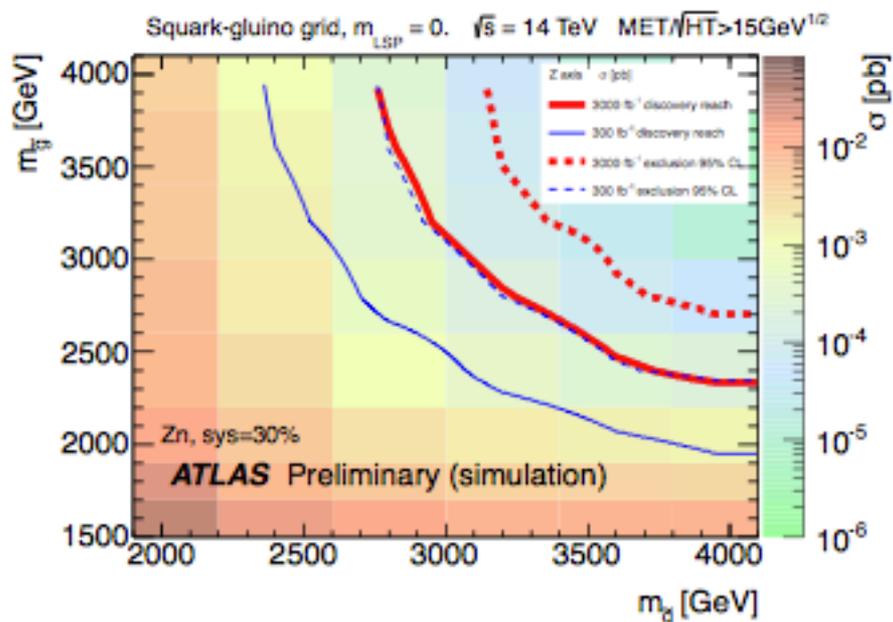
Jets+ E_T^{miss} strategy not optimal for dijet+ E_T^{miss} topology

- Use CMS approach from LHC8 ([PAS-SUS-13-019](#)):
 - Bin in H_T^{jets}
 - Optimize cuts on m_{T2} (leading jets + p_T^{miss})



$pp \rightarrow \tilde{g}\tilde{g}, \tilde{g}\tilde{q}, \tilde{q}\tilde{q}$

Assume massless LSP, vary $m_{\tilde{g}}$ and $m_{\tilde{q}}$:



Multijets+ E_T^{miss} gives good sensitivity, but richer topologies are also likely:

- Naturalness suggests $m_{\tilde{t}} < m_{\tilde{q}}$, so decays via off-shell \tilde{t} are more likely than light-flavor squarks

So... what if $\tilde{g} \rightarrow t\bar{t}\tilde{\chi}_1^0$?

Glino-Neutralino Signature

Impact of Systematic Uncertainties

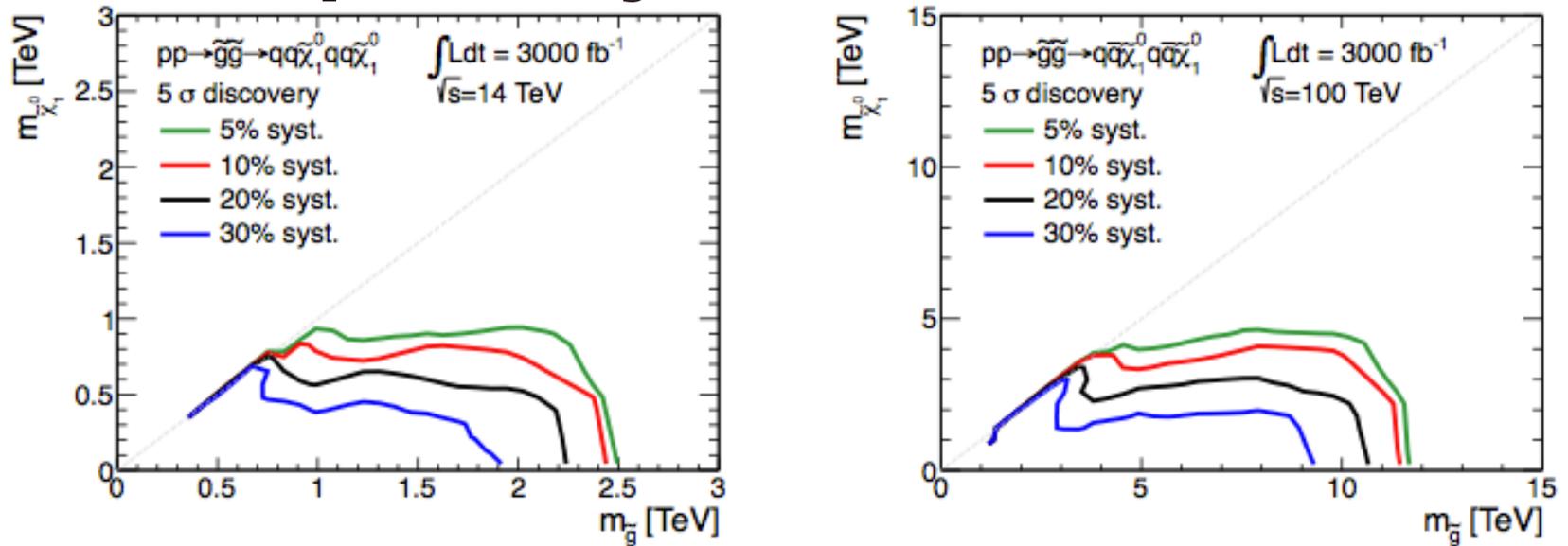


Figure 12: Expected 5σ discovery contours for the $\sqrt{s} = 14$ TeV LHC [left] and a 100 TeV proton collider [right] with 3000 fb^{-1} . The different curves correspond to various assumptions for the systematic uncertainty on the background: 5% [green], 10% [red], 20% [blue], and 30% [black].

- It is likely that the experiments will significantly reduce these uncertainties with larger datasets and an improved understanding of their detectors
- Varying the systematic background uncertainty from 30% to 5%, the discovery reach increases by roughly 600 GeV (3.4 TeV) in $m(\tilde{g})$ at 14 TeV (100 TeV) and the coverage in LSP direction is roughly doubled

Impact of Pileup

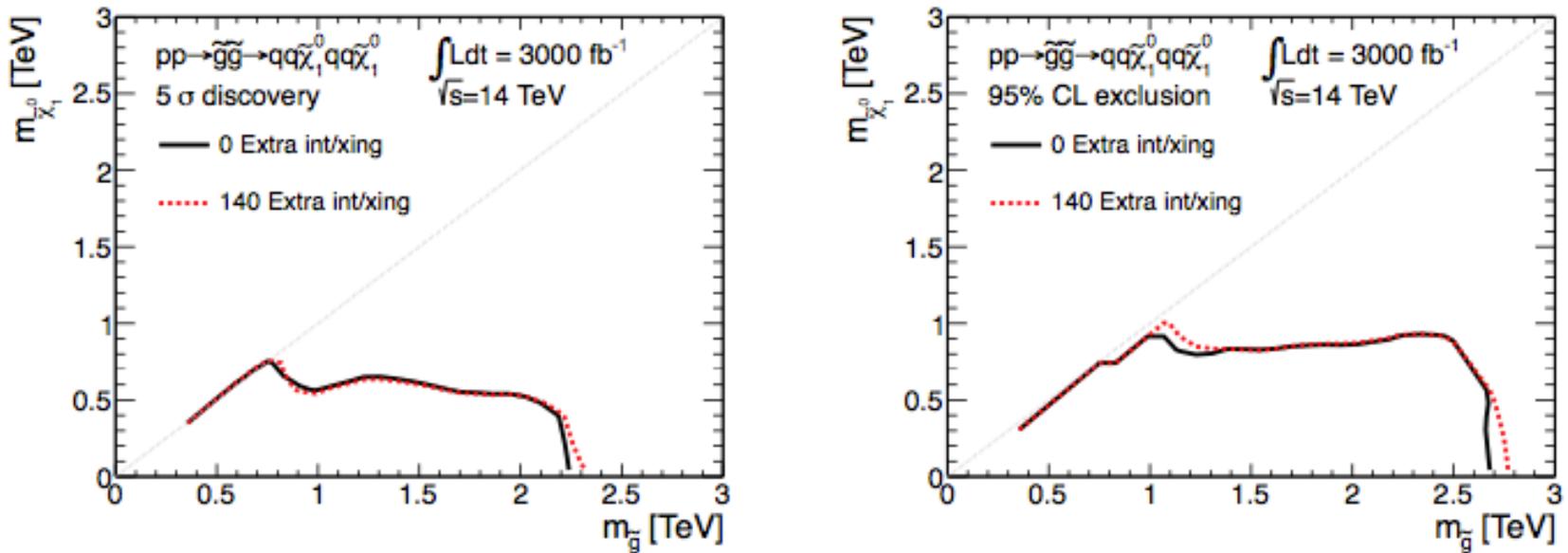
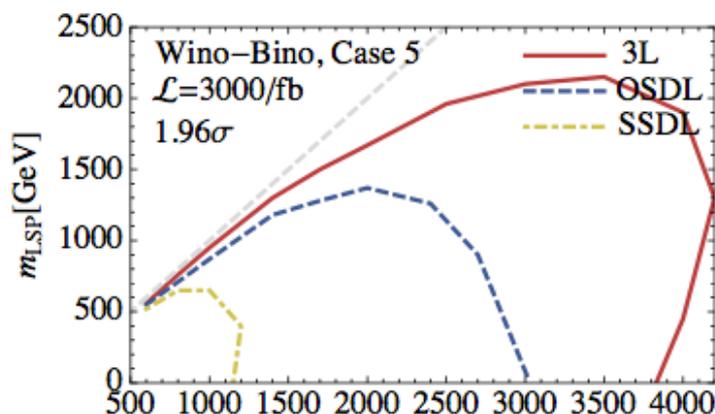
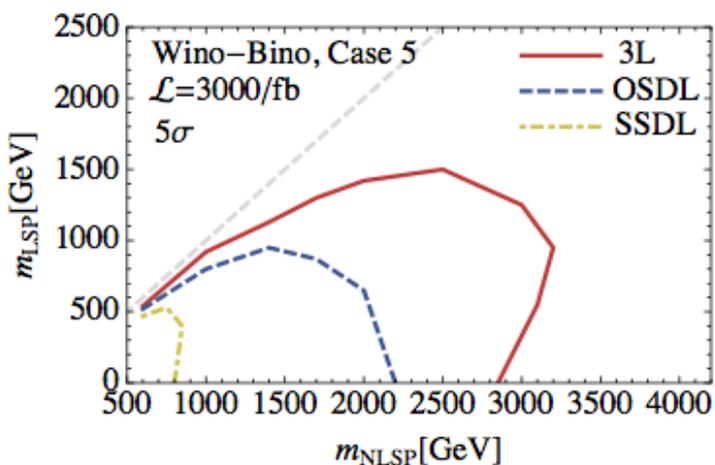
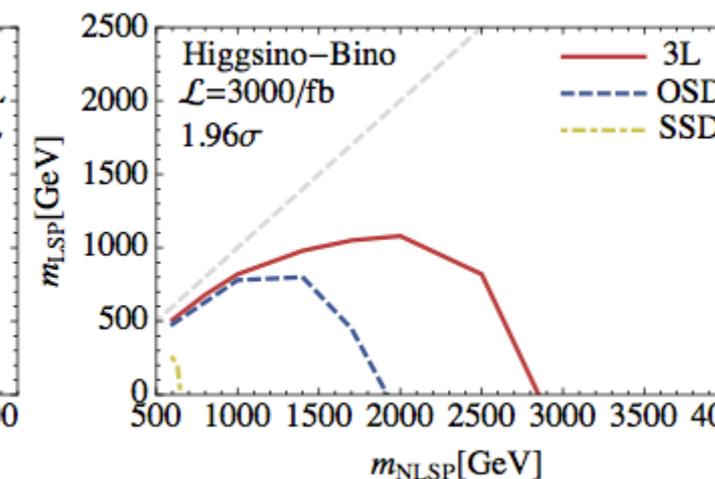
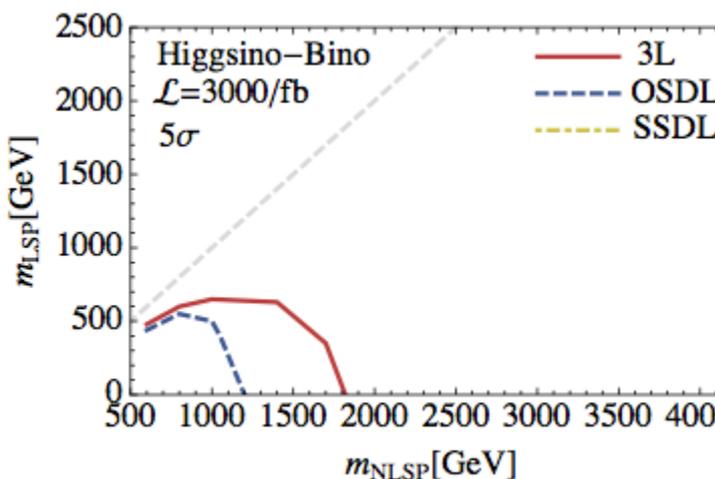
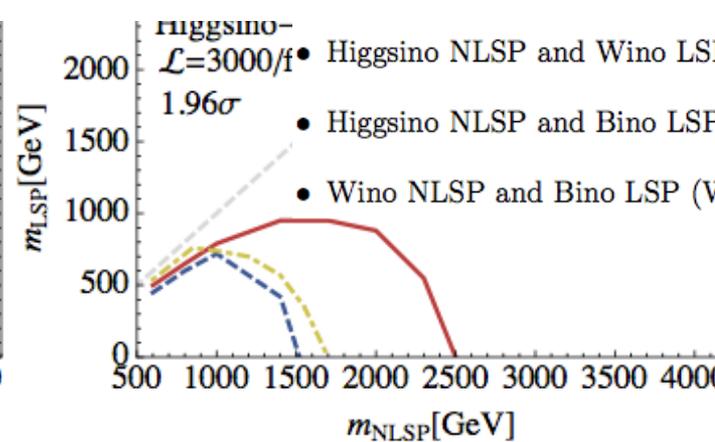
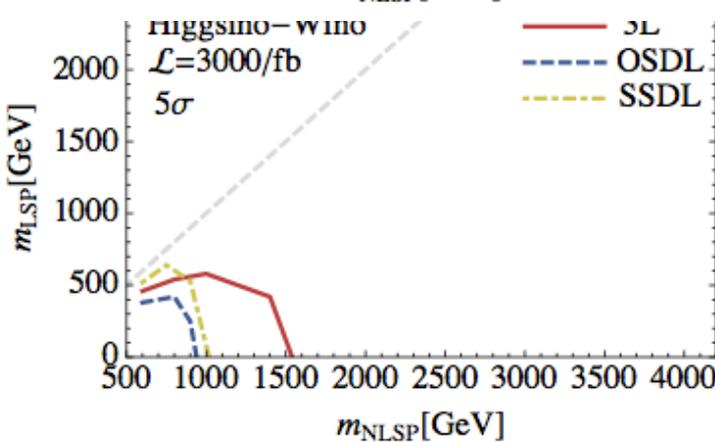


Figure 14: Discovery contours [right] and expected limits [left] for the analyses performed with [red, dotted] and without [black, solid] pileup at the 14 TeV LHC with 3000 fb^{-1} integrated luminosity.

- Compared the results with 140 additional minimum-bias interactions
- The Delphes based Snowmass simulation includes a pileup suppression algorithm that primarily impacts the Emiss resolution (Snowmass detector:ArXiv:1309.1057)
- Given that the HT and ETmiss distributions are effectively unchanged, it is not surprising that the results are very similar with and without pileup



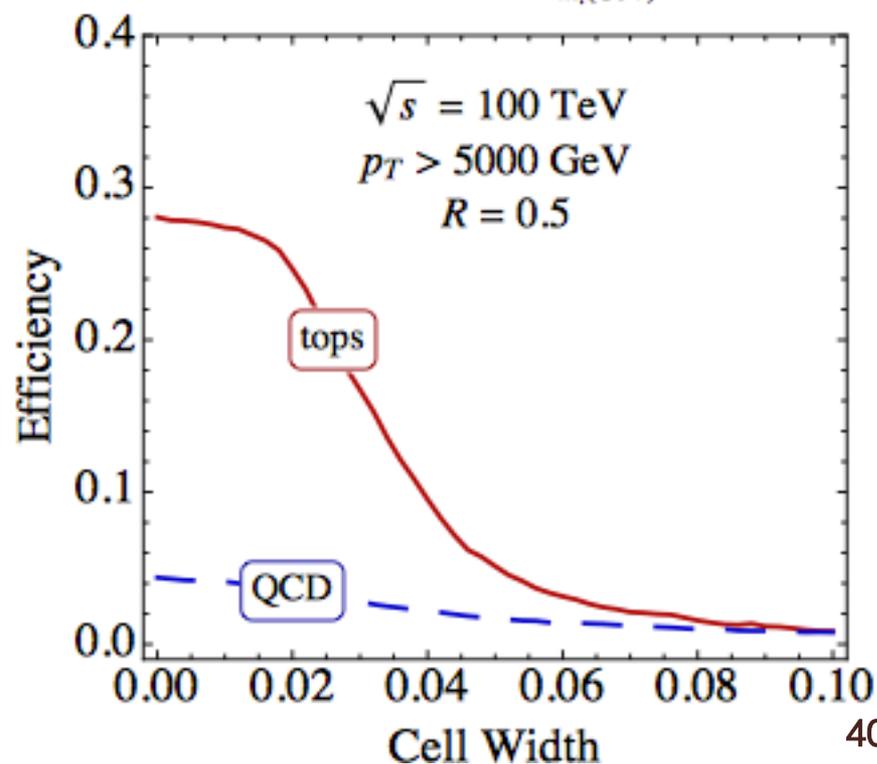
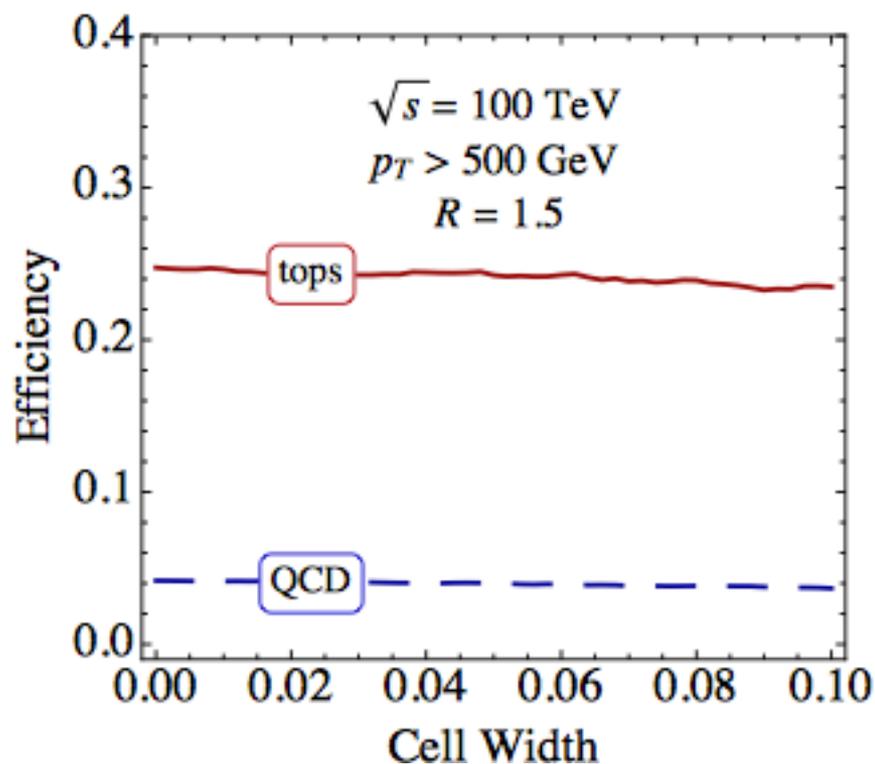
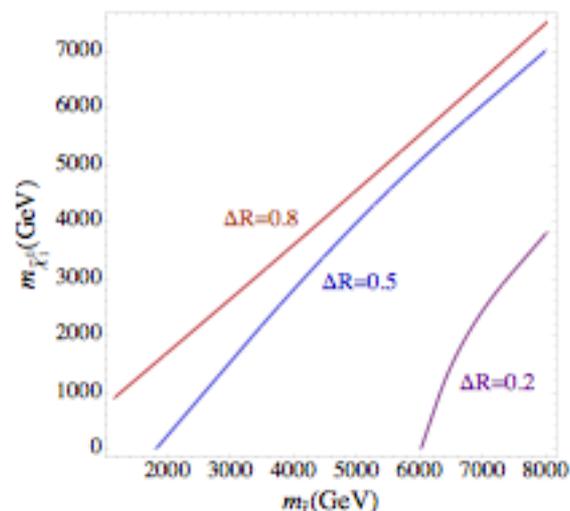
- Wino NLSP and Higgsino LSP (Wino-Higgsino) : $M_1 \gg M_2 > \mu$,
- Higgsino NLSP and Wino LSP (Higgsino-Wino) : $M_1 \gg \mu > M_2$,
- Higgsino NLSP and Bino LSP (Higgsino-Bino) : $M_2 \gg \mu > M_1$,
- Wino NLSP and Bino LSP (Wino-Bino) : $\mu \gg M_2 > M_1$.



Direct Stop Search – Top Tagging?

Top-tagging at 100 TeV?

- Tops are **very** boosted
- Efficiency depends on detector granularity
- Requires lots of assumptions about calorimeters, trackers, etc
- **What's possible with a simpler approach?**

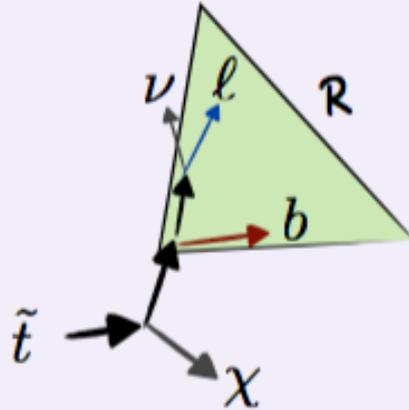


Stop-Neutralino Signature

8 TeV

650 GeV stop

$m_{\tilde{t}} \sim 3m_t$



Typical decay radius $R < 0.2$
(for light neutralino)

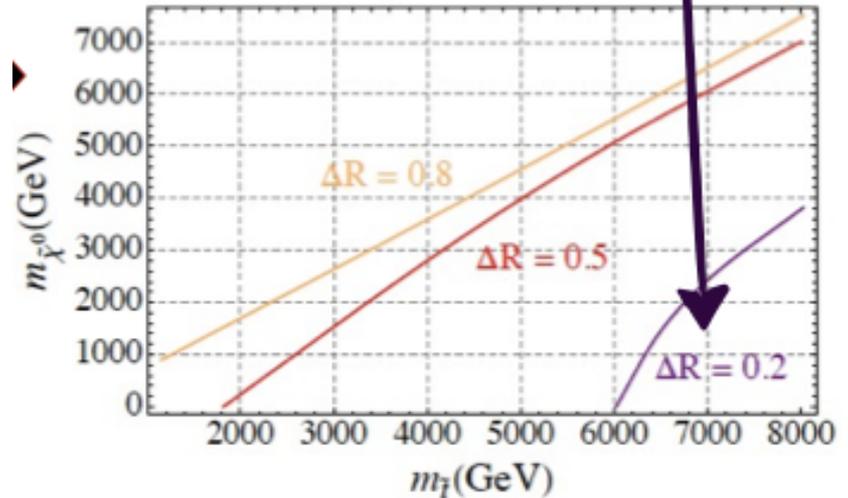
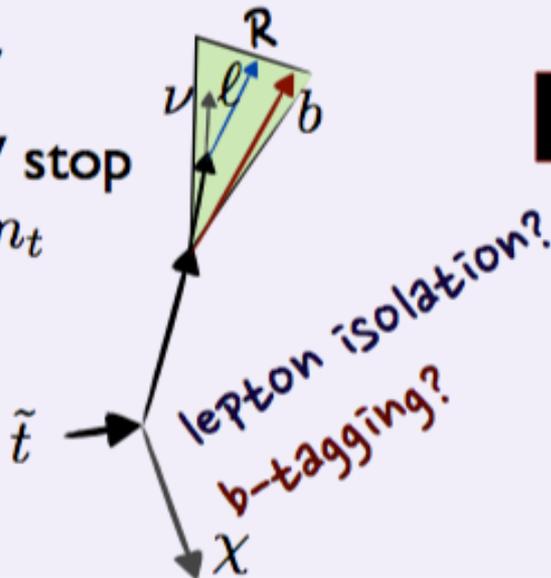
$$R \sim 8 / (\pi \gamma_t)$$

$$\tilde{t} \rightarrow t \tilde{\chi}^0, \sqrt{s} = 100 \text{ TeV}$$

100 TeV

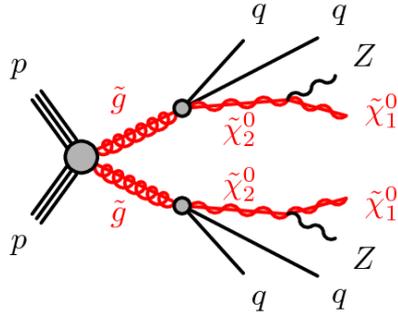
7000 GeV stop

$m_{\tilde{t}} \sim 30m_t$

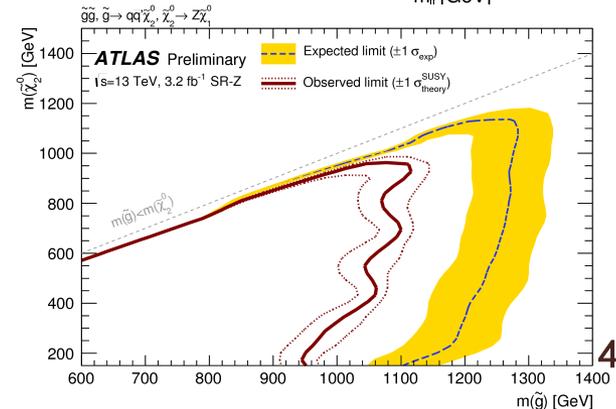
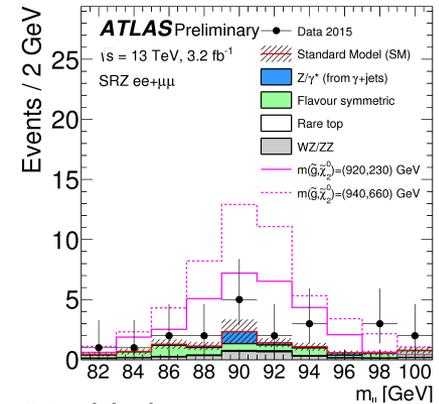
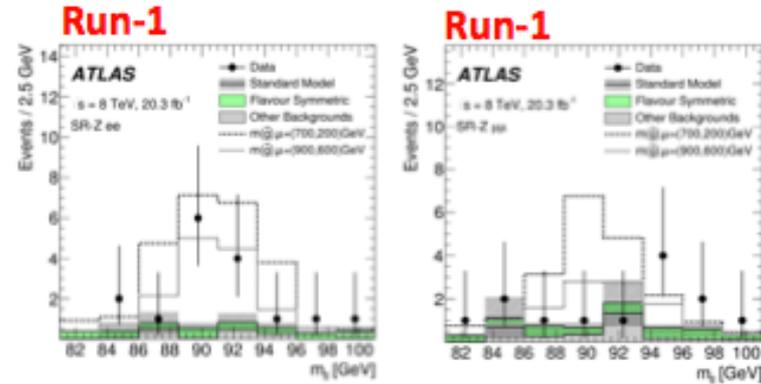


Strong Production: Z(II)+MET

- Search for **gluinos** with a Z + jets + MET signature



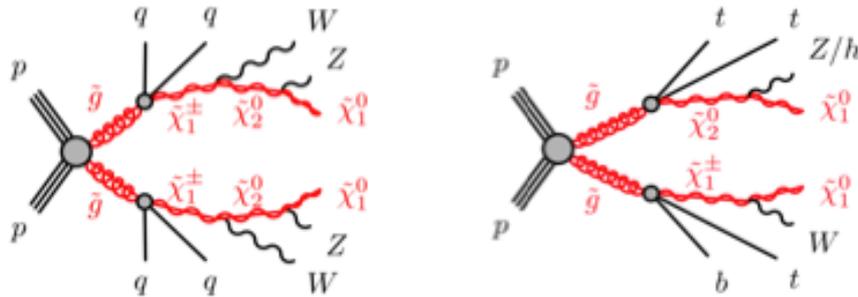
- There is an excess (3σ) at ATLAS Run1 (not at CMS): obs. 29, exp. 10.8 ± 2.2
- Check it with Run2 using run1-like SR: Z (II), 2jets, MET > 225 GeV, HT > 600 GeV
- a mild excess seen in Run2: obs. 21, exp. 10.4 ± 2.4 (2.2σ in intermediate MET)
- Excludes gluino masses up to 1.1 TeV



Strong Production: 0L+7-10j+MET

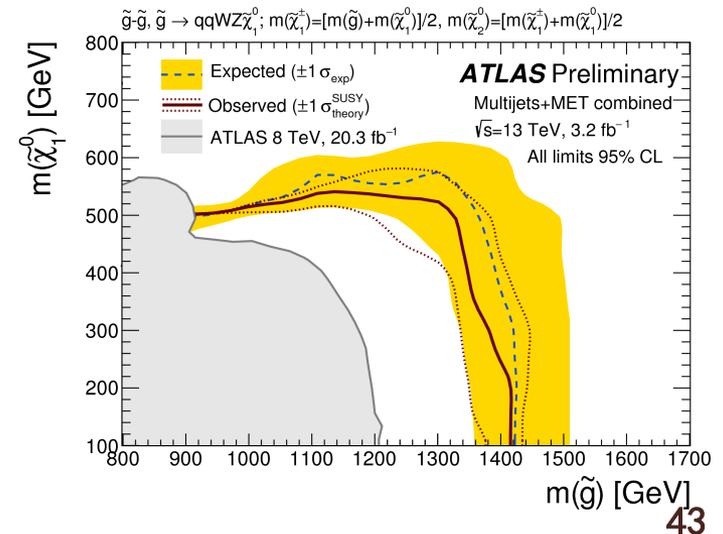
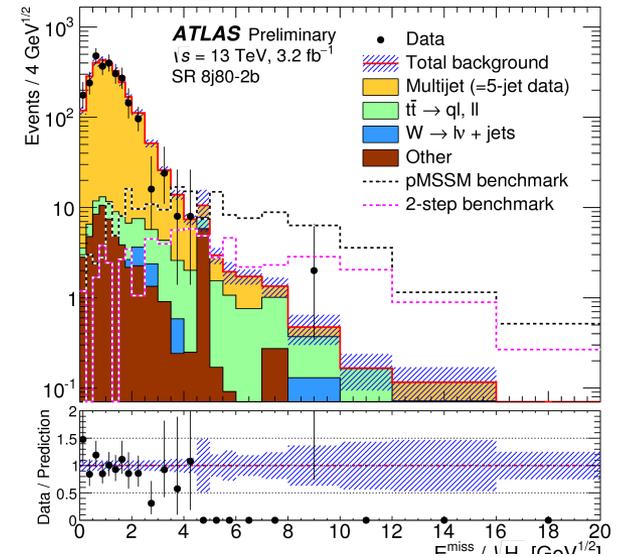
ATLAS-CONF-2015-077

- Search for gluinos and squarks aiming at more complex decay chains



- Signal to BG discrimination based on: $MET/\sqrt{H_T}$
- 15 signal regions defined based on jet multiplicity 7-10 and b-jet multiplicity
- Excludes gluino masses up to 1.4 TeV, significantly extending run1 reach

No significant excess

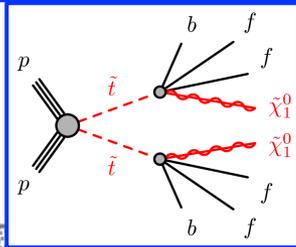


1-lepton stop search: 2/3/4-body decay to LSP

JHEP 11 (2014) 118

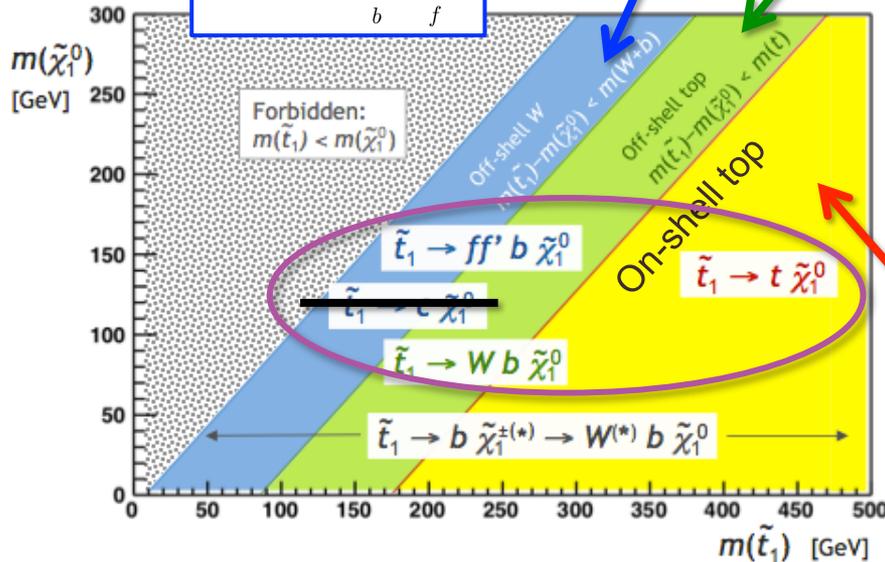
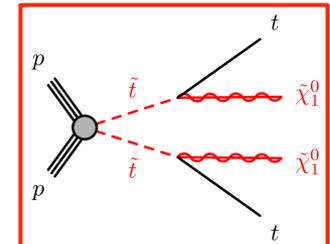
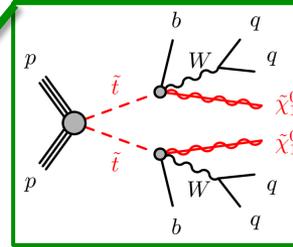
Stop 4-body decay:

- 1 soft lepton (6/7 GeV mu/e), hard ISR jet, ≥ 1 b-jet, MET cut
- Shape fit in lepton p_T



Stop 3-body decay:

- 1 lepton, ≥ 4 jets, ≥ 1 b-jet, MET cut
- Softer thresholds on MET, MT...
- 2-D shape fit in m_T and m_{T2}



Stop \rightarrow top + neutralino decay:

- 1 lepton, ≥ 4 jets, ≥ 1 b-jet, MET cut
- Large-R jets (collect decay products of boosted top in heavy stop search)
- Shape fit for diagonal

Dominant BG: tt, W (MC normalized to data)

Excesses seen in RUN1 (Exotics, SUSY)

■ For a more detailed review, see the [physics plenary talk \(July 18th\) by T. Golling](#)

■ **Mono-jet** [CDS link](#)

- $\sim 1.7\sigma$ / 2.4σ excess above BG in the two highest MET SRs
- High MET SRs dropped for paper (very low stat in CR)

■ **VV \rightarrow JJ** [CDS link](#)

- Mass of fat jets each consistent with W,Z mass

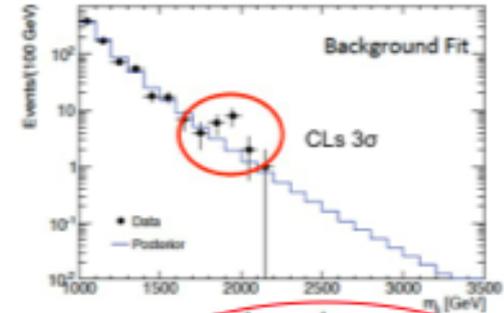
■ **Same-sign leptons / 3-leptons + b-jets** [CDS link](#)

■ **3-leptons + 3 b-jets** [CDS link](#) (obs. 9, exp. 1.29 ± 0.65)

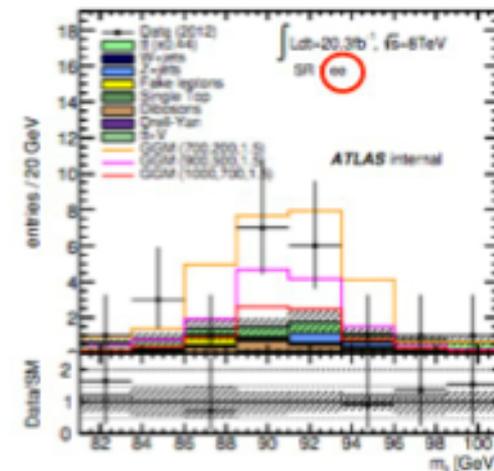
- $\sim 3.5\sigma$ in a validation region of the 3-lepton search
- Plan a dedicated SR for run2

■ **Z+jets + MET** [CDS link](#)

- Peaking at Z mass, BG dominated by non-Z (tt)



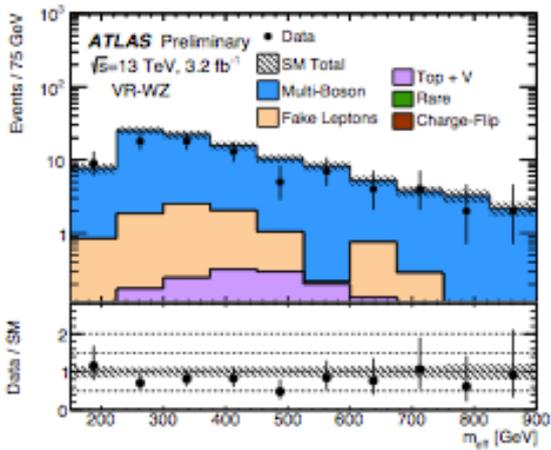
RVLQ5/SR4t2	SRVLQ6/SR4t3	SRVLQ7/SR4t4
$16 \pm 0.73 \pm 0.87$	$4.25 \pm 0.46 \pm 0.85$	$1.12 \pm 0.30 \pm 0.23$
6	12	6
0.430	0.00952	0.00734



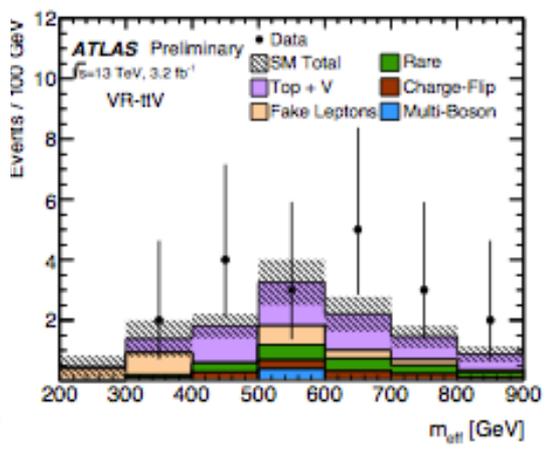
SS/3L

	$N_{\text{lept}}^{\text{signal}} (N_{\text{lept}}^{\text{cand}})$	$N_{b\text{-jets}}^{20}$	N_{jets}^{25}	$E_{\text{T}}^{\text{miss}}$ [GeV]	m_{eff} [GeV]	Other
VR-WW	=2 (=2) =1 SS pair	=0	≥ 2	35–200	300–900	$m(j_1 j_2) > 500$ GeV $p_{\text{T}}(j_2) > 40$ GeV $p_{\text{T}}(\ell_2) > 30$ GeV veto $80 < m_{ee} < 100$ GeV
VR-WZ	=3 (=3)	=0	1–3	30–200	<900	$p_{\text{T}}(\ell_3) > 30$ GeV
VR-ttV	≥ 2 (-) ≥ 1 SS pair	≥ 2	$\geq 5 (e^\pm e^\pm, e^\pm \mu^\pm)$ $\geq 3 (\mu^\pm \mu^\pm)$	20–200	200–900	$p_{\text{T}}(\ell_2) > 25$ GeV veto $E_{\text{T}}^{\text{miss}} > 125$ and $m_{\text{eff}} > 650$ GeV
VR-ttZ	≥ 3 (-) ≥ 1 SFOS pair	≥ 1	≥ 4 (=1 b -jet) ≥ 3 (≥ 2 b -jets)	20–150	100–900	$p_{\text{T}}(\ell_2) > 25$ GeV $p_{\text{T}}(\ell_3) > 20$ GeV (if e) $80 < m_{\text{SFOS}} < 100$ GeV
All VRs	Veto events belonging to any SR, or if ℓ_1 or ℓ_2 is an electron with $ \eta > 1.37$ (except in VR-WZ)					

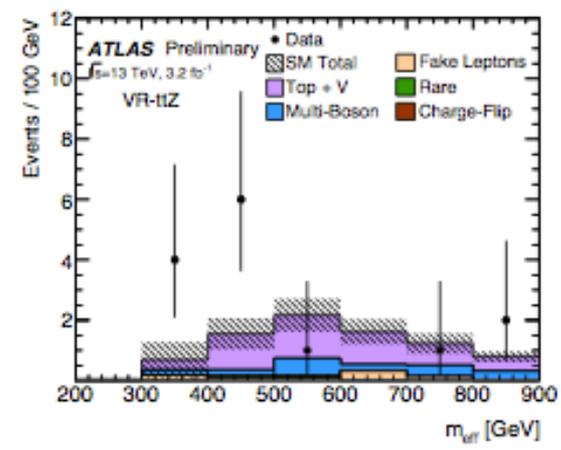
	VR-WW	VR-WZ	VR-ttV	VR-ttZ
Observed events	4	82	19	14
Total bkg events	4.1 ± 0.9	106 ± 16	11.6 ± 2.8	8.4 ± 2.0
Fake/non-prompt leptons	0.63 ± 0.46	8 ± 5	2.0 ± 1.4	0.7 ± 1.0
Charge flip	0.26 ± 0.04	–	1.14 ± 0.14	–
$t\bar{t}W, t\bar{t}Z$	0.07 ± 0.03	0.81 ± 0.29	5.5 ± 1.9	4.7 ± 1.5
WZ	1.1 ± 0.4	81 ± 14	0.20 ± 0.08	1.3 ± 0.5
$W^\pm W^\pm jj$	1.4 ± 0.5	–	0.02 ± 0.02	–
ZZ	0.47 ± 0.30	16 ± 5	0.3 ± 0.3	0.7 ± 0.5
Triboson	0.01 ± 0.01	0.67 ± 0.34	< 0.01	< 0.01
Rare	0.10 ± 0.05	0.9 ± 0.5	2.3 ± 1.2	1.1 ± 0.6



(d) m_{eff} in WZ validation region



(e) m_{eff} in $t\bar{t}V$ validation region



(f) m_{eff} in $t\bar{t}Z$ validation region

Table 1: Summary of the event selection criteria for the signal regions (see text for details).

Signal region	$N_{\text{lept}}^{\text{signal}}$	$N_{b\text{jets}}^{20}$	N_{jets}^{50}	$E_{\text{T}}^{\text{miss}}$ [GeV]	m_{eff} [GeV]
SR0b3j	≥ 3	$= 0$	≥ 3	> 200	> 550
SR0b5j	≥ 2	$= 0$	≥ 5	> 125	> 650
SR1b	≥ 2	≥ 1	≥ 4	> 150	> 550
SR3b	≥ 2	≥ 3	-	> 125	> 650

SS/3L

Table 5: The number of observed data events and expected background contributions in the signal regions. The p -value of the observed events for the background-only hypothesis is denoted by $p(s = 0)$. The ‘‘Rare’’ category contains the contributions from $t\bar{t}t\bar{t}$, $t\bar{t}t$ and $t\bar{t}WW$ production. Background categories shown as ‘‘-’’ denote that they cannot contribute to a given region (charge flips or $W^{\pm}W^{\pm}jj$ in 3-lepton regions). The individual uncertainties can be correlated and therefore do not necessarily add up in quadrature to the total systematic uncertainty.

	SR0b3j	SR0b5j	SR1b	SR3b	VR-ttZ
Observed events	3	3	7	1	14
Total bkg events	2.4 ± 0.7	0.98 ± 0.32	4.3 ± 1.0	0.78 ± 0.24	8.4 ± 2.0
$p(s = 0)$	0.33	0.06	0.12	0.36	
Fake/non-prompt leptons	< 0.2	$0.04^{+0.17}_{-0.04}$	0.8 ± 0.8	0.12 ± 0.16	0.7 ± 1.0
Charge flip	-	0.02 ± 0.01	0.60 ± 0.12	0.19 ± 0.06	-
$t\bar{t}W, t\bar{t}Z$	0.13 ± 0.06	0.11 ± 0.06	2.0 ± 0.7	0.21 ± 0.09	4.7 ± 1.5
WZ	1.5 ± 0.5	0.61 ± 0.25	0.17 ± 0.09	< 0.02	1.3 ± 0.5
$W^{\pm}W^{\pm}jj$	-	0.11 ± 0.05	0.03 ± 0.01	< 0.01	-
ZZ	0.6 ± 0.4	< 0.14	< 0.03	< 0.03	0.7 ± 0.5
Triboson	0.09 ± 0.05	0.02 ± 0.01	0.02 ± 0.01	< 0.01	< 0.01
Rare	0.05 ± 0.04	0.05 ± 0.04	0.7 ± 0.4	0.26 ± 0.14	1.1 ± 0.7

Study the impact of the full set of ATLAS SUSY searches on the pMSSM.

Use 19-parameter pMSSM

- Minimal flavor violation with no new source of CP violation
- Degenerate 1st and 2nd generation squarks and sleptons
- No RPV and the LSP is the $\tilde{\chi}_1^0$

500×10^6 models in the pMSSM are randomly sampled.
 300×10^3 models survive theory and non-LHC constraints
(precision EW, LEP, Higgs, DM)

22 ATLAS Run 1 RPC SUSY searches are reinterpreted in the pMSSM \Rightarrow **200 SR!**

Best expected SR used for exclusion.

Makes full use of ATLAS simulation, reconstruction and analysis.

$> 30 \times 10^9$ events generated for truth-based analysis.

$> 600 \times 10^6$ events simulated & reconstructed.

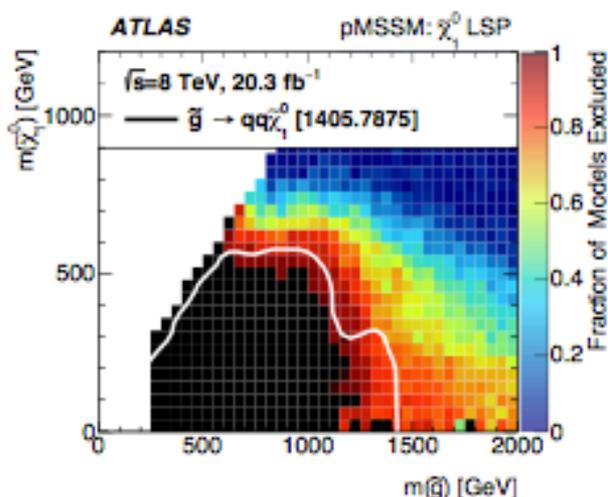
Most comprehensive results from ATLAS on SUSY to date

Analysis

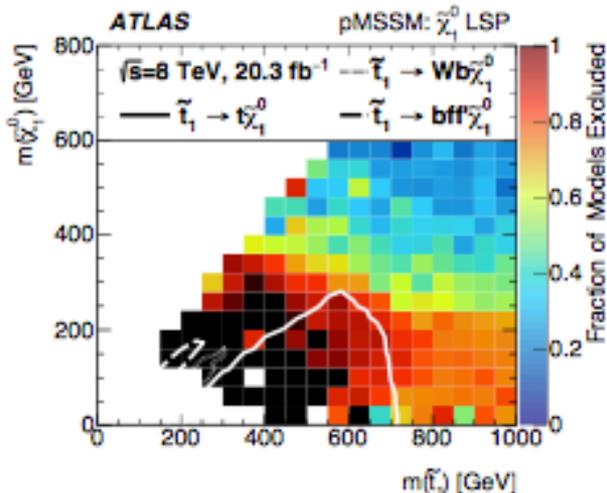
0-lepton + 2-6 jets + E_T^{miss}
 0-lepton + 7-10 jets + E_T^{miss}
 1-lepton + jets + E_T^{miss}
 $\tau(\tau/\ell)$ + jets + E_T^{miss}
 SS/3-leptons + jets + E_T^{miss}
 0/1-lepton + 3b-jets + E_T^{miss}
 Monojet

0-lepton stop
 1-lepton stop
 2-leptons stop
 Monojet stop
 Stop with Z boson
 2b-jets + E_T^{miss}
 $t\bar{b} + E_T^{\text{miss}}$, stop

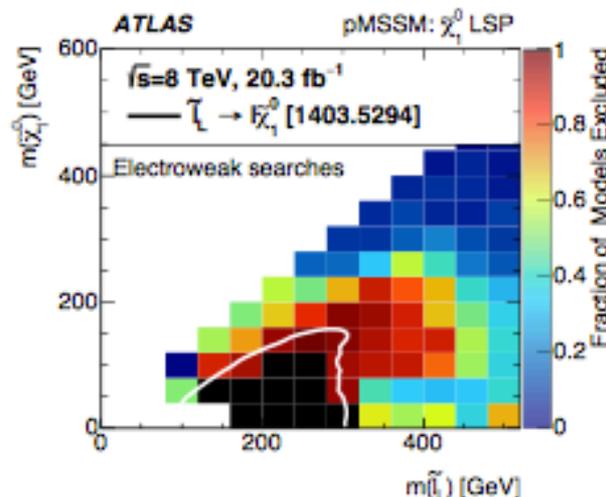
ℓh
 2-leptons
 2- τ
 3-leptons
 4-leptons
 Disappearing Track
 Long-lived particle
 $H/A \rightarrow \tau^+\tau^-$



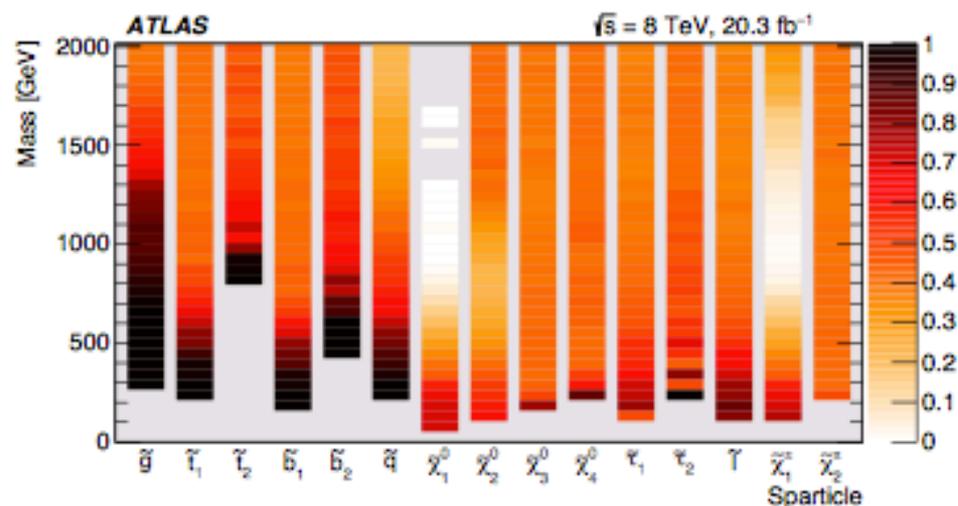
Good agreement with simplified models. Diagonal excluded by mono-jet analysis. Intermediate sparticles reduce exclusion for heavy \tilde{g} .



Simplified model overestimates reach (100% BR). Higgs mass constraint excludes light $\tilde{\tau}_1$ models. Heavy $\tilde{\tau}_1$ models with long-lived $\tilde{\chi}_{1\pm}$ excluded by disappearing track analysis.



Good agreement with simplified models.



- Highest sensitivity to strong processes.
- Simplified models \leftrightarrow pMSSM models (some differences observed).
- Good complementarity between different searches and with direct detection experiments (see paper for details).

Interpretation strategy

Based on the number of observed, expected events in all regions with all uncertainties:
Probability density function (PDF)

From the constructed distribution of test statistic for s+b, find the p-value of the observation

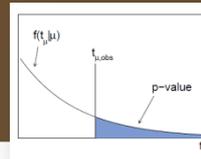
$$p_{\mu} = \int_{t_{\mu, \text{obs}}}^{\infty} f(t_{\mu} | \mu) dt_{\mu}$$

If $CL_s < 0.05$: the value of signal is excluded at 95% CL.....

$$CL_s = \frac{CL_{s+b}}{CL_b} = \frac{p_{s+b}}{1 - p_b}$$

Likelihood function: $L(\mu, \theta)$
 μ : signal strength (POI);
 θ : nuisance parameters (NP)
Profile Likelihood: constrain uncertainty (NP) as part of a likelihood fit

Construct the PDF of test statistic t_{μ} : generate toy Monte Carlo or using asymptotic formula



The above check has been done for each signal grid points on the SUSY model. The line can be drawn for the area where points are excluded

Construct test statistics t_{μ} based on likelihood ratio λ :

$$\tilde{\lambda}(\mu) = \begin{cases} \frac{L(\mu, \hat{\theta}(\mu))}{L(\hat{\mu}, \hat{\theta})} & \hat{\mu} \geq 0, \\ \frac{L(\mu, \hat{\theta}(\mu))}{L(0, \hat{\theta}(0))} & \hat{\mu} < 0 \end{cases} \quad t_{\mu} = -2 \ln \lambda(\mu)$$

Find the observed test statistic for tested μ : $t_{\mu, \text{obs}}$

