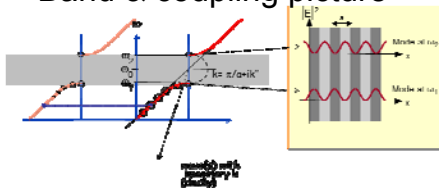


▶ Course 3 :

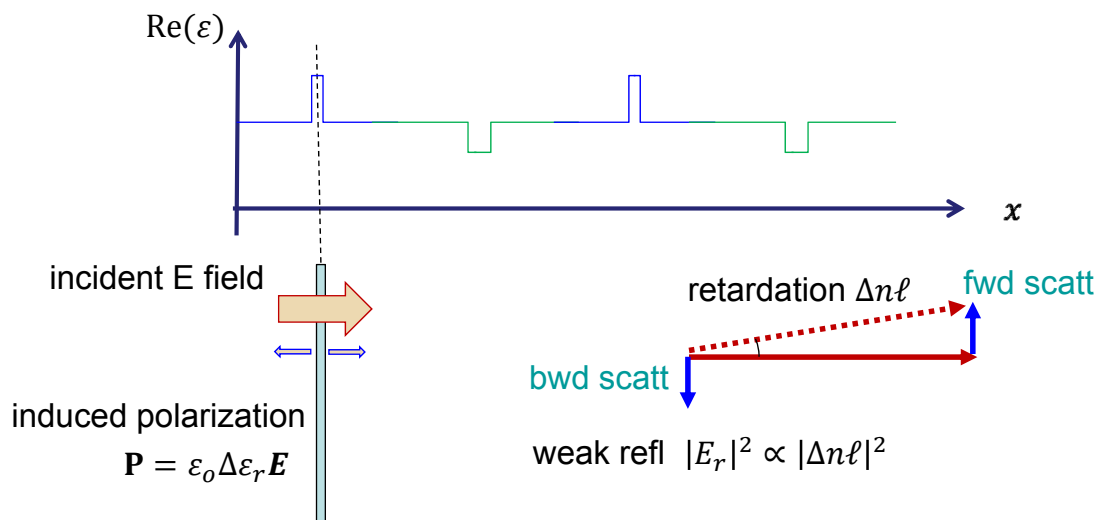
- **Bragg with gain/loss (complex  $\epsilon$ ) modulation**
- Unidirectionality of plane-wave coupling
- History of gain-modulation (1970's & 1990's)
- Kulishov's proposals :  
single-sided mirrors, strange cavities, memories
- WGM lasers
- Fano & EIT

*Another view of modulation : scattering*

- Band & coupling picture

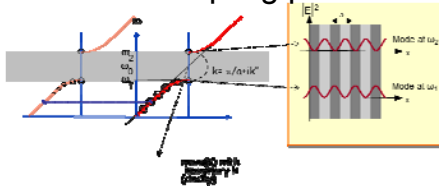


- Scattering picture [1] real index

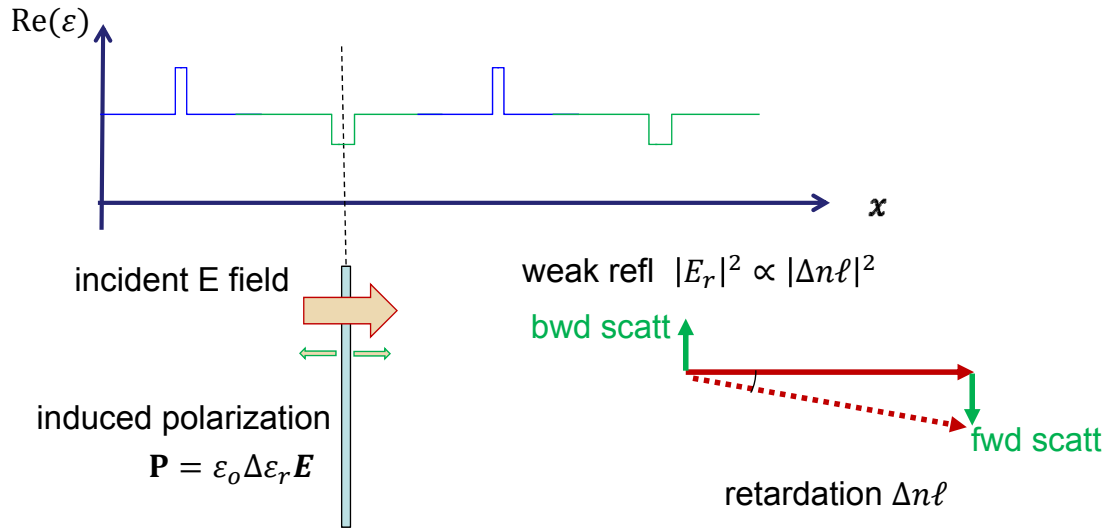


# Another view of modulation : scattering

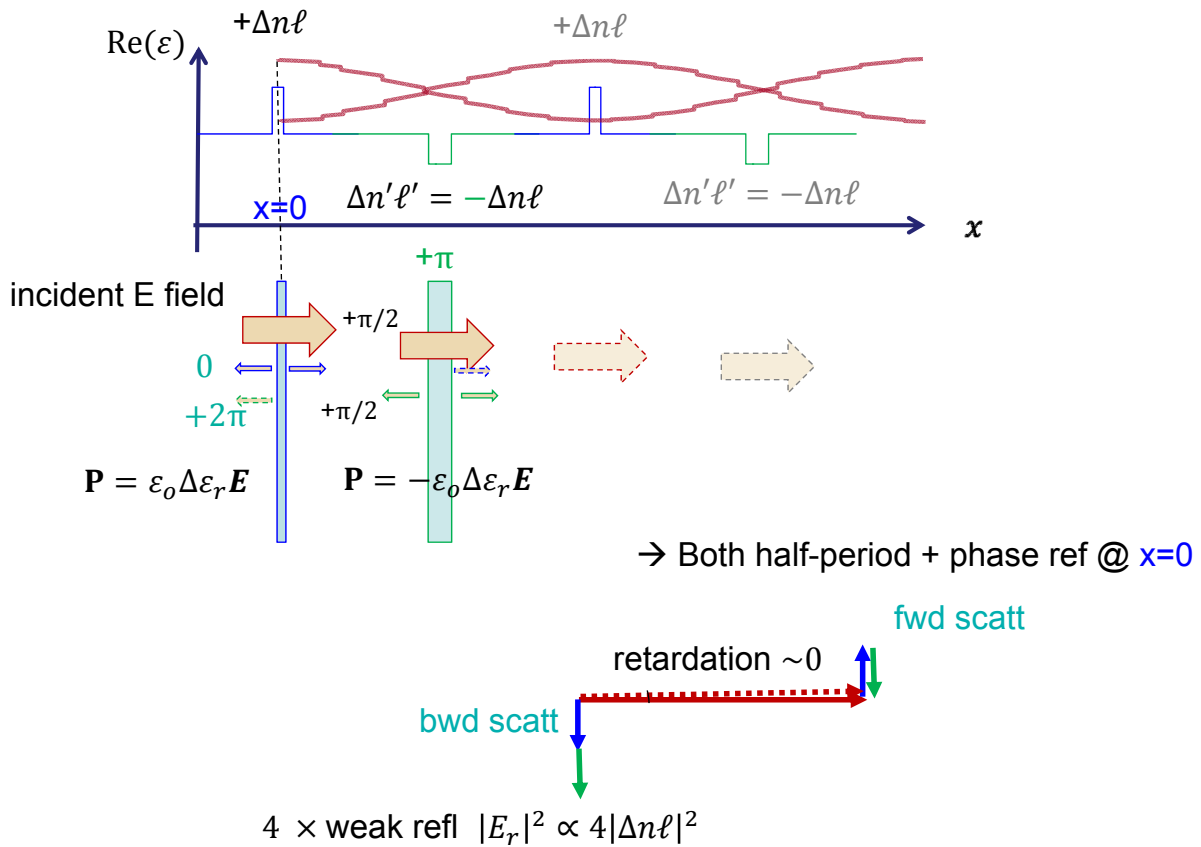
- Band & coupling picture



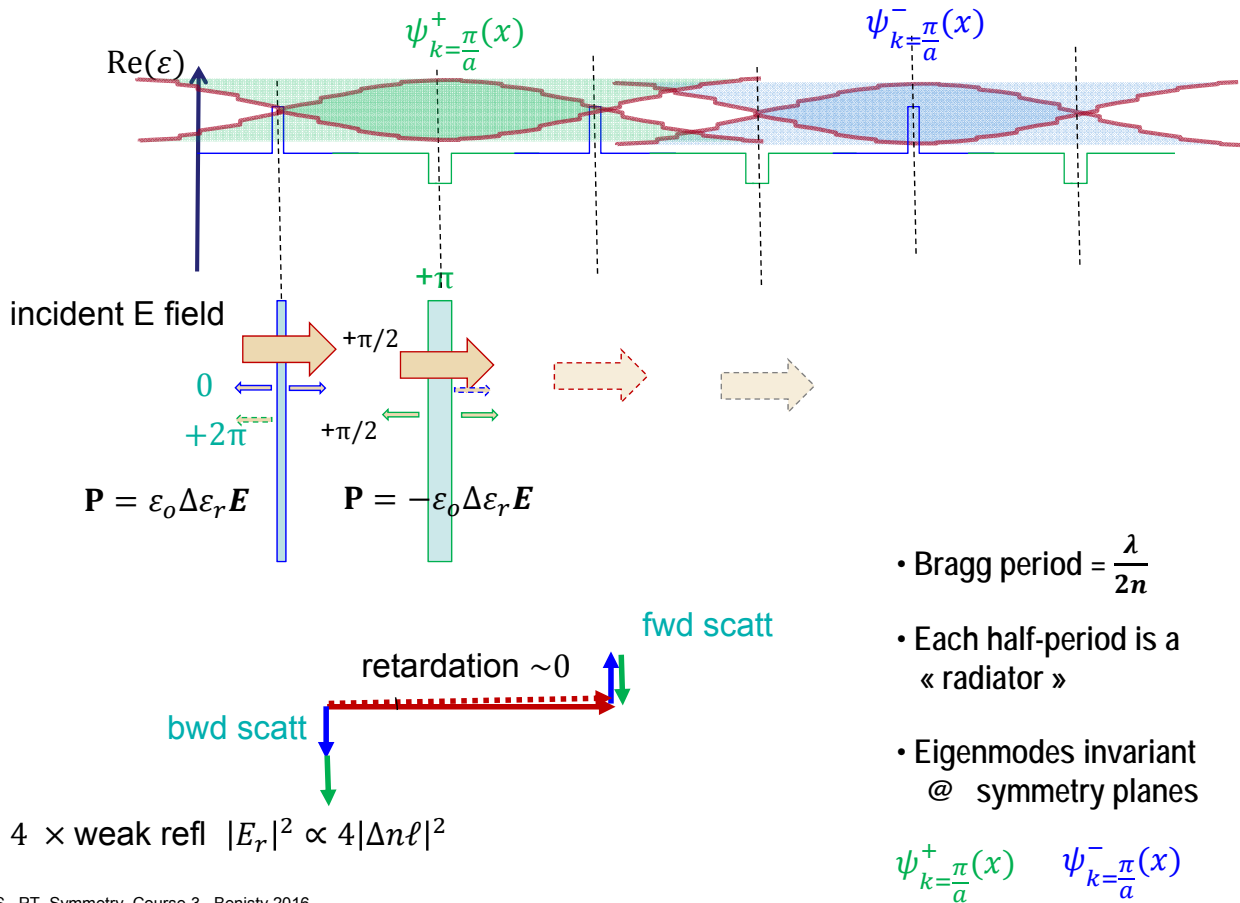
- Scattering picture [1] real index.... Second half period



# Scattering and Bragg

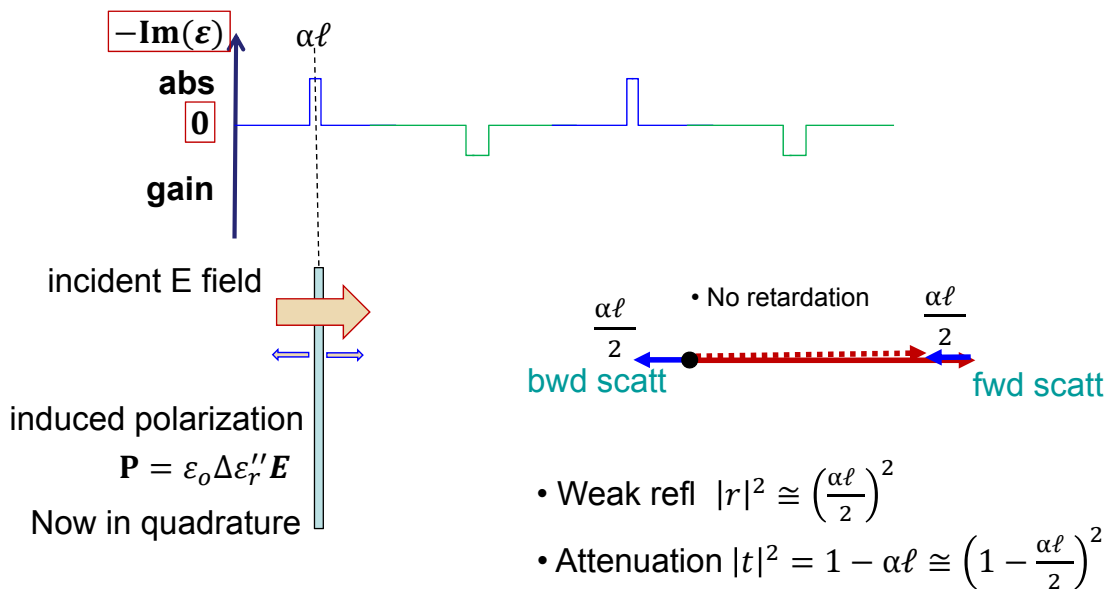


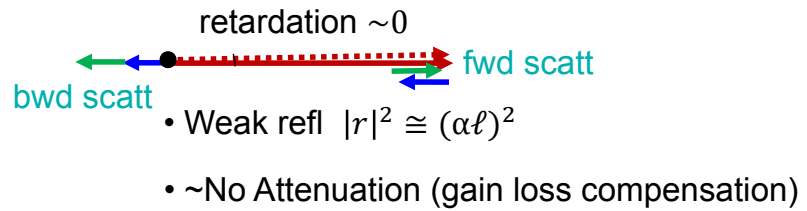
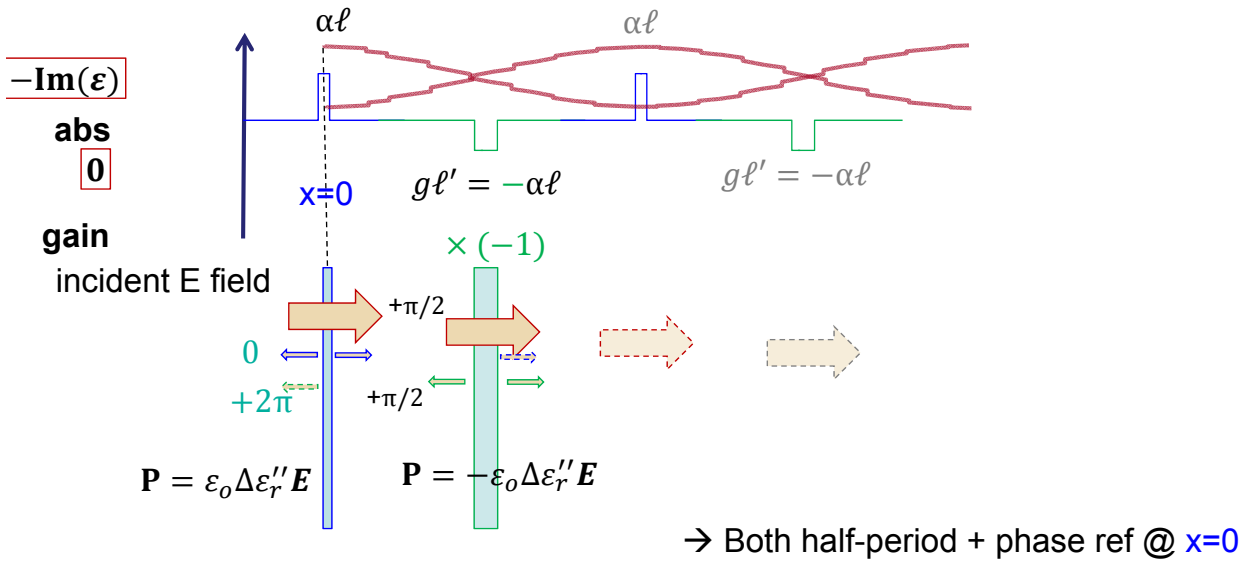
# Scattering and Bragg (real part)



# Another view of modulation : scattering of abs/gain layer

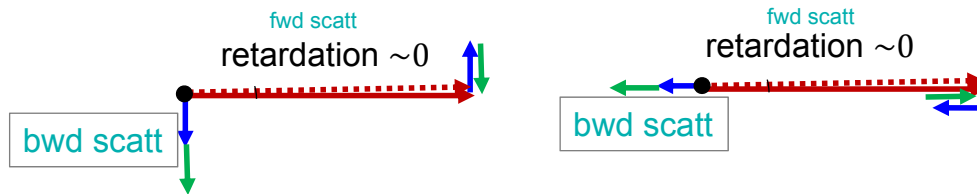
- Scattering picture: [2] imaginary index



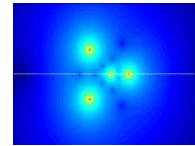


## Comparison of Re and Im scattering

- $|t| \sim 1$  @ 1st order,
- Only phase of  $r$  changes



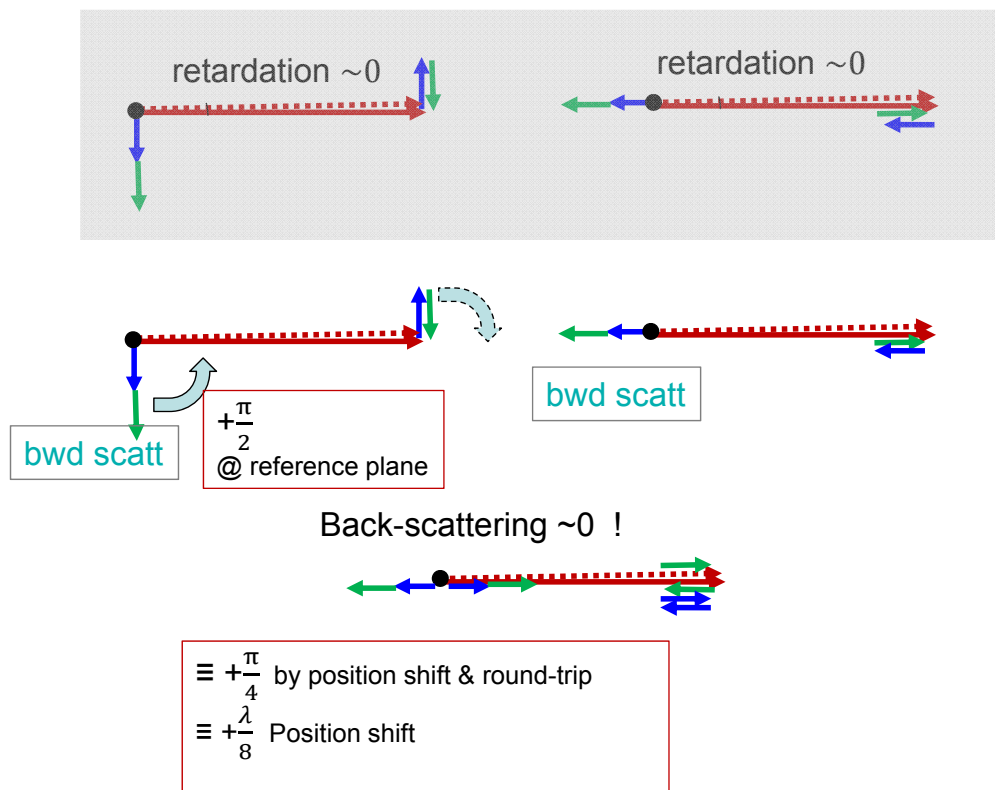
... What if we devise some clever combination ???



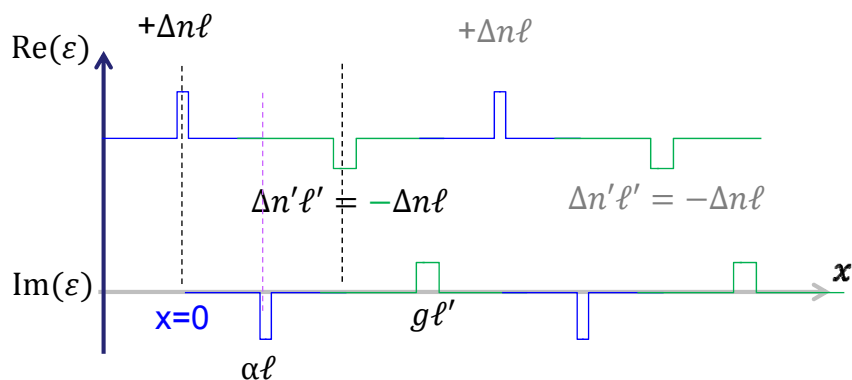
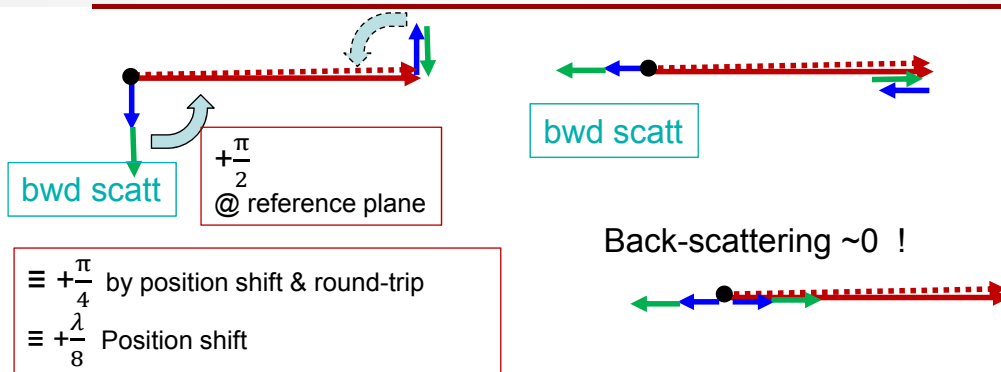
▶ Course 3 :

- Bragg with gain/loss (complex  $\varepsilon$ ) modulation
- **Unidirectionality of plane-wave coupling**
- History of gain-modulation (1970's & 1990's)
- Kulishov's proposals :  
single-sided mirrors, strange cavities, memories
- WGM lasers
- Fano & EIT

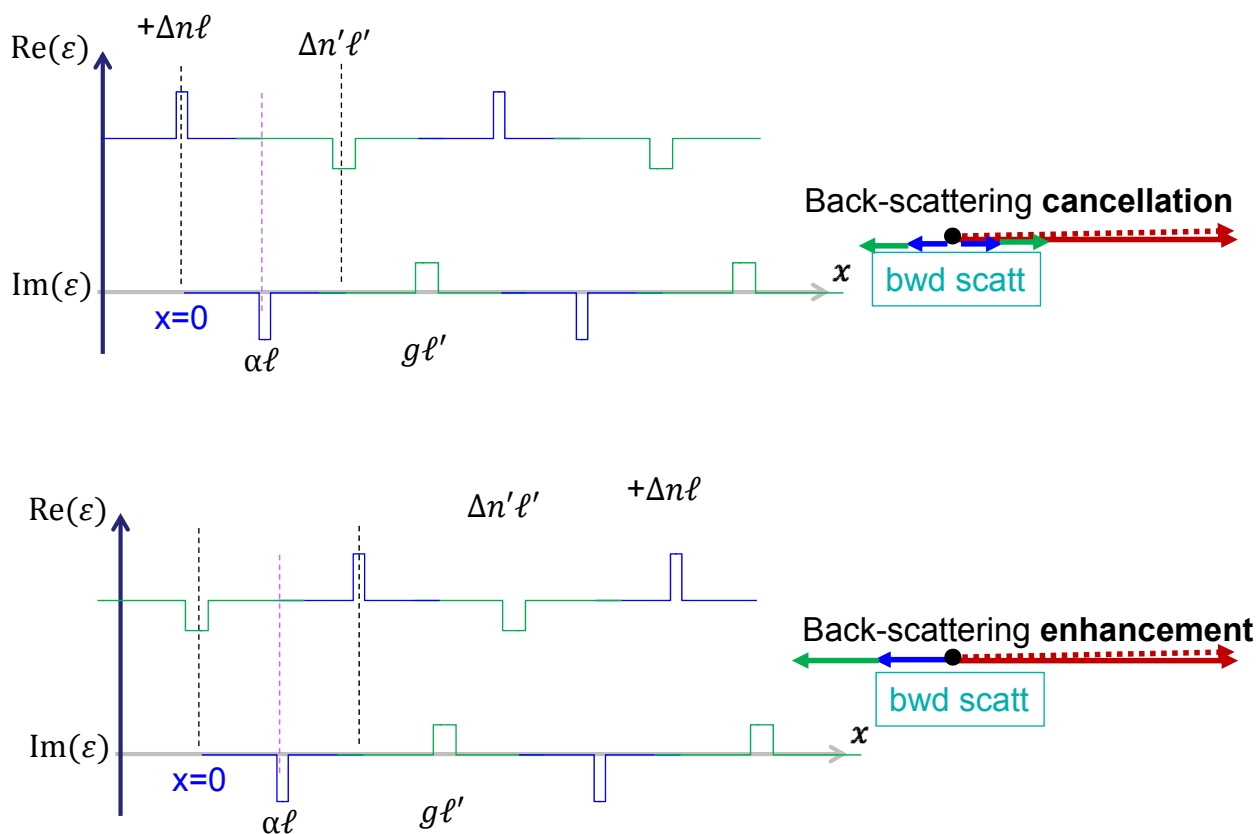
*One-sided cancellation of Re and Im scattering*

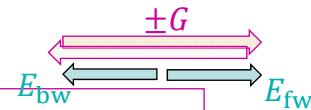


# « Single-sided scattering »



# « Single-sided scattering »





- Usual coupling constant of index grating:

$$\kappa_G \equiv \langle E_{fw} | \Delta\varepsilon(x) | E_{bw} \rangle = \int e^{-\frac{iGx}{2}} \widehat{\Delta\varepsilon}_G \cos(Gx) e^{-\frac{iGx}{2}} dx \equiv \left(\frac{1}{2}\right) \widehat{\Delta\varepsilon}_G$$

Hence same  $\pm G$  coupling,  $\kappa_G = \kappa_{-G}$

- In more generality, coupling is complex but ...

$$\kappa_{\pm G} \equiv \langle E_{bw} | \Delta\varepsilon(x) | E_{fw} \rangle = \int e^{\pm \frac{iGx}{2}} \widehat{\Delta\varepsilon}_G \cos(Gx + \varphi) e^{\pm \frac{iGx}{2}} dx = \left(\frac{1}{2}\right) \widehat{\Delta\varepsilon}_G e^{\mp i\varphi}$$

phase here only means *shift* of grating position – usual Fourier manipulation

- Single sided band means :

$$\kappa_{+G} = \int e^{-\frac{iGx}{2}} \widehat{\Delta\varepsilon}_G (\cos Gx + i \sin Gx) e^{-\frac{iGx}{2}} dx = \int e^{-\frac{iGx}{2}} \widehat{\Delta\varepsilon}_G e^{+iGx} e^{-\frac{iGx}{2}} dx = \widehat{\Delta\varepsilon}_G$$

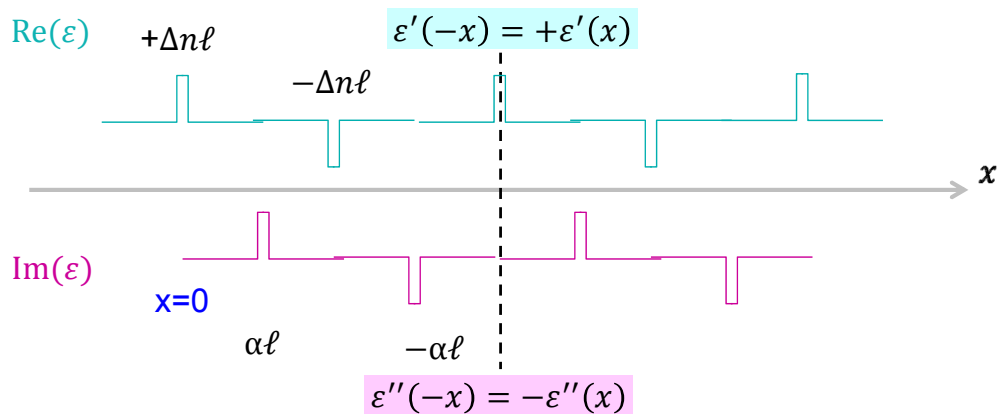
- But

$$\kappa_{-G} = \int e^{-\frac{iGx}{2}} \widehat{\Delta\varepsilon}_G (\cos Gx - i \sin Gx) e^{-\frac{iGx}{2}} dx = \int e^{-\frac{iGx}{2}} \widehat{\Delta\varepsilon}_G e^{-iGx} e^{-\frac{iGx}{2}} dx = 0$$

*This is PT symmetry ... in the basic case*

What about PT symmetry ...

- In our basic implementation  
Re( $\varepsilon$ ) is symmetric and Im( $\varepsilon$ ) antisymmetric

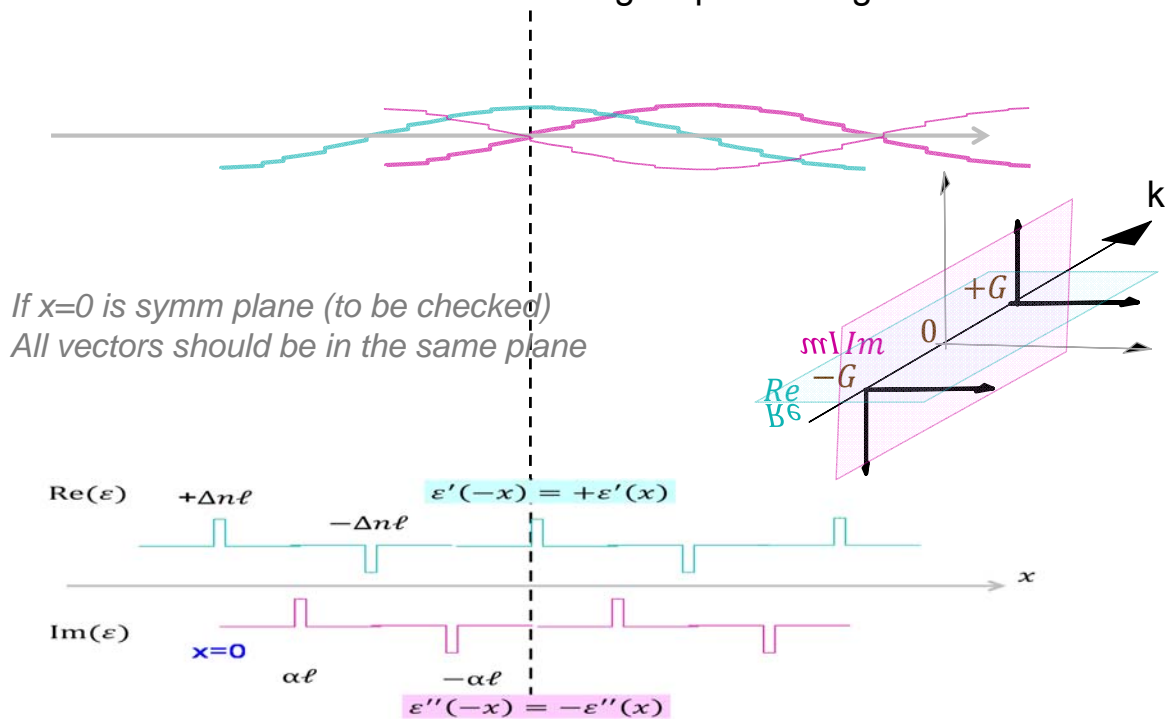


## This is PT symmetry ... in more general case

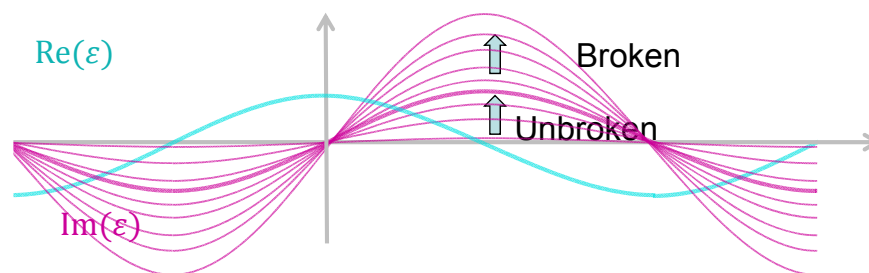
What about PT symmetry ...

- In a more general case

Think of same Fourier rules as for signal processing



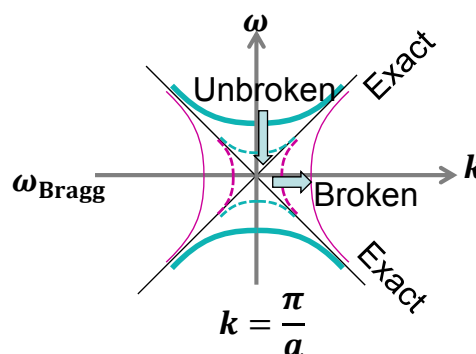
## This is PT symmetry ... broken or not ?



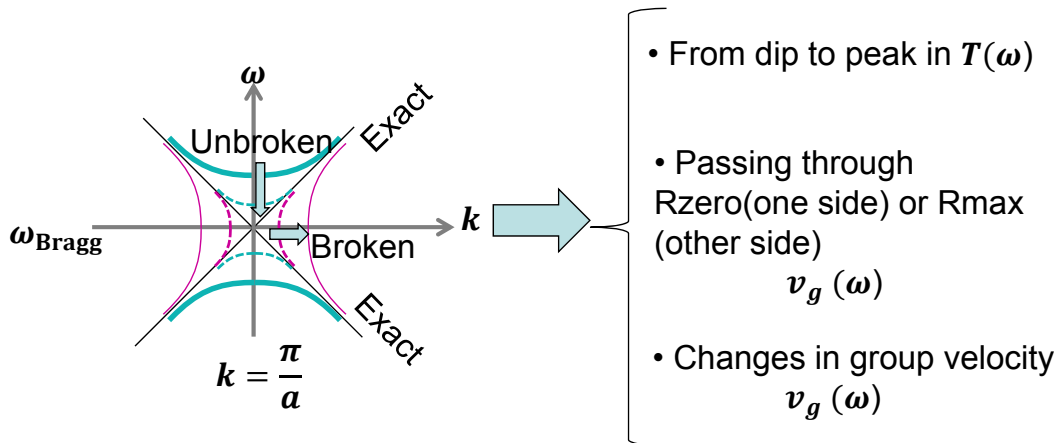
$T = 1$  (since  $R = 0$  from one side) at Bragg frequency ?

→ only for exact balance of **Re** and **Im** (cf. scattering picture).

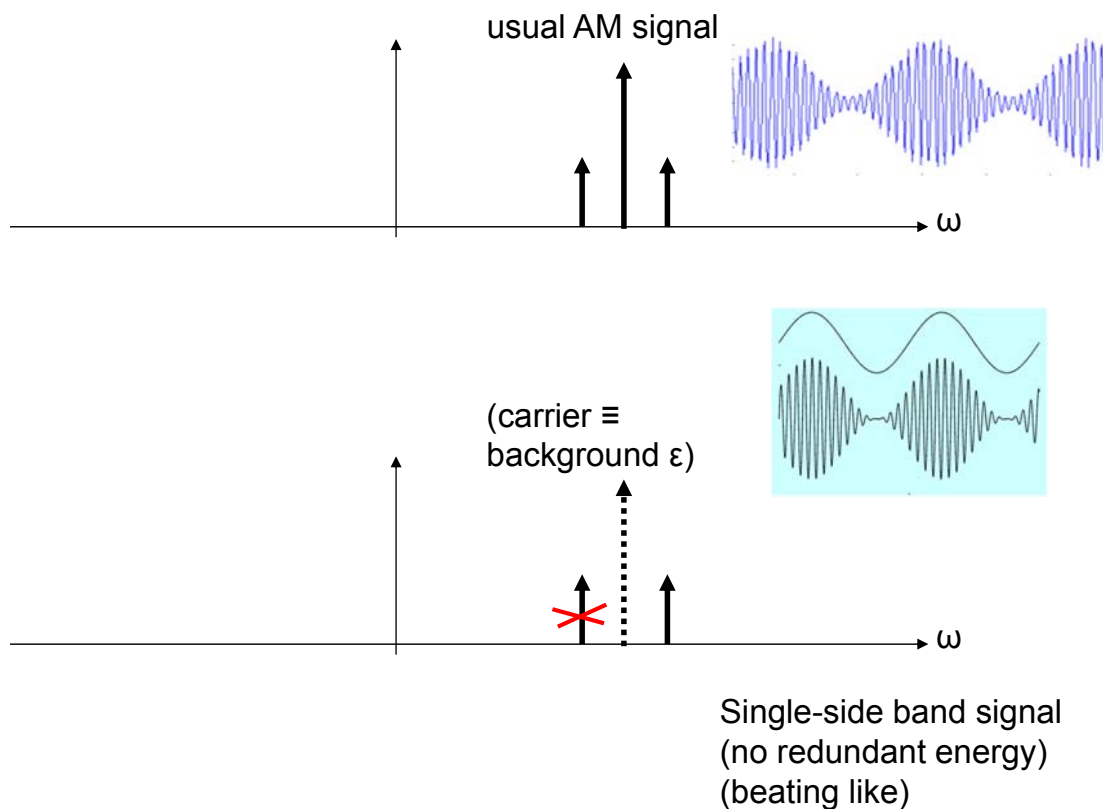
→ This is fully analogous to the case of merging eigenvalues



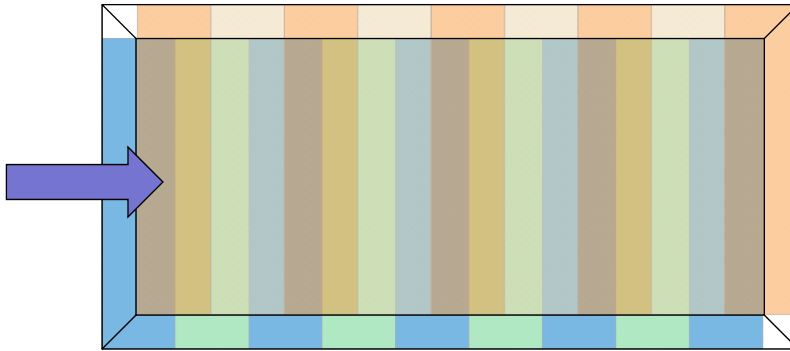




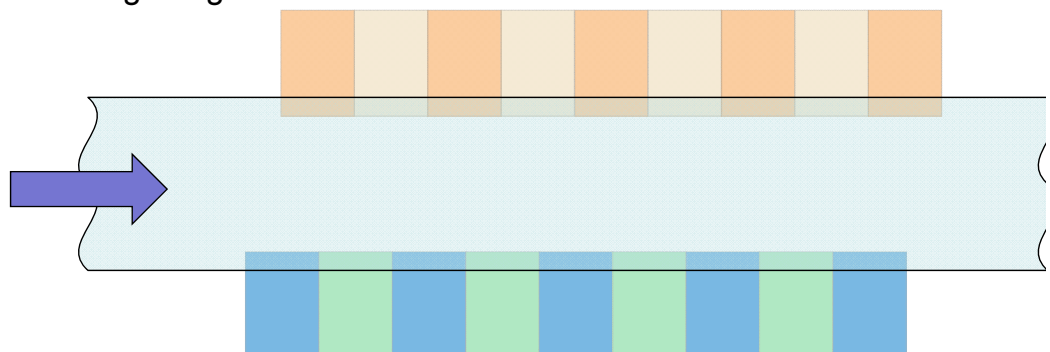
## « Single-sided scattering » in (radio) Fourier language



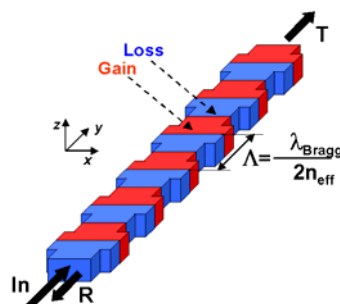
- Requires four different layers in layered materials

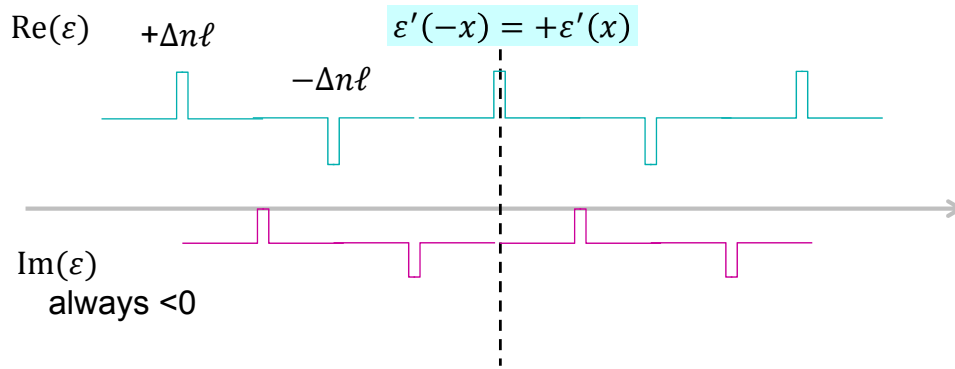


- ... or two different gratings



- ... possible a « shape » and a « material » grating (for Re and Im resp.)





All ideal  $\mathcal{PT}$ -Sym systems can be multiplied by  $\exp(-\langle \text{average loss} \rangle z)$  to lower  $\text{Im}(\varepsilon)$  in negative-only territory  
 (~ "Passive  $\mathcal{PT}$  systems")

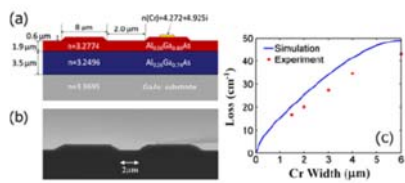


FIG. 3 (color online). Non-Hermitian dual structure. (a) Design details and complex refractive index distribution. (b) Scanning electron microscopy picture of the finalized passive  $\mathcal{PT}$  device with the Cr stripe shown on the right. (c) Modal loss of isolated waveguide structure as a function of Cr width.

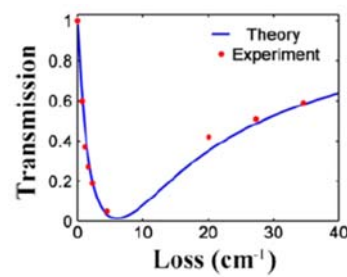


FIG. 4 (color online). Experimental observation of spontaneous passive  $\mathcal{PT}$ -symmetry breaking. Output transmission of a passive  $\mathcal{PT}$  complex system as the loss in the lossy waveguide arm is increased. The transmission attains a minimum at  $6 \text{ cm}^{-1}$ .

Observation of  $\mathcal{PT}$ -Symmetry Breaking in Complex Optical Potentials

A. Guo and G.J. Salamo

Department of Physics, University of Arkansas, Fayetteville, Arkansas 72701, USA

D. Duchesne and R. Morandotti

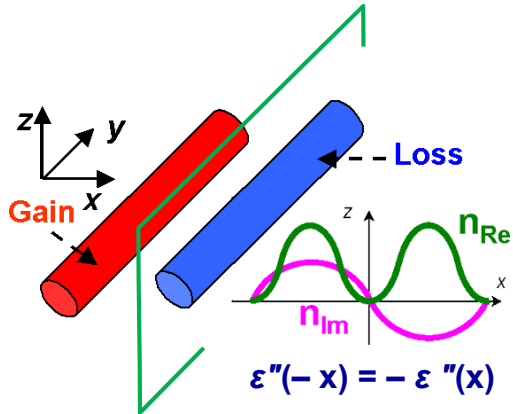
INRS-EMT, Varennes, Québec J3X 1S2, Canada

M. Volatier-Ravat and V. Aimez

Centre de Recherche en Nanofabrication et en Nanocaractérisation, Université de Sherbrooke, Sherbrooke, Québec J1K 2R1, Canada

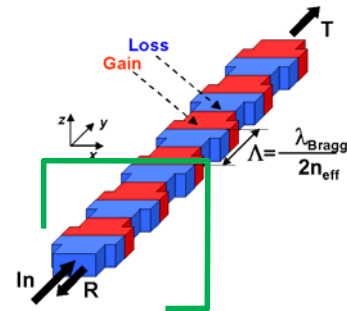
G. A. Siviloglou and D. N. Christodoulides

## Transverse $PT$ -symmetry



$PT$ -symmetry coupled waveguides

## Longitudinal $PT$ -symmetry



$PT$ -symmetry Bragg grating waveguide

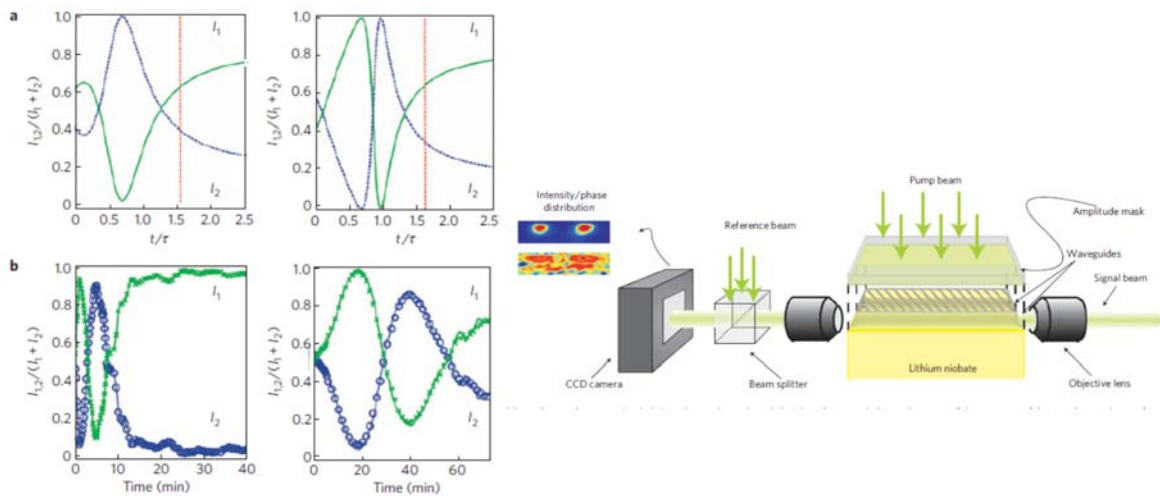
## *PT-symmetry and Waveguides / (3) Waveguides & Bragg structures*

### Examples

- Waveguide based
- Just planar

Christian E. Rüter<sup>1</sup>, Konstantinos G. Makris<sup>2</sup>, Ramy El-Ganainy<sup>2</sup>, Demetrios N. Christodoulides<sup>2</sup>,  
Mordechai Segev<sup>3</sup> and Detlef Kip<sup>1\*</sup>

NATURE PHYSICS | VOL 6 | MARCH 2010 |

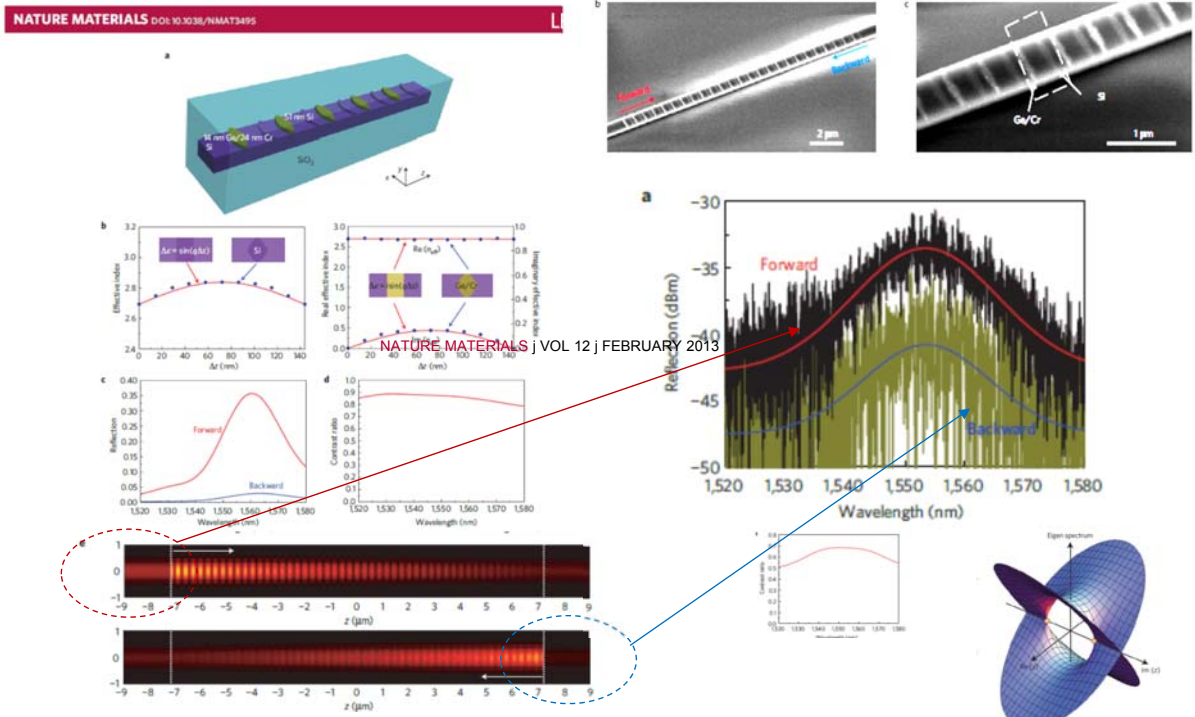


**Figure 3 | Computed and experimentally measured response of a PT-symmetric coupled system.** **a**, Numerical solution of the coupled equations (1) describing the PT-symmetric system. The left (right) panel shows the situation when light is coupled into channel 1 (2). Red dashed lines mark the symmetry-breaking threshold. Above threshold, light is predominantly guided in channel 1 experiencing gain, and the intensity of channels 1 and 2 depends solely on the magnitude of the gain. **b**, Experimentally measured (normalized) intensities at the output facet during the gain build-up as a function of time.

## Experimental demonstration of a unidirectional reflectionless parity-time metamaterial at optical frequencies

NATURE MATERIALS | VOL 12 | FEBRUARY 2013  
p.108

Liang Feng<sup>1\*</sup>, Ye-Long Xu<sup>2</sup>, William S. Fegadolli<sup>1,3,4</sup>, Ming-Hui Lu<sup>2\*</sup>, José E. B. Oliveira<sup>3</sup>,  
Wilson R. Almeida<sup>3,4</sup>, Yan-Feng Chen<sup>2</sup> and Axel Scherer<sup>1</sup>

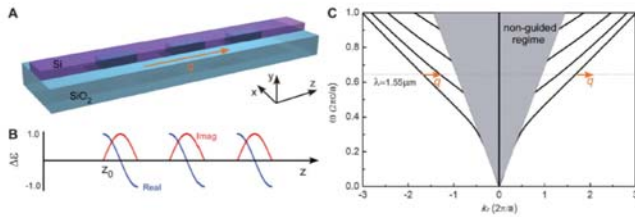


**Figure 3 |** The two solutions of a two-channel waveguide with a complex and interacting Hamiltonian coalesce at the exceptional points (orange spheres). The destructive interference of the two can lead to the observation of unidirectional reflectionless waveguiding without involving gain media.  $\text{Re}(\epsilon)$  and  $\text{Im}(\epsilon)$  are the real and imaginary parts of the complex parameter, respectively.

# Nonreciprocal Light Propagation in a Silicon Photonic Circuit

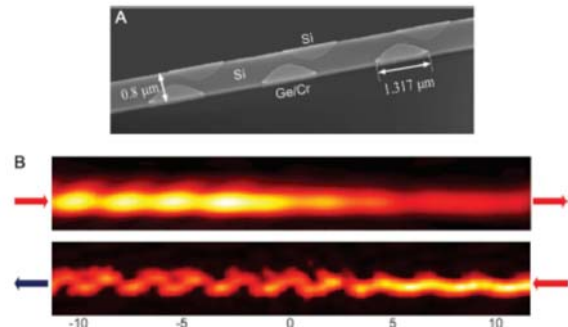
Liang Feng,<sup>1,2,4,\*</sup> Maurice Ayache,<sup>3\*</sup> Jingqing Huang,<sup>1,4\*</sup> Ye-Long Xu,<sup>2</sup> Ming-Hui Lu,<sup>2</sup>  
Yan-Feng Chen,<sup>2†</sup> Yeshaiahu Fainman,<sup>3</sup> Axel Scherer<sup>1,4†</sup>

SCIENCE VOL 333 5 AUGUST 2011

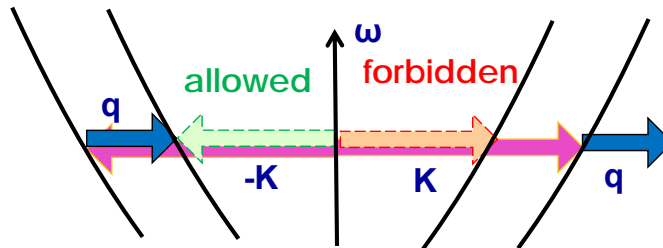


**Fig. 1.** (A) Nonreciprocal light propagation in a Si photonic circuit. Based on a SOI platform, PT optical potentials with exponentially modulated dielectric constants, as depicted in (B) where blue and red curves represent the real and imaginary parts of  $\Delta\epsilon$ , respectively, are embedded in the Si waveguide to introduce an additional wave vector  $q$  to guided light. (C) Band diagram for TE-like polarization of the Si waveguide, where the frequency and wave vector are normalized with  $a = 1 \mu\text{m}$ . At the wavelength of  $1.55 \mu\text{m}$ , if incoming light is a fundamental symmetric mode, one-way mode conversion is only expected for backward propagation where the phase-matching condition is satisfied as indicated by arrows.

729



→ Transition between two dispersion branches



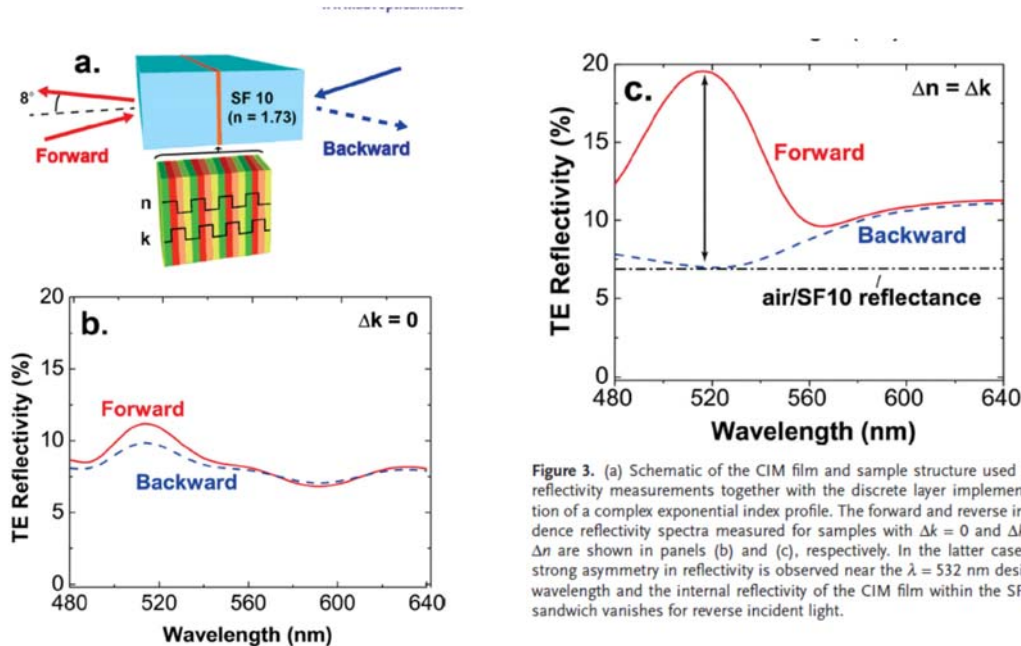
~~$-K \rightarrow -K-q$~~   
 ~~$K \rightarrow K-q$~~   
No -q!

# Passive PT Symmetry in Organic Composite Films via Complex Refractive Index Modulation

Multilayer passive PT

Yixin Yan and Noel C. Giebink \*

Adv. Optical Mater. 2014,  
DOI: 10.1002/adom.201400021



**Figure 3.** (a) Schematic of the CIM film and sample structure used for reflectivity measurements together with the discrete layer implementation of a complex exponential index profile. The forward and reverse incidence reflectivity spectra measured for samples with  $\Delta k = 0$  and  $\Delta k = \Delta n$  are shown in panels (b) and (c), respectively. In the latter case, a strong asymmetry in reflectivity is observed near the  $\lambda = 532 \text{ nm}$  design wavelength and the internal reflectivity of the CIM film within the SF10 sandwich vanishes for reverse incident light.

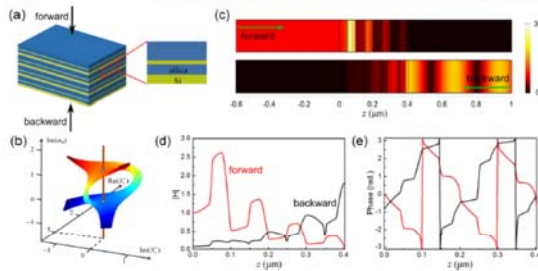


Fig. 1. (a) Schematic of the optical exceptional point structure on a glass wafer designed at the wavelength of 532 nm, where  $n_{Si} = 4.86 - j0.65$  and  $n_{silica} = 1.46$ . (b) Complex eigenvalue solutions of the modified scattering matrix at 532 nm construct a multi-valued Riemann surface as a function of  $\text{Im}(n_p)$ , where red color indicates optical gain and blue corresponds to absorption as we have in Si layers. (c) Simulations of light propagating through the exceptional point structure in the forward (upper panel) and backward (lower panel) directions, in which the distribution of the amplitude of the magnetic field is shown normalized to the incident magnetic field of 1. (d) and (e) are amplitude and phase of the magnetic field in the device as light propagate in the forward (red) and backward (black) directions, respectively.

### Demonstration of a large-scale optical exceptional point structure

Liang Feng,<sup>1</sup> Xuefeng Zhu,<sup>1,2</sup> Sui Yang,<sup>1,3</sup> Hanyu Zhu,<sup>1</sup> Peng Zhang,<sup>1</sup> Xiaobo Yin,<sup>1,3</sup> and Yuan Wang,<sup>1,3</sup> and Xiang Zhang<sup>1,3,4</sup>

<sup>1</sup>National Science Foundation Nanoscale Science and Engineering Center, 3112 Echeverry Hall, University of California, Berkeley, CA 94720, USA

<sup>2</sup>Huazhong University of Science and Technology, Wuhan, Hubei 430074, China

<sup>3</sup>Materials Sciences Division, Lawrence Berkeley National Laboratory (LBNL), 1 Cyclotron Road, Berkeley, CA

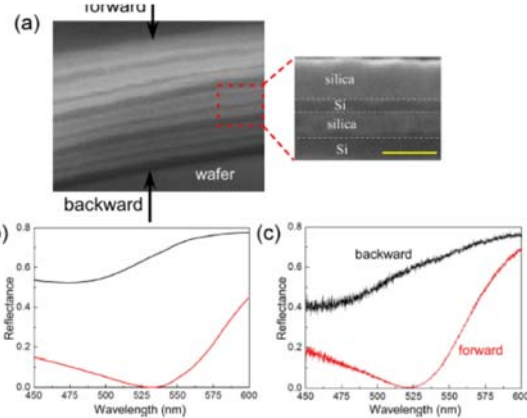
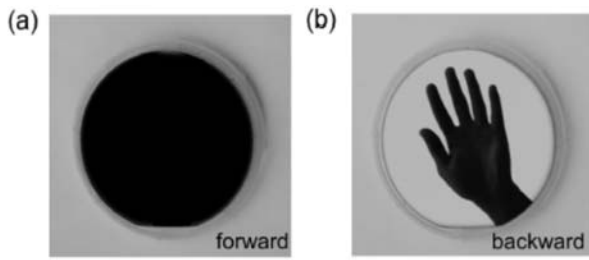


Fig. 3. (a) SEM pictures of the cross-section of the fabricated exceptional point structure. Scale bar, 50 nm. (b) and (c) are numerically calculated and experimentally measured reflection spectra of the exceptional point structure from 450 nm to 600 nm, respectively, for both forward (red) and backward (black) incidence.



## Temporal version of PT symmetry

# Parity-time synthetic photonic lattices

Alois Regensburger<sup>1,2</sup>, Christoph Bersch<sup>1,2</sup>, Mohammad-Ali Miri<sup>3</sup>, Georgy Onishchukov<sup>2</sup>, Demetrios N. Christodoulides<sup>3</sup> & Ulf Peschel<sup>1</sup>

9 AUGUST 2012 | VOL 488 | NATURE | 167

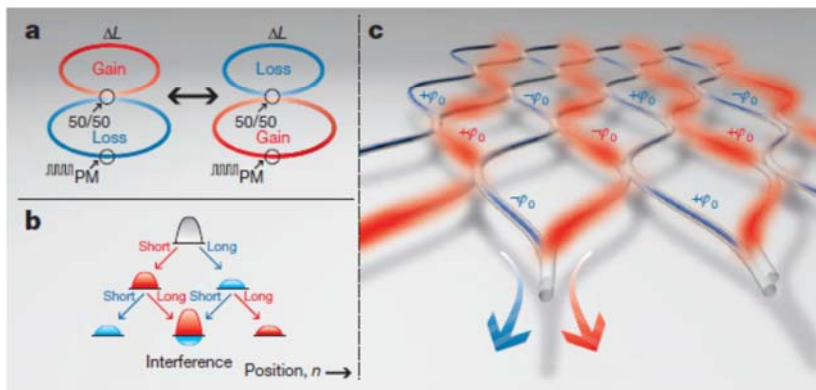
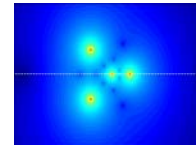


Figure 1 | PT-symmetric fibre networks. a, Two coupled fibre loops periodically switching between gain and loss as used in the experiment (Supplementary Fig. 1). Pulses are delayed or advanced as a result of a length difference  $\Delta L$  between the loops. PM, phase modulator. b, Pulse evolution in the networks. Passages through short and long loops are indicated. c, Equivalent PT-symmetric lattice network. Gain (red) and loss (blue) channels are positioned antisymmetrically and are periodically coupled. Moreover, the real part of the potential is evenly imposed by phase shifts  $\pm\phi_0$ .

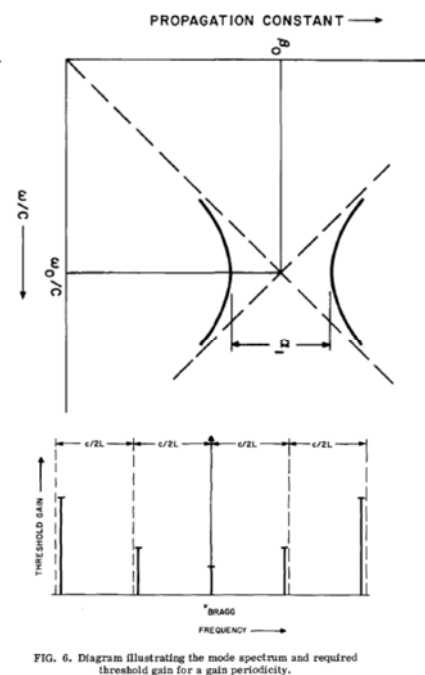
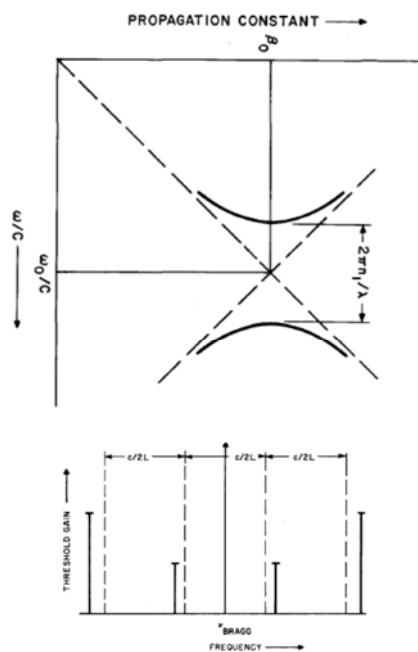
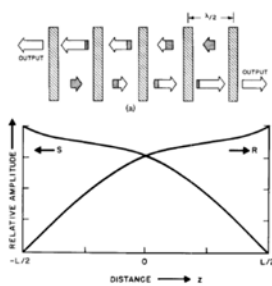


- ▶ Course 3 :
  - Bragg with gain/loss (complex  $\varepsilon$ ) modulation
  - Unidirectionality of plane-wave coupling
  - **History of gain-modulation (1970's & 1990's)**
  - Kulishov's proposals :
    - single-sided mirrors, strange cavities, memories
  - WGM lasers
  - Fano & EIT

Historical 1972 Kogelnik&Shank CMT paper : already gain DFB is there

Coupled-Wave Theory of Distributed Feedback Lasers

H. Kogelnik and C. V. Shank J. Appl. Phys., Vol. 43, No. 5, May 1972





tion spot. Effects of rigid refractive index and gain-loss profiles built into the laser crystal on the mode stability have been examined, and conditions for kink-free, single lateral mode oscillations have been investigated.

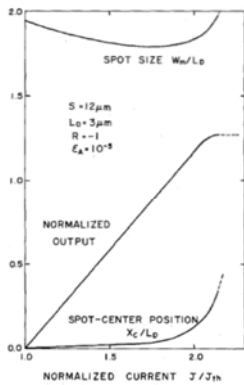


Fig. 2. Solid lines are calculated current dependence of output, emission spot size, and spot-center position.

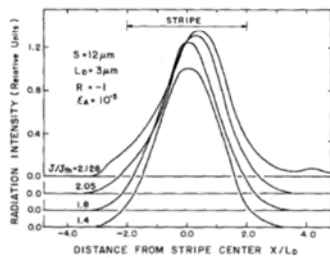


Fig. 3. Calculated near-field intensity profiles at different current levels corresponding to Fig. 2.

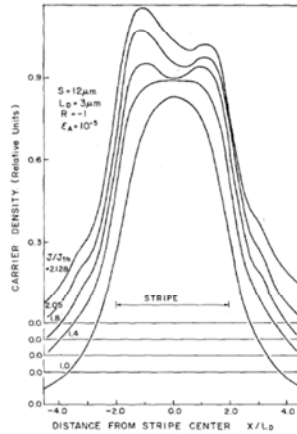


Fig. 4. Calculated carrier density profiles at different current levels corresponding to Fig. 2.

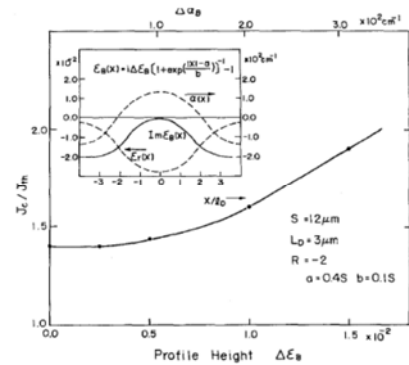


Fig. 9. Dependence of the critical current density on the built-in profile height  $\Delta\epsilon_B$  of the imaginary dielectric constant ( $\Delta\epsilon_B$  of loss). The assumed profile shape is shown in the inset. Other notations are the same as those in Fig. 8.

## Gain-coupled DFB the 90s' come-back (ca. 1990 : Nakano (NTT), Makino (ATT), ...)

### Purely gain-coupled distributed feedback semiconductor lasers

Y. Luo,<sup>(a)</sup> Y. Nakano,<sup>(b)</sup> and K. Tada<sup>(a)</sup>  
 University of Tokyo, 7-3-1 Hongo, Bunkyo-ku, Tokyo 113, Japan  
 T. Inoue, H. Hosomatsu, and H. Iwacka  
 Optical Measurement Technology Development Co., Ltd., 2-11-13 Naka-cho, Musashino-shi, Tokyo 180, Japan

1620 Appl. Phys. Lett. 56 (17), 23 April 1990

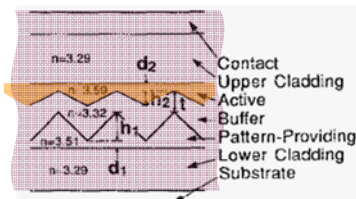


FIG. 1. Schematic drawing of the longitudinal cross section of the new DFB laser structure for pure gain coupling.

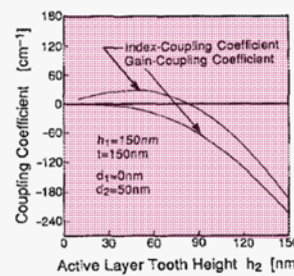


FIG. 2. Gain- and index-coupling coefficients for a second-order symmetric triangular grating.

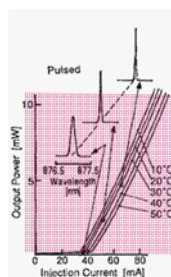
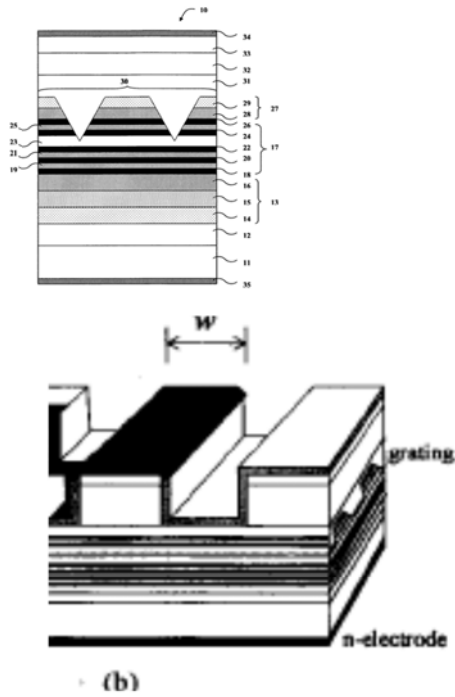


FIG. 4. Light output vs current characteristics and emission spectra at several injection levels.



JOURNAL OF LIGHTWAVE TECHNOLOGY, VOL. 13, NO. 2, FEBRUARY 1995  
196

### Multi- $\lambda$ Ridge Waveguide Gain-Coupled DFB Laser Array

G. P. Li, T. Makino, Member, IEEE, and C. M. Wu

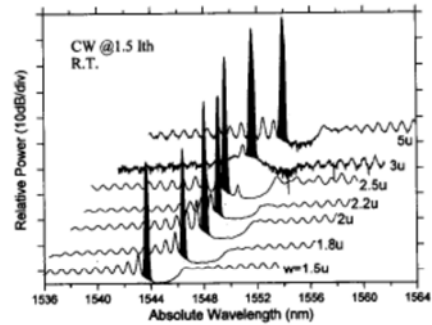


Fig. 3. Lasing spectra of 7 element lasers in the array at cw  $I_{th}$ , 20°C. ( $w$  = ridge width).

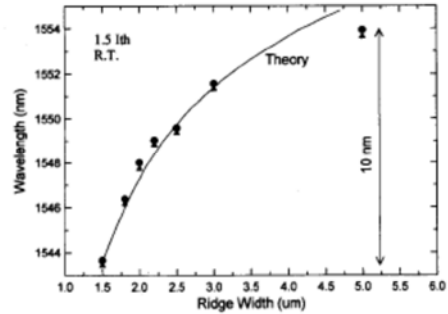


Fig. 4. Ridge width dependence of lasing wavelengths at 1.5  $I_{th}$ , and 20°C. The closed circles are the results of cw and triangles are those for the pulse (T: 10 ms; Duty: 0.8 ms) operations, respectively. The solid curve shows theoretical results.

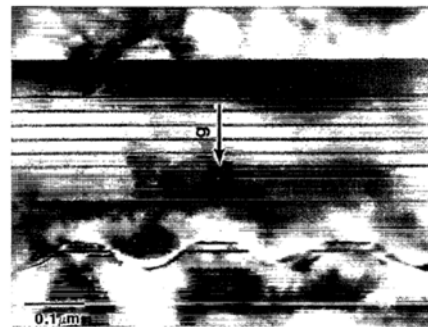
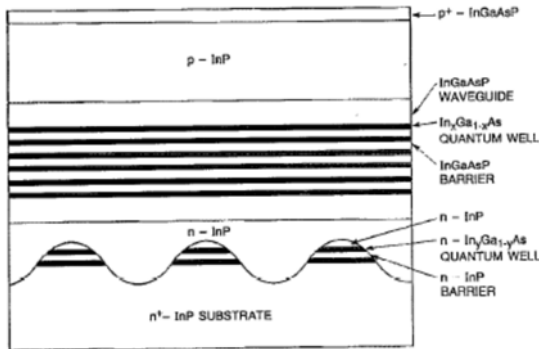


FIG. 2. A TEM photograph of the cross-sectional view of a 6-QW  $In_{0.5}Ga_{0.4}As$  (5 nm)/ $Q_{1.25}$  (18.6 nm) active-layer DFB laser with a 2-QW  $In_{0.61}Ga_{0.38}As$  (4 nm)/InP (9.3 nm) grating.

### Semiconductor distributed feedback lasers with quantum well or superlattice gratings for index or gaincoupled optical feedback

W. T. Tsang, F. S. Choa, M. C. Wu, Y. K. Chen, R. A. Logan, S. N. G. Chu, A. M. Sergent, and C. A. Burrus

Citation: Applied Physics Letters 60, 2580 (1992); doi: 10.1063/1.106915

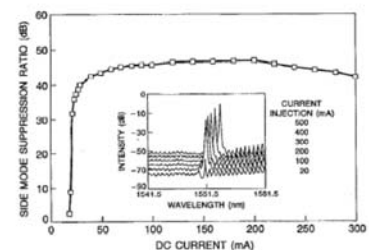
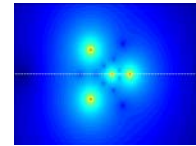


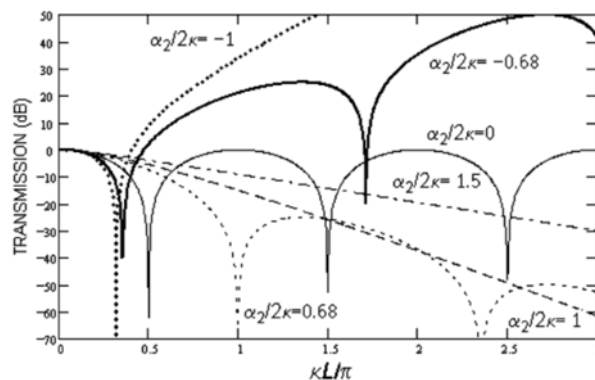
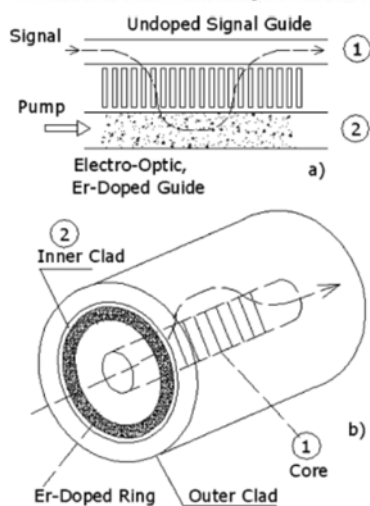
FIG. 5. The SMSR as a function of injection current. The inset shows the spectra at different injection currents. Near threshold the DFB mode is relatively well centered with a small Bragg stop band.



▶ Course 3 :

- Bragg with gain/loss (complex  $\varepsilon$ ) modulation
- Unidirectionality of plane-wave coupling
- History of gain-modulation (1970's & 1990's)
- **Kulishov's proposals :**  
**single-sided mirrors, strange cavities, memories**
- WGM lasers

Fig. 1. General structure of an amplifying tunable filter based on (a) grating-assisted codirectional coupler and (b) long-period fiber grating.



Variation of the grating transmission at the resonance wavelength with the grating strength  $\kappa L$  for different gain/loss parameter values.

## Nonreciprocal waveguide Bragg gratings

Mykola Kulishov <sup>a,b</sup>, Jacques M. Laniel <sup>a</sup>, Nicolas Bélanger <sup>a</sup>, José Azaña <sup>c</sup>, David V. Plant <sup>a</sup>

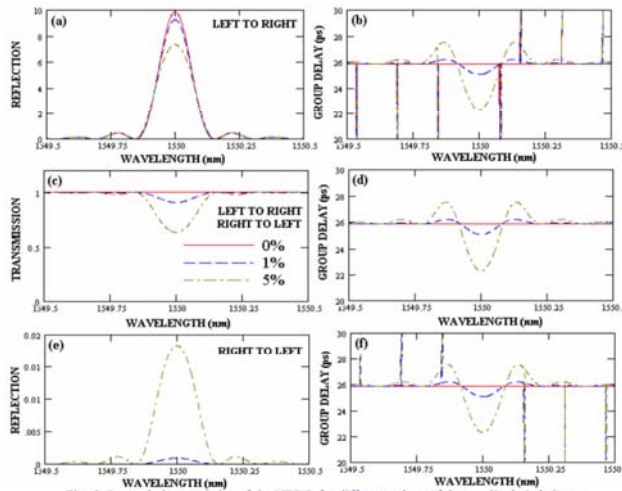


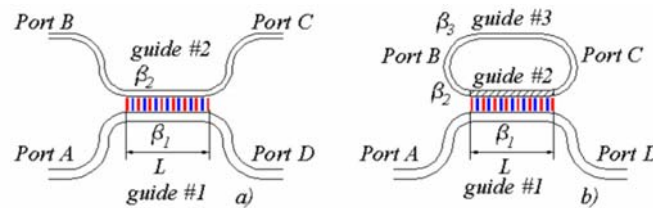
Fig. 5. Spectral characteristics of the NRBG for different values of the amplitude imbalance between the real  $\kappa_n$  and  $\kappa_n$  imaginary components. There is no grating position deviation ( $\Delta z = 0$ ): (a) reflection spectrum and (b) reflection group delay for light launched into the left side of the grating ( $z = 0$ ); (c) transmission spectrum and (d) transmission group delay (the transmission characteristics are the same regardless the light input direction,  $z = 0$  or  $L$ ); (e) reflection spectrum and (f) reflection group delay for light injected into the right side of the grating ( $z = L$ ).

$$\kappa_{12} = [\kappa_n - \kappa_\alpha \exp(j 2\pi\Delta z/\Lambda)],$$

$$\kappa_{21} = [\kappa_n + \kappa_\alpha \exp(-j 2\pi\Delta z/\Lambda)].$$

18 April 2005 / Vol. 13, No. 8 / OPTICS EXPRESS 3068

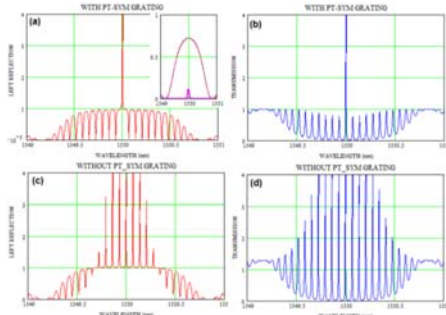
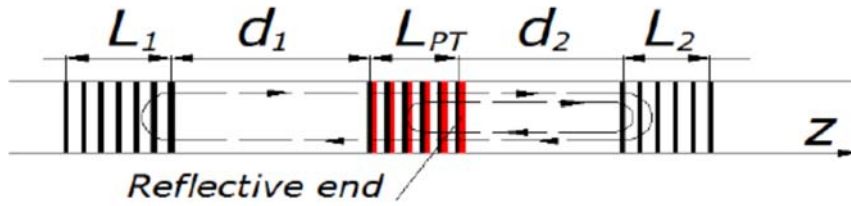
## Use of Four-port devices, with memory in a loop



### Trapping light in a ring resonator using a grating-assisted coupler with asymmetric transmission

Mykola Kulishov <sup>a,b</sup>, Jacques M. Laniel <sup>a</sup>, Nicolas Bélanger <sup>a</sup>, David V. Plant <sup>a</sup>

2 May 2005 / Vol. 13, No. 9 / OPTICS EXPRESS 3567

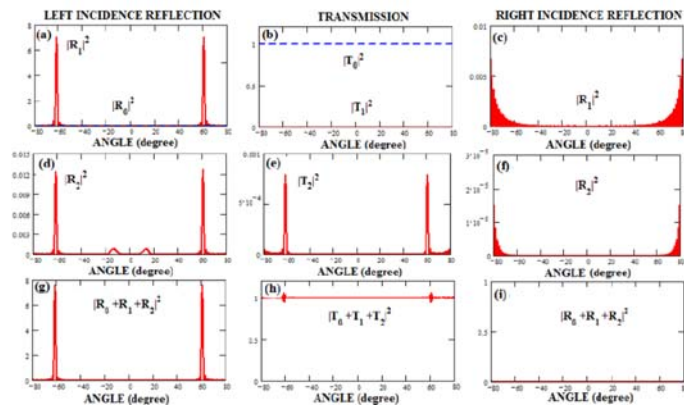
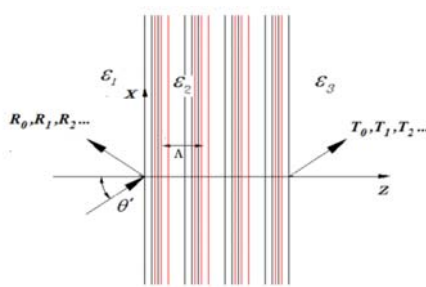


<http://arxiv.org/ftp/arxiv/papers/1505/1505.01391.pdf>

Fig. 2. Fully constructive interference: left reflection (a, c) and transmission (b, d) spectra of the DBR FP resonator with the PT-SBO grating inside the cavity and of the DBR FP resonator without PT-SB (b, d) and with an amplifying waveguide ( $\sigma = -12 \mu\text{m}^2$ ). The structure parameters are:  $d = 0.5 \mu\text{m}$ ,  $L_1 = L_2 = 2000d = 1 \mu\text{m}$ ,  $n_1 = n_2 = 1.27 \mu\text{m}^{-1}$ ,  $L_{PT} = 2000d = 2000 \mu\text{m}$ ,  $\Lambda_{PT} = 32.67 \mu\text{m}$ ,  $d_1 = 100\Lambda = 50 \mu\text{m}$ ,  $d_2 = 1000.5d = 500.25 \mu\text{m}$ . The inset in (a) shows the reflection spectra of the left (blue), right (red) and PT-symmetric Bragg grating (magenta).

## Unique optical characteristics of a Fabry-Perot resonator with embedded *PT*-symmetrical grating

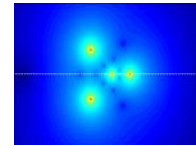
Mykola Kulishov,<sup>1\*</sup> Bernard Kress,<sup>2</sup> and H. F. Jones<sup>3</sup>



<http://arxiv.org/ftp/arxiv/papers/1505/1505.01391.pdf>

## Analysis of unidirectional non-paraxial invisibility of purely reflective *PT*-symmetric volume gratings

Mykola Kulishov,<sup>1\*</sup> H.F. Jones,<sup>2</sup> and Bernard Kress<sup>3</sup>



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- Unidirectionality of plane-wave coupling
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- Kulishov's proposals :  
single-sided mirrors, strange cavities, memories
- **WGM lasers**
- Fano & EIT

## Coupled Laser studies related to PT symmetry

(beyond the caveat « infinite transmission »)

PRL 108, 173901 (2012)

M. Lierzter,<sup>1,\*</sup> Li Ge,<sup>2</sup> A. Cerjan,<sup>3</sup> A. D. Stone,<sup>2</sup> H. E. Türeci,<sup>2,4</sup> and S. Rotter<sup>1,†</sup>

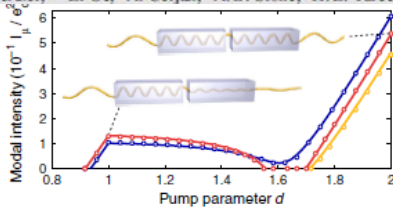
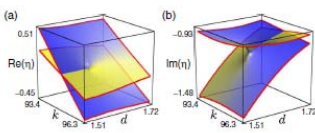


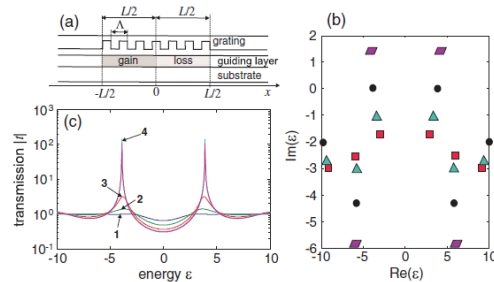
FIG. 1 (color online). Intensity output of a laser system consisting of two 1D coupled ridge lasers, each of length 100  $\mu\text{m}$  with an air gap of size 10  $\mu\text{m}$  and an (unpumped) index of refraction  $n = 3 + 0.13i$ . For  $0 < d < 1$ , the pump in the left ridge is linearly increased in the range  $0 < D < 1.2$ , and, for



Stefano Longhi

PRL 105, 013903 (2010)

PHYSICAL REV



Non-Hermitian Dirac equation and its optical realization.—Let us consider the Dirac equation in one spatial



Won-Tien Tsang, one of the three inventors of the cleaved coupled-cavity laser, prepares

Bell Lab patent 1965  
Tsang 1984  
C3 laser  
(Coupled cavity laser)

## Symmetry-breaking scanned by means of Variable Coupling

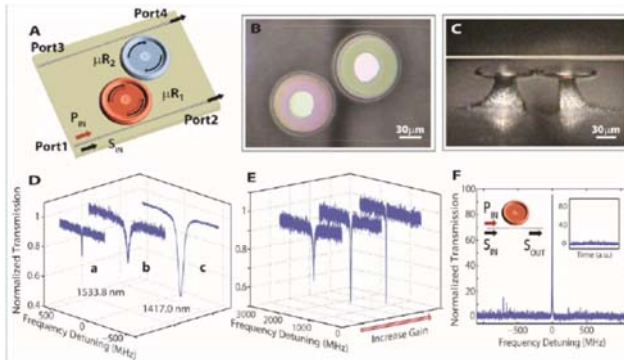


Fig.1. Concept of the PT-symmetric WGM microcavities. (A) The system consists of two directly coupled WGM resonators, and two fiber-taper waveguides.  $\mu R_1$ : active  $Er^{3+}$ -doped silica microtoroid.  $\mu R_2$ : passive silica microtoroid.  $P_{in}$ : pump laser in 1460 nm band to excite  $Er^{3+}$  ions which provide gain in the 1550 nm band.  $S_{in}$ : probe light (signal) in the 1550 nm band.

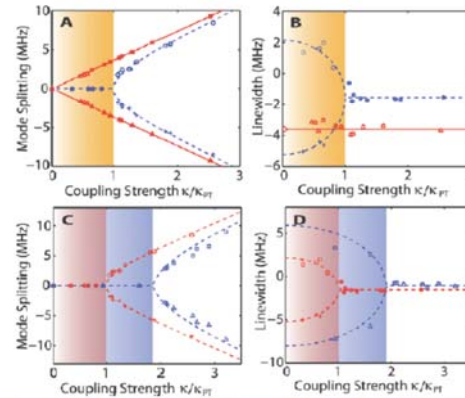
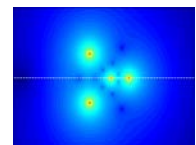


Fig.2. Experimentally observed mode-splitting and linewidth-difference of the supermodes in the coupled-microresonator system as a function of coupling strength  $\kappa$ . Mode-splitting (A&C) and linewidth (B&D) variation correspond to the difference between the real parts and changes in the imaginary parts of the eigenfrequencies, respectively. (A&B) Comparison when resonators are passive (no gain in  $\mu R_1$ ; red square and triangular marks) with  $Q$  factors  $2.9 \times 10^7$  and  $3.0 \times 10^7$ , respectively, for  $\mu R_1$  and  $\mu R_2$ , and when one resonator is active and the other is passive (with gain in  $\mu R_1$ ; blue circular and cross marks). (C&D) Effect of the initial  $Q$ -factor (loss) of  $\mu R_2$  on the eigenfrequencies. Two resonance modes with  $Q$ -factors  $2.0 \times 10^7$  (blue) and  $3.0 \times 10^7$  (red) are chosen for  $\mu R_2$ . Shaded regions correspond to the broken-PT-symmetric region when gain and loss are balanced.

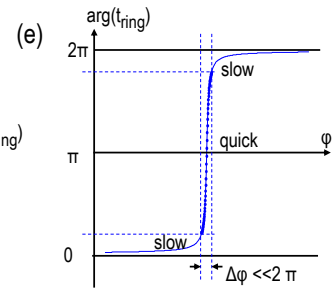
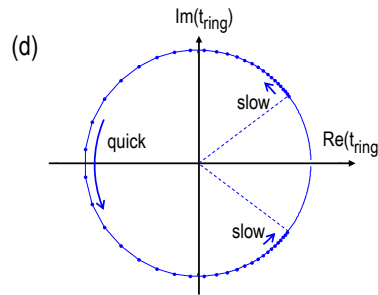
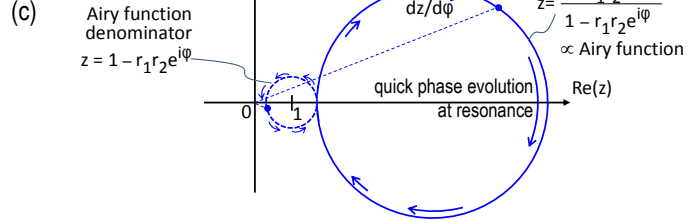
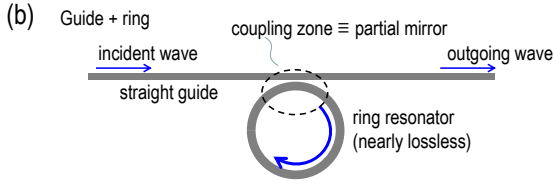
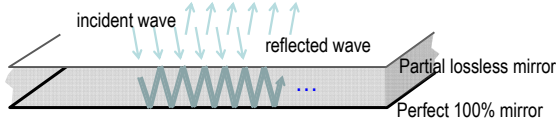
## PT-symmetry and Waveguides / (1) Waveguides & Bragg structures



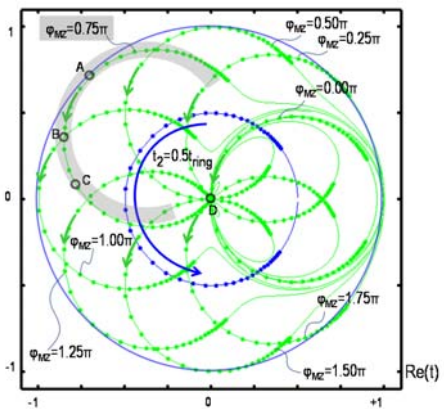
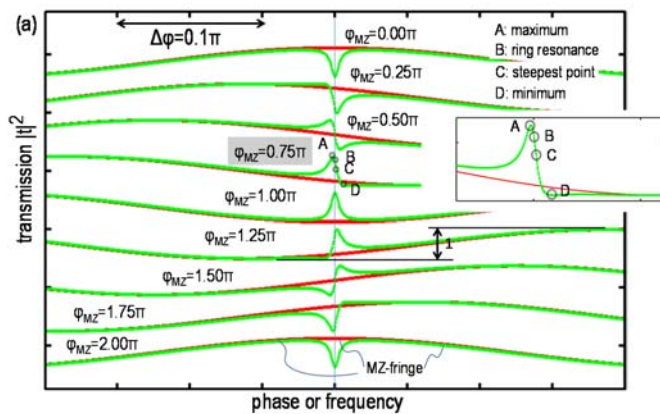
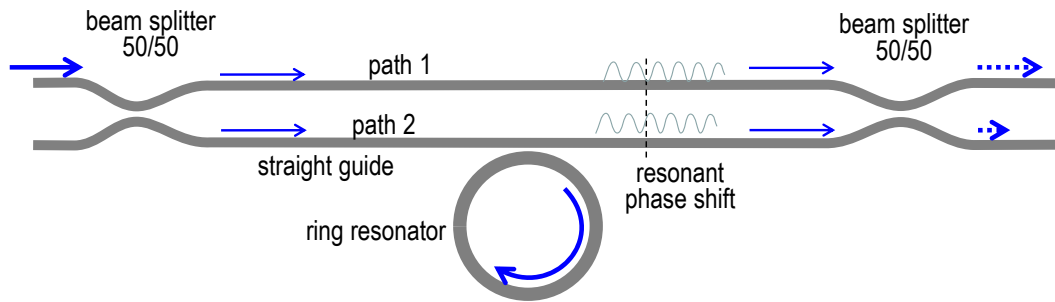
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- **Fano & EIT**

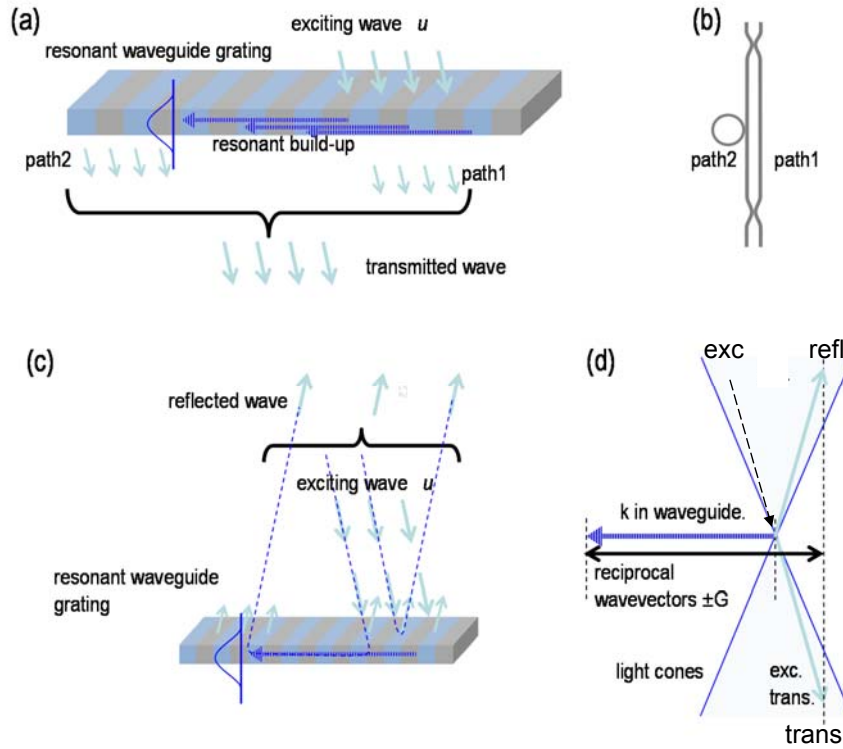
(a) FP with 100% mirror  $\equiv$  Gires-Tournois interferometer



## Fano = 3 continuum ports + 1 resonance



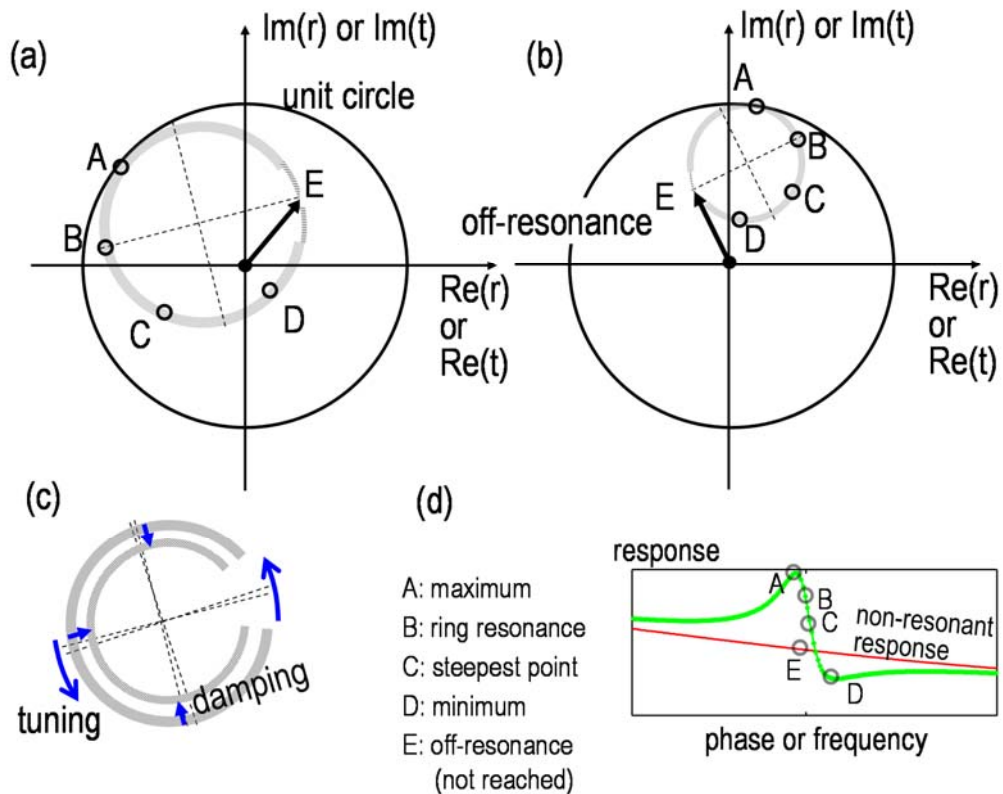




Fano, Poles picture and CMT

Bridging pole and coupled wave formalisms for grating waveguide resonance analysis and design synthesis

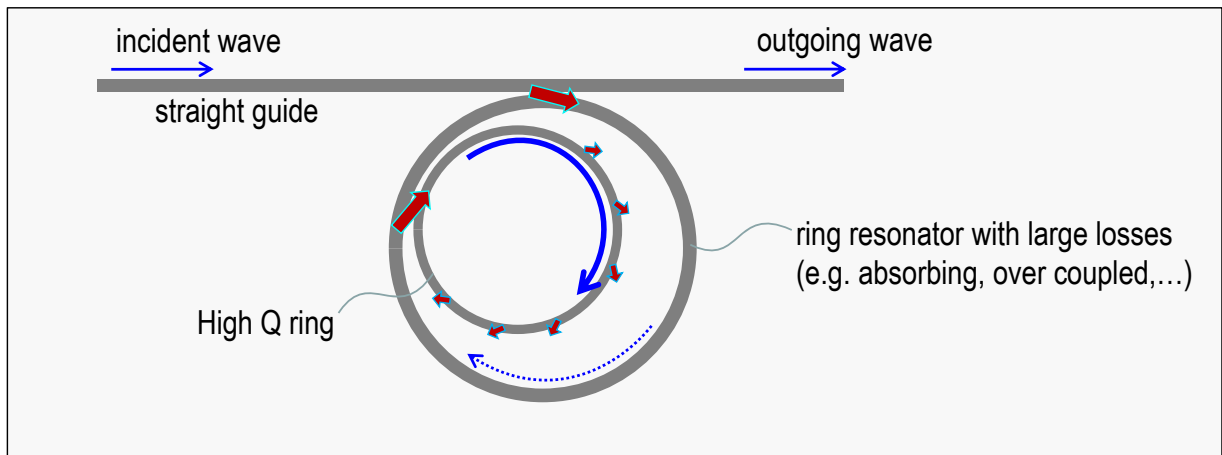
*Pietroy et al. OE, 15, 9831, 2007*



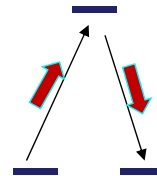
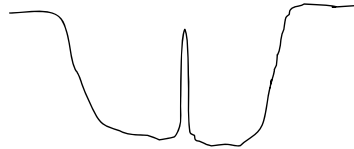
# EIT (Electromagnetically Induced Transparency)

(historically: a linear phenomenon of atom physics)

...albeit a nonlinear optical phenomenon : lasers intensities are coupling constants for atoms)



KEY ? equal transfers across lossy resonator:



## PT-symmetry and Waveguides / (3) Waveguides & Bragg structures

### Conclusion

- *Microscopic view of Reflectivity-asymmetry in basic PT-symmetric Bragg structures*
- *Many possible implementations investigated (planar, guided, organics, semiconductors)*
- *Trove of concepts*
  - from « PT outsiders », (e.g. Kulishov)
  - from metamaterials (here e.g. Jensen Li)
  - Around lasing and coupled lasers (thus good scientific « friction »)